

Max Planck, Kiel and the beginning of the quantum era

Michael Bonitz

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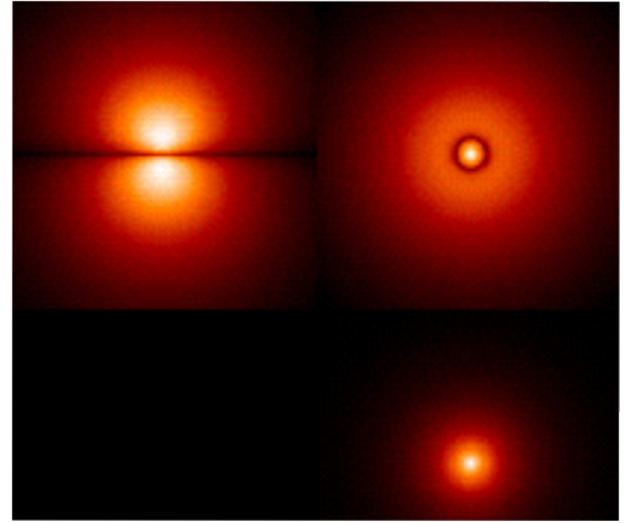
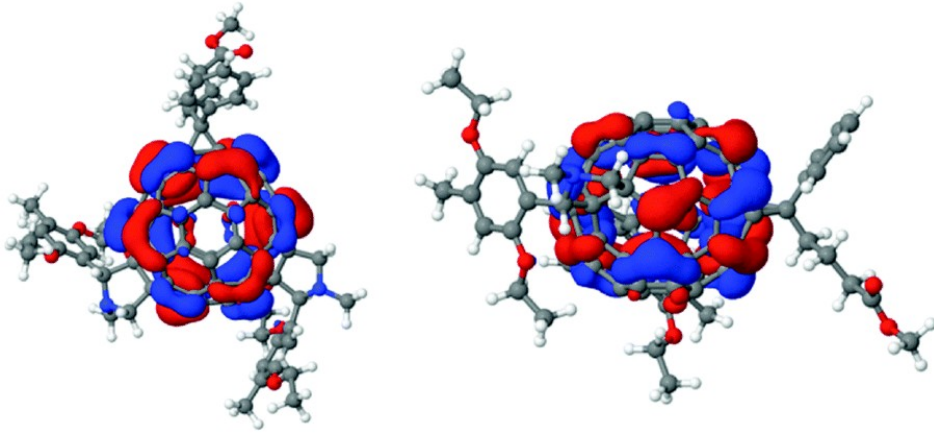
Chair „Statistical Physics“

www.itap.uni-kiel.de/theo-physik/bonitz

Lund, December 2025

Atoms and molecules

lowest hydrogen atom orbitals
(analytical results)



DFT result for 3 LUMO frontier orbitals for the most probable PPCBMB adducts, phenyl-C61-butyric acid methyl ester,
Stephen *et al.*, Chem. Commun. 2016

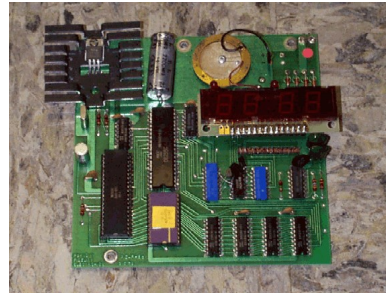
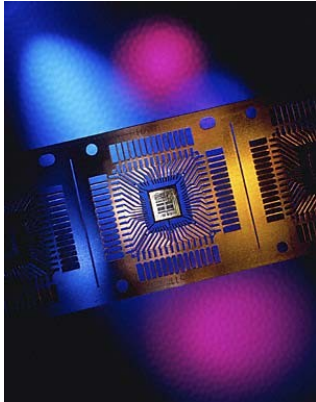
Quantum physics today

The basis for the description of atoms, molecules, nuclei, elementary particles...

The basis for modern (quantum) chemistry, material science

The basis for electronic conduction: from nanotechnology to electrical engineering

Nanotechnology



“Max Planck, Kiel and the beginning of the quantum era”, M. Bonitz, 2025

Quantum physics today

The basis for the description of atoms, molecules, nuclei, elementary particles...

The basis for modern (quantum) chemistry, material science

The basis for electronic conduction: from nanotechnology to electrical engineering

The basis for understanding the Universe and its history

Quantum physics – a „gold mine“:

Recent Nobel prizes in physics

2025: Macro quantum effects: Clarke, Devoret, Martinis

2023: attosecond pulses (atomic physics): L'Huillier, Agostini, Krausz

2022: entangled photons: Aspect, Clauser, Zeilinger

2018: optical tweezer, High intensity lasers: Ashkin, Mourou, Strickland

2016: Topological phase transitions in 2D: Thouless, Kosterlitz, Haldane

2015: Neutrino Oscillations: Kajita, Mc Donald

2014: blue LEDs: Akasaki, Amano, Nakamura

2013: Higgs boson: Englert, Higgs

Vast majority of areas in physics

Also chemistry nobel prizes for quantum chemistry (physics)

2025

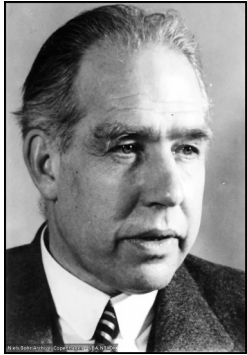


$$i\hbar \frac{\partial}{\partial t} \psi(\underline{r}, t) = \left[-\frac{\hbar^2}{2m} \nabla^2 + V(\underline{r}) \right] \psi(\underline{r}, t)$$

100 years of Heisenberg's/Schrödinger's equation

honoring the „fathers“ (and „mothers“) of quantum mechanics,
in particular: Bohr, Schrödinger, Heisenberg, Born, Pauli, Dirac, Fermi...

2025



Niels Bohr (1947):
one „researcher **who created the
foundation on which we all work today**“



Outline

1. Quantum physics today
2. Max Planck and Kiel
3. Planck and the discovery of elementary quanta
4. The Quantum universe: from atoms to galaxies
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2. Max Planck.

Childhood in Kiel, 1858-1867

Born in Kiel, 23. April 1858

Father Julius Wilhelm Planck (1817-1900), law professor in Kiel

Mother Emma Planck, (born Patzig)

Uncle Gottlieb Planck (1824-1907), lawyer

Grandfather Gottlieb Jakob Planck (1751-1833), theologist



Parents

Max with brothers
and sister, 1862



Max Planck's family moves to Munich

German/Austrian-Danish War Februar-October 1864

for the duchies Holstein, Saxe-Lauenburg,
and Schleswig

Reason: passing of the November
Constitution, which integrated the Duchy of
Schleswig into the Danish kingdom in
violation of the London Protocol

1867: Planck's father under protest
against Prussia leaves Kiel

Max Planck **retains ties to his hometown
and state** throughout his life



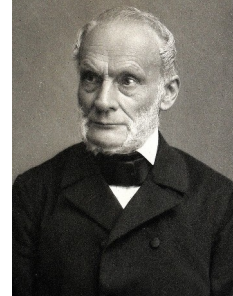
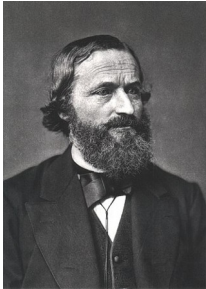
Map: Maximilian Dörrbecker (Chumwa)

Max Planck studies physics

School in Munich: 1867-1874

University: 1874-1879, Munich and Berlin

Lectures by Helmholtz, Kirchhoff, Weierstraß; Self-education: Clausius



Planck was fascinated by theoretical physics, in particular, Clausius' thermodynamics

Continue in Theoretical Physics?

Advice from Prof. Philipp von Jolly*, in Munich, 1877

*„Theoretical Physics is **close to completion**,
... similar as geometry is long complete.“*

*„in some „corners“ there might be a few tiny „dust grains“ left to
explore and categorize, but the system as a whole is well founded.“*



*view of an experimentalist

Planck, Naturwiss. **13**, 52-59 (1925)

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Planck: *„I do not desire to discover new ground, but only
to understand the existing fundamentals of the physical science
and, possibly, to deepen them“*



*view of an experimentalist

Planck, Naturwiss. **13**, 52-59 (1925)

Graduation in physics

PhD thesis 1879: on 2nd law of thermodynamics

Habilitation 1880

No response or recognition from the experts.

Privatdozent: 1879-1885, Munich, unpaid lectures, no position

1885: „Relief“ - Professor in Kiel

1886: Max Planck founds a family

marries his girlfriend from childhood, Marie Merck

the couple has 4 children:

- 1888: son Karl
- 1889: twins Emma, Grete
- 1893: son Erwin



Scientific results in Kiel

Important papers in Kiel: on thermodynamics

- *"Über das Prinzip der Vermehrung der Entropie"* (3 papers)
- *"Über die molekulare Konstitution verdünnter Lösungen"*
- *"Das chemische Gleichgewicht in verdünnten Lösungen"*
- *"Über die Hypothese der Dissoziation der Salze in sehr verdünnten Lösungen"*
- *"Über die Dampfspannung verdünnter Lösungen flüchtiger Stoffe"*
- *"Zur Theorie der Thermoelektrizität in metallischen Leitern"*

1887: wins 2nd prize in Göttingen theory challenge
(supported Helmholtz' ideas against W. Weber)

1889: offer to Berlin University (successor of G. Kirchhoff beating L. Boltzmann),
Then center of physics, Planck stays at the university until 1926

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Theoretical physics around 1875

Electrodynamics

Electrical and
magnetic processes, electromagn.
waves, etc.
(Maxwell's eq-s)

Mechanics

dynamics of bodies,
liquids, and planets,
elastic media
(Newton's laws)

Thermodynamics

Heat, gases,
heating and cooling
machines
(1st and 2nd law)

Theoretical physics around 1875

Radiation
of moving
bodies



Black-body
radiation

ether

Mechanics

phlogiston

Electrodynamics

Thermodynamics

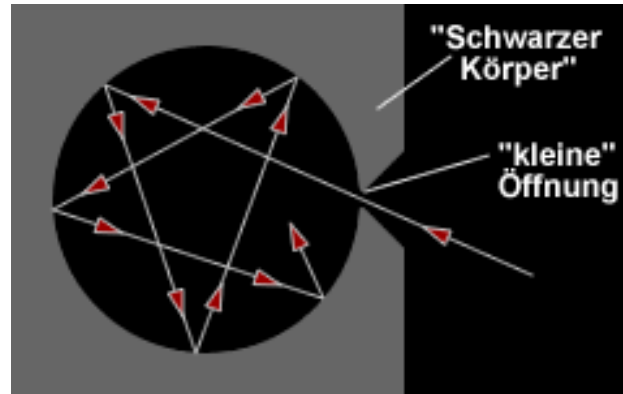
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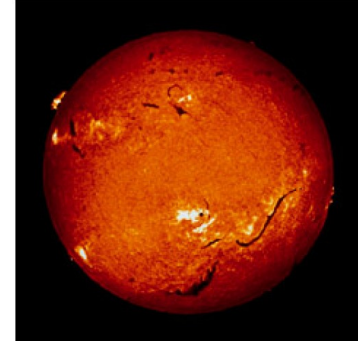
Max Planck and black-body radiation

1860: Gustav Kirchhoff formulates model of „black body“:
EM waves in resonator in **TD equilibrium**



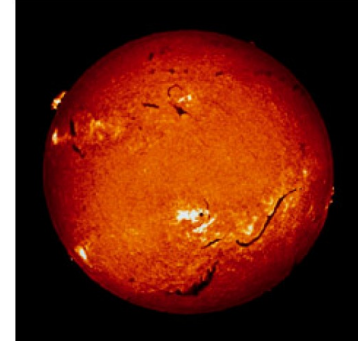
1894: Berlin – Experimentalists at PTR A produce new data at longer λ
– successful theory of W. Wien
– Planck starts to look for his own thermodynamic approach

Every body radiates, only T matters



universal relation between color and temperature (W. Wien)

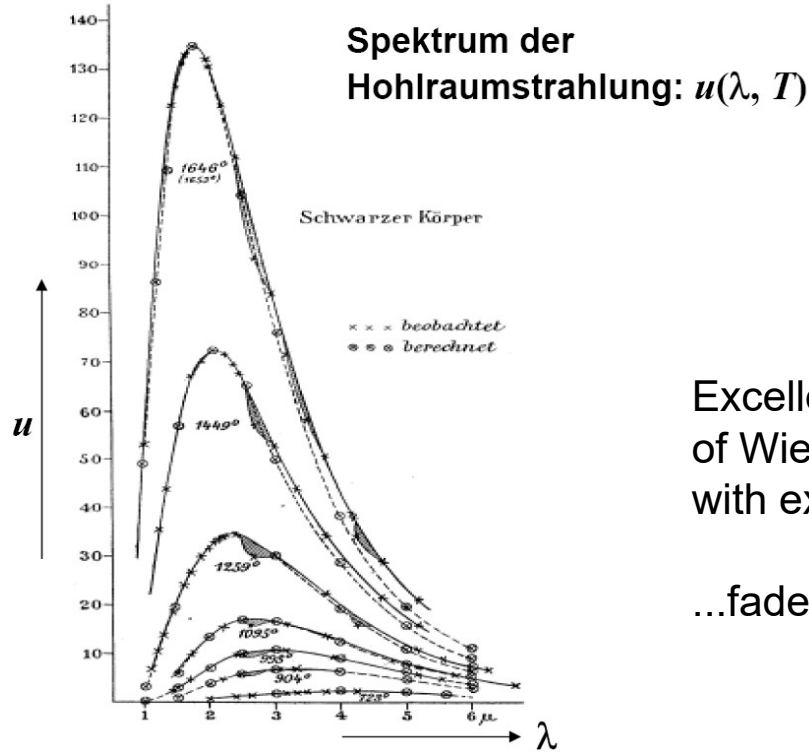
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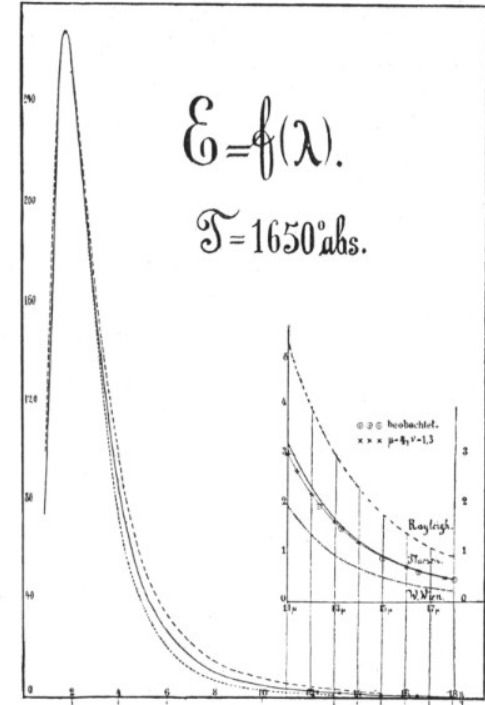
New accurate experimental data in the far infrared



Messung von Lummer und Pringsheim (1900)

Excellent agreement
of Wien's theory
with experiment...

...fades at large λ



modern textbooks: „Planck resolves ultraviolet
catastrophe, interpolates...” ... *pure fiction*

Planck finds the radiation law

I. Wien-Formel
(große Frequenzen)

$$U(\beta) = b e^{-a\beta}$$

$$R = \left(\frac{d^2 S}{dU^2} \right)^{-1} = -aU$$

II. Rayleigh-Rubens Gesetz
(kleine Frequenzen)

$$U(\beta) = \frac{d}{\beta}, \quad \beta = 1/kT$$

$$R = -U^2 / d$$

Kombination: $R = -aU - U^2 / d$

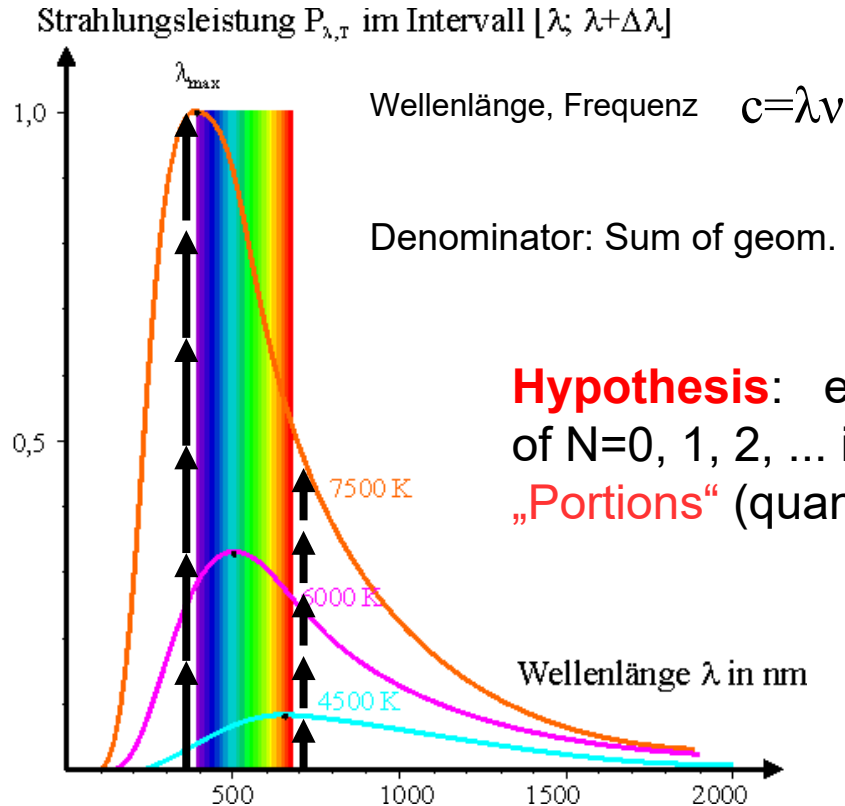
Integration: $\frac{dS}{dU} = \beta(U) = \frac{1}{a} \ln \left[1 + \frac{ad}{U} \right]$

Auflösen nach U:

$$U(\beta) = \frac{ad}{e^{a\beta} - 1}$$

DPG Berlin,
19.10. 1900

Plancks derivation of the radiation law



$$\rho(\lambda, T) = \frac{8\pi ch}{\lambda^5} \frac{1}{e^{hc/kT\lambda} - 1}$$

$$U_\nu = N_\nu \cdot \underline{\varepsilon_\nu} = N_\nu \cdot \underline{h\nu}$$

DPG Berlin, **14.12. 1900**
„Birthday of quantum theory“

Planck computes the entropy of radiation

Integration of the combined R yields:

$$\left. \frac{dS}{dU} \right|_{V,N} = \frac{1}{a\nu} \ln \left(1 + \frac{h\nu}{U} \right) \equiv \frac{1}{T},$$

$$S = \frac{h}{a} \left[\left(\frac{U}{h\nu} + 1 \right) \ln \left(\frac{U}{h\nu} + 1 \right) - \frac{U}{h\nu} \ln \frac{U}{h\nu} \right]$$

Derivation via partition function of (discrete) random process (*a la* Boltzmann): $S = k_B \ln Z_\mu$

model: N identical oscillators containing

P equal energy portions (P, N large):

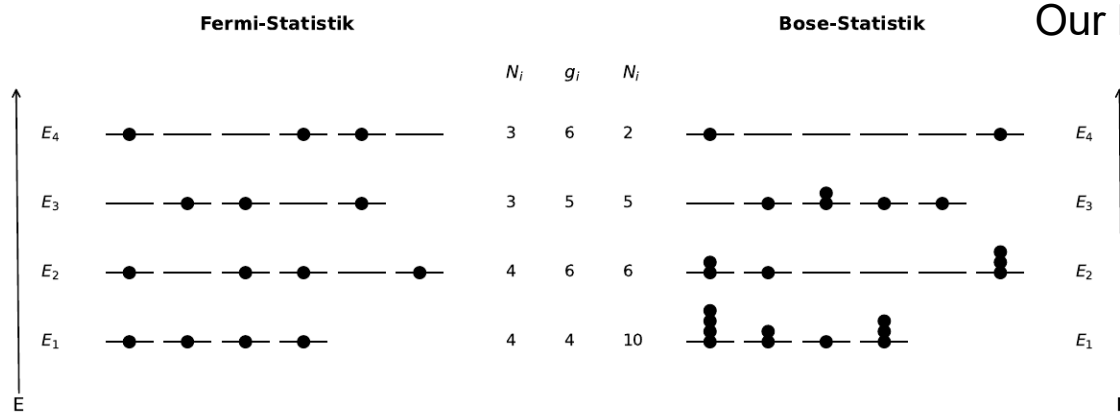
$$U_N = N \cdot U = P \cdot \epsilon$$

$$Z_\mu = \frac{(P+N)!}{P!N!} \approx \frac{(P+N)^{P+N}}{P^P N^N}$$

$$S = k_B \left\{ \left(\frac{P}{N} + 1 \right) \ln \left(\frac{P}{N} + 1 \right) - \frac{P}{N} \ln \frac{P}{N} \right\}$$

$$\frac{1}{k_B} S_N = \frac{N}{k_B} S$$

Planck discovered the N-body Bose system



Our knowledge of Fermi/Bose statistics

$$Z_{\mu,i}^B = \frac{(N_i + g_i - 1)!}{N_i! (g_i - 1)!}$$

$$\frac{1}{g_i} \frac{S_{\mu,i}^B}{k_B} = \left(1 + \frac{N_i}{g_i}\right) \ln \left(1 + \frac{N_i}{g_i}\right) - \frac{N_i}{g_i} \ln \frac{N_i}{g_i}$$

Entropy of Bose gas

Abbildung 6.14: Besetzungszahlen N_i der Energiezustände E_i , die g_i -fach entartet sind, für Fermionen links und für Bosonen rechts. Die Zahl N_i der Teilchen auf Energieniveau E_i kann bei Fermionen g_i nicht übersteigen (Pauli-Prinzip), für Bosonen ist sie nur durch die Gesamtteilchenzahl begrenzt. Abb.: C. Makait. M. Bonitz, „Statistical Physics“. Lecture notes

$$U_N = N \cdot U = P \cdot \epsilon$$

$$S = k_B \left\{ \left(\frac{P}{N} + 1 \right) \ln \left(\frac{P}{N} + 1 \right) - \frac{P}{N} \ln \frac{P}{N} \right\}$$

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Broad scepticism against Planck's quanta

- Striking contradiction to radiation laws of classical electrodynamics
- Criticism from Rayleigh, Jeans, Ehrenfest, H.A. Lorentz and many other theoreticians
- Planck remained skeptical himself

1911: Nobel prize for Wilhelm Wien,
"for his discoveries regarding the
laws governing the *radiation of heat*"



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Gradual confirmation of concept of elementary quanta

- 1905 Einstein: theory of photoelectric effect
- 1907 Einstein, Debye 1912: theory of heat capacity of solids
- 1908 Rutherford, Geiger: measurement of elementary charge
- 1913 Bohr: „planetary“ model of hydrogen atom

1919: Nobel prize for Max Planck (for 1918)

„for his work on the establishment and development
of the theory of elementary quanta“

Planck's „theoretical conclusion stands in very sharp opposition to our earlier concept of the radiation phenomenon. Experience had to provide powerful confirmation, therefore, before Planck's radiation theory could be accepted. In the meantime this theory has had unheard-of success.“

A.G. Ekstrand, President of the Royal Swedish Academy of Sciences, 1. June 1920

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„Planck's radiation theory is, in truth, the most significant lodestar for modern physical research, and it seems that it will be a long time before the treasures will be exhausted which have been unearthed as a result of Planck's genius.“

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1925-28: Quantum mechanics

Systematic mathematical theory (initiated by Planck 1900)

Bohr, DeBroglie, Heisenberg, Schrödinger, Born,
Jordan, Sommerfeld, Fermi, Dirac, Born, Einstein, Pauli u.v.a.

basis of our picture of the Micro world
excellent agreement with experiments

Universe

classical

quantum

EM
radiation



Light

continuous „flow“ of
EM field energy

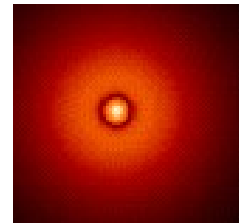
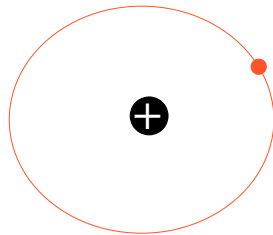
EM field energy composed
of discrete quanta

Micro particles

discrete point particles

continuously distributed particles

Electron

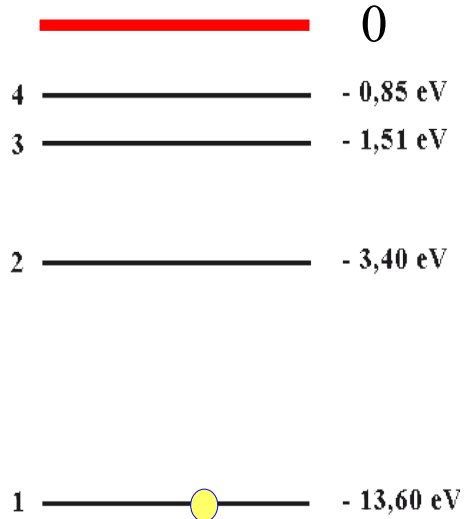


Atom

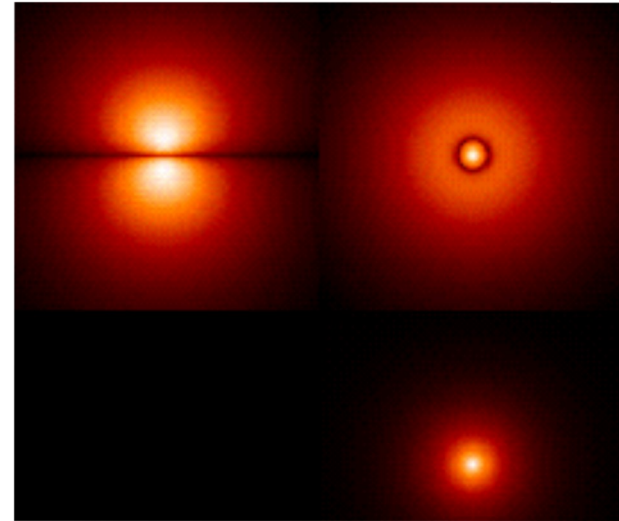
Quantum mechanics

Strict mathematical description of electrons, **Atoms**, Molecules

Energy of electrons
quantized



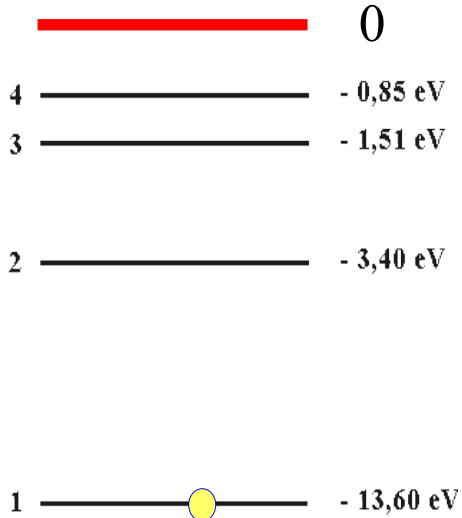
Example: hydrogen atom



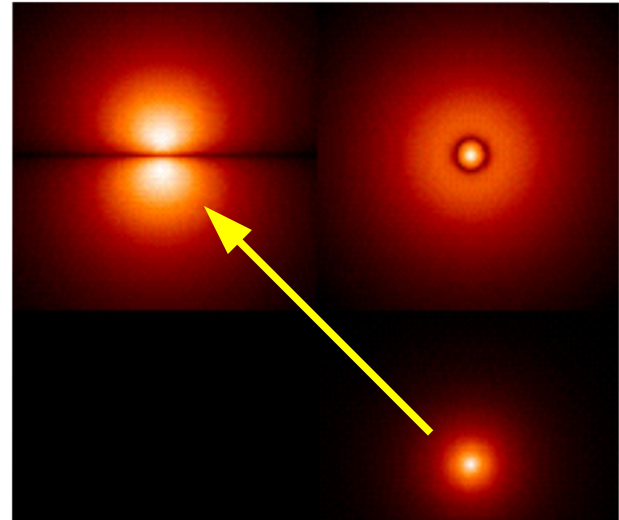
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Strict mathematical description of electrons, **Atoms**, Molecules

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quantized



Example: hydrogen atom



Quantum mechanics

Strict mathematical description of electrons, **Atoms**, Molecules

→ *Videos*: solution of
Schrödinger equation
Sebastian Bauch

Freies Elektron

Elektron an Hindernis

Quantenphysik an der CAU

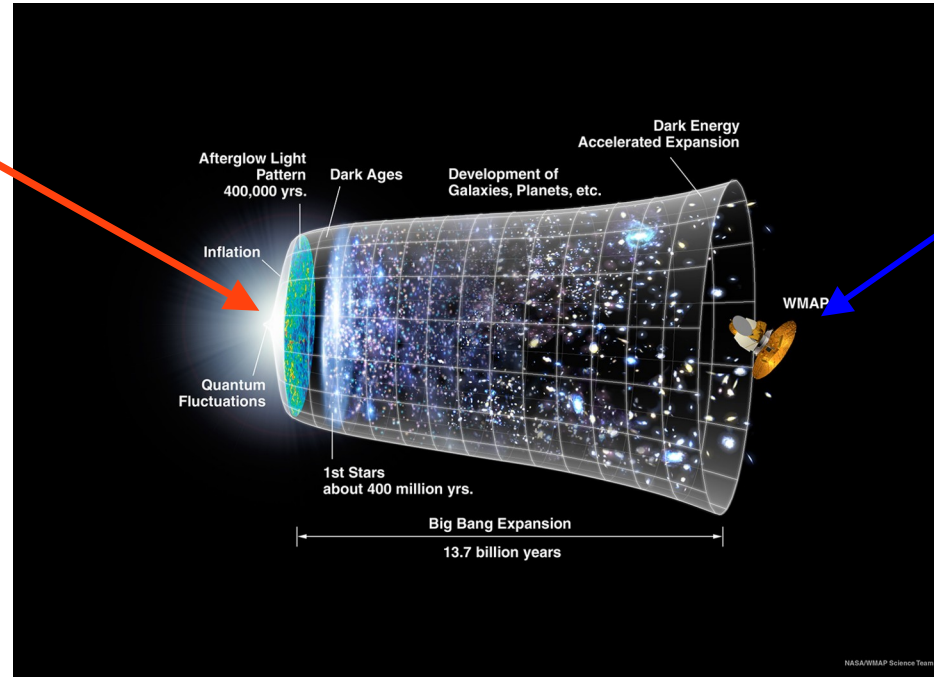
Quantum effects on cosmic scales

Expansion, cooling, condensation

Big
bang

time

today



Discovery of cosmic Microwave background

1964: Penzias, Wilson



Measurement of cosmic radio waves

Expansion and cooling $3000\text{K} \rightarrow 2.73\text{K}$
Wave lengths increases by factor ~ 1000

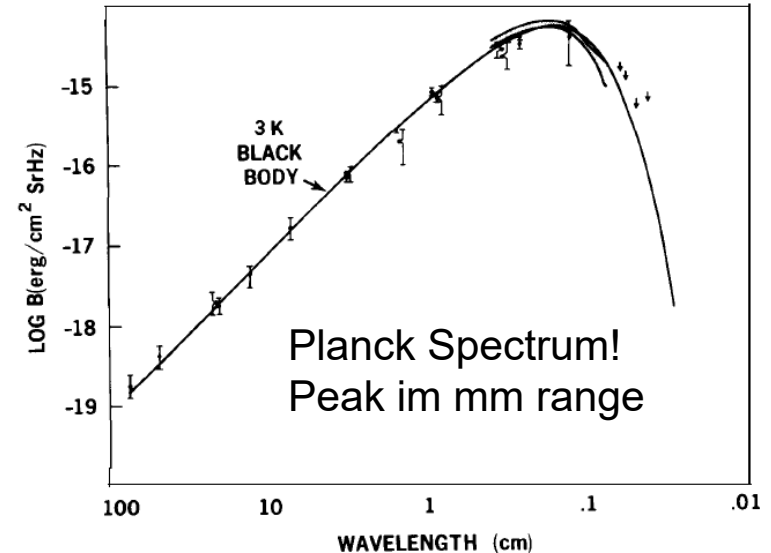
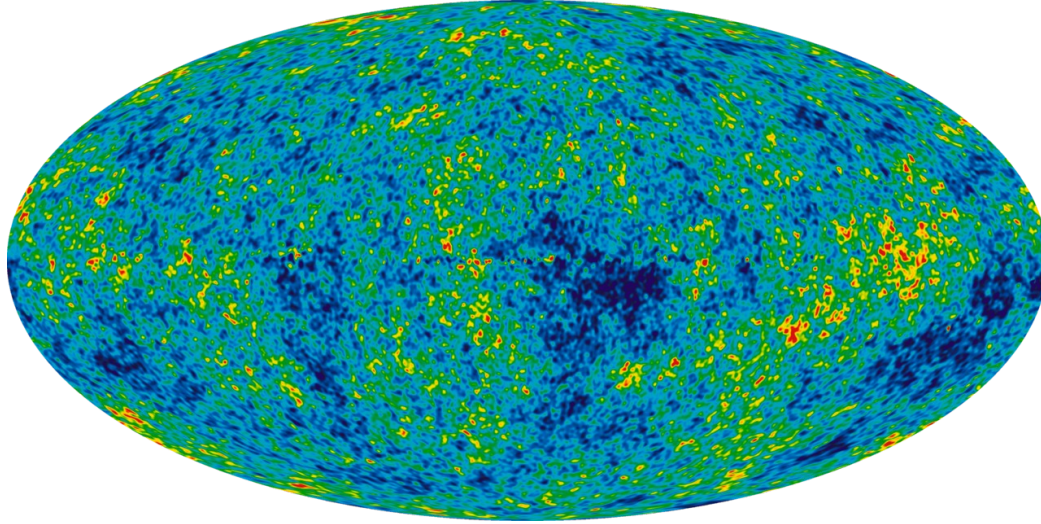


Fig. 12 Measurements of the spectrum of the cosmic microwave background radiation.

Fig.: Wilson, Nobel lecture 1978

A window into the Universe 13.7 billion years ago!



source: Wikipedia

2006: Physics Nobel prize for Mather and Smooth, COBE satellite (1989-93)

today: Satellites measure anisotropy, mass distribution etc., WMAP (2001-10), Planck (2009-13)

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Max Planck: tragic personal life

- 1909 **death of wife** Marie
- 1911 marriage with Marga von Hoeßlin,
Son Hermann (1911-1954, mentally ill)
- Death of three children within 3 years
 - **Son Karl: died** in 1916 in World War I
 - **daughter Grete died** 1917 when giving birth
 - **daughter Emma died** 1919 when giving birth



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World War II: Planck stayed in Nazi Germany (conservative, loyal, patriot)

- 1943, October: during a lecture in Kassel Planck barely survived bombing of the city
- 1944: Planck's house in Berlin was bombed, he lost everything
- 1945, Jan. 23.: **son Erwin executed** (participant in Hitler assassination attempt
of Stauffenberg and others)
- May 1945: brought from Rogätz (near Magdeburg) to Göttingen (Kuipers)
- Oct 4 1947: Planck dies in Göttingen (89 years old)

Planck's public activities (selection)

- permanent Secretary of Prussian Academy of Sciences (1912/38)
- Rector of Berlin University (1913/14), supported Einstein, many colleagues
- President of German Physical Society (4 times, 1905-09, 1915-16)
- President of Kaiser-Wilhelm-Society (1930-37)

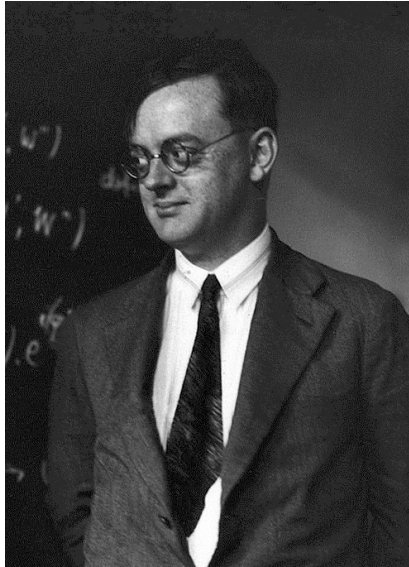
- many public lectures about science, ethics, philosophy

highly respected among scientists world-wide
well known to the general public

Influenced several generations of scientists
Impressively documented in the **Max-Planck estate in Kiel**

Planck in the words of colleagues

condolence letter to Marga Planck, 1947*



Pascual Jordan
1902-1980 (Wikipedia)

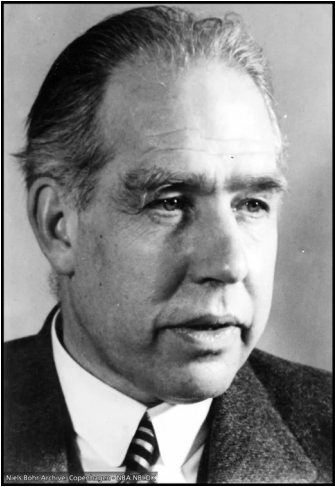
„...I personally am indebted to him - as are most of the physicists of my generation – for the entire content and the entire purpose of my own scientific life's work...“



*C. Pitschellis, E. Schroedter, and M. Bonitz (2024)
English: R. Lackner, P. Ludwig, and M. Bonitz (2025)

Planck in the words of colleagues

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Niels Bohr, Nobel prize
1922 (Wikipedia)

„...The deep impression of his splendid and pure personality is one of my most treasured experiences, and I will always remember with gratitude the friendship which he extended to me for many years...”



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Max Born, Nobel prize
1954 (Wikipedia)

„...It is impossible for me to express what I have lost through the death of your husband. I owe him my scientific development and my career; above and beyond that, he was a sterling example of noble humanity for me....."



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Liese Meitner
(1878-1958)
In Washington DC 1946

„...Your husband's life was unusual, as he himself was unusual, with his wonderful, pure personality, which made everyone who even came near him a better person...."



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Max Planck – conservative patriot and humanist

- Supported the Kaiser at the beginning of WWI, distanced himself later on
- After WWI strong engagement for German science
- 1933: as president of Kaiser-Wilhelm Gesellschaft Planck tries to convince Hitler to abstain from repressing Jewish scientists. Unsuccessful
- Defended DPG and KWG against Nazi indoctrination.
Supported Jewish colleagues and their families (F. Haber, Fam. Rubens u.a.)
- Defended understanding between nations (Dialogue with Francois-Poncet 1938)
- Opposed to public protests or declarations

Max Planck – Respect abroad

- 1946 British scientists celebrated the 300th birthday of Isaac Newton with many international guests
- German scientists (those who had not emigrated) were not invited because they discredited themselves during the Nazi period.

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There was one exception: Max Planck

Laid the foundation for Max Planck society

Planck in the words of German humanists

condolence letter to Marga Planck, 1947*



Elisabeth Schiemann
(1881-1972)

Biologist, part of Resistance
2014: „Righteous among
the nations“

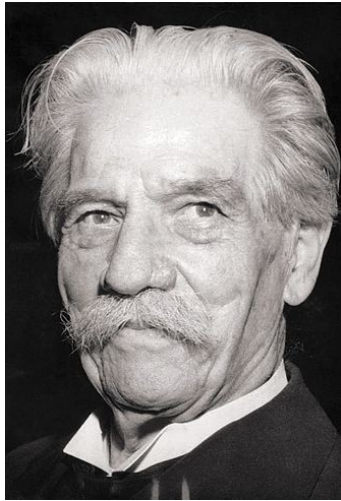
„...For us he was the exponent of the good German conscience throughout all the evil years; and therefore his name, which today is well known in the entire world, will be our best defender, so that we may maintain the belief in a better Germany...”



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Albert Schweitzer
(1865-1948)

Nobel peace prize 1952
1955, © Bundesarchiv

“He represented eternal ethical cultural values in the face of those who attempted to change and devalue them. Thereby he gave comfort and strength in terrible times to many who did not want to take part in the general confusion....

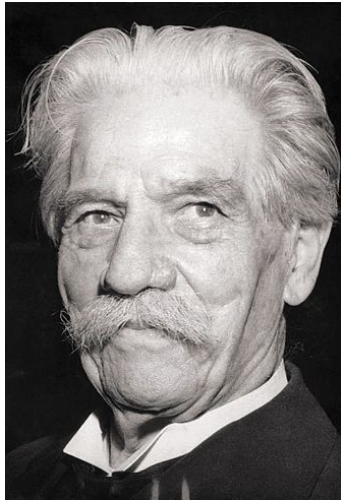


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“Max Planck, Kiel and the beginning of the quantum era”, M. Bonitz, 2025

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Nobel peace prize 1952
1955, © Bundesarchiv

“...In a time when so many learned men showed themselves to be much smaller as human beings, he preserved a most noble humanity and exhibited a quiet imperturbability...”



*C. Pitschellis, E. Schroedter, and M. Bonitz (2024)
English: R. Lackner, P. Ludwig, and M. Bonitz (2025)

“Max Planck, Kiel and the beginning of the quantum era”, M. Bonitz, 2025

Summary and Outlook

„I do not desire to discover new ground, but only to understand the existing fundamentals of the physical science and, possibly, to deepen them“



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Summary and Outlook

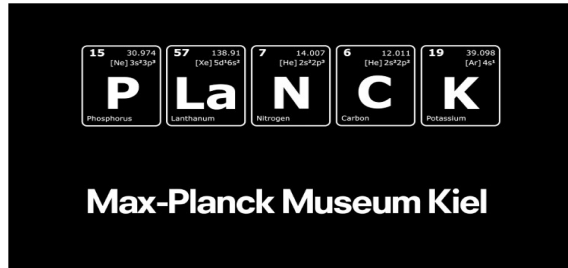


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Quantum theory: Revolution in science, technology –
comparable to Kopernikus, Newton, Darwin
A unique example of scientific discovery and personal integrity
A story that should be kept and told

14.12. 2013 - Opening of a Museum for Max Planck and quantum physics in Kiel



Physikzentrum of CAU Kiel
Presenting Planck's discovery (*after 5 years of struggle*)

14.12. 2013 - Opening of a Museum for Max Planck and quantum physics in Kiel



2 grandgranddaughters of Max Planck – Christine Roos und Cornelia Kulenkampff -
Attended the opening. Support of our museum by the family

Museum for Max Planck and quantum physics



Museum in the Physics Library, Physikzentrum of CAU Kiel today

Support of the Museum by the Planck family: the Planck estate arrives at Kiel



Frank Homann and Patrick
Ludwig, October 8 2020, Kiel



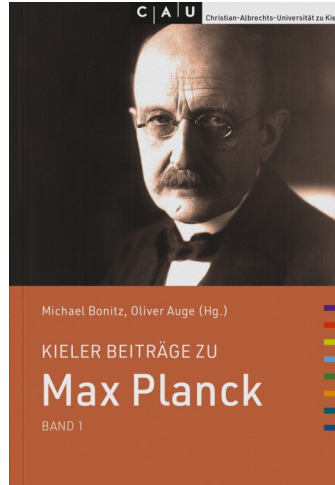
Walhalla, July 15. 2022: Gabriele Taylor,
signs the lease of the estate

Planck estate: first publications

11.12. 2024 Start of
**Open access book series
in CAU-Verlag**

M. Bonitz, O. Auge (Eds.)

vol. 1: M. Bonitz,
"Max Planck, Kiel und der
Beginn der Quantentheorie"



vol. 2: C. Pittschellis, E. Schroedter und M. Bonitz,
„Die Kondolenzen von Wissenschaftlerinnen und Wissen-
schaftlern zum Tode Max Plancks 1947“

Results on display at Museum

In press:

vol. 3: english translation of
condolences

vol. 4: Letters from Liese Meitner
and Max von Laue

In progress:

Digitization of entire estate (2,000
letters, 10,000 pages)

Parts available online:

[Planck-Repositoryum](#)

The future: Max Planck quantum science center

Supported by Planck family, Max Planck foundation,

State of Schleswig-Holstein

Sponsors welcome