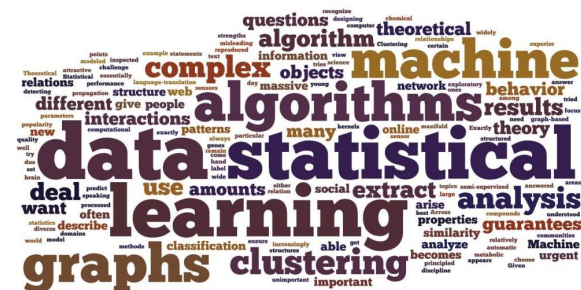


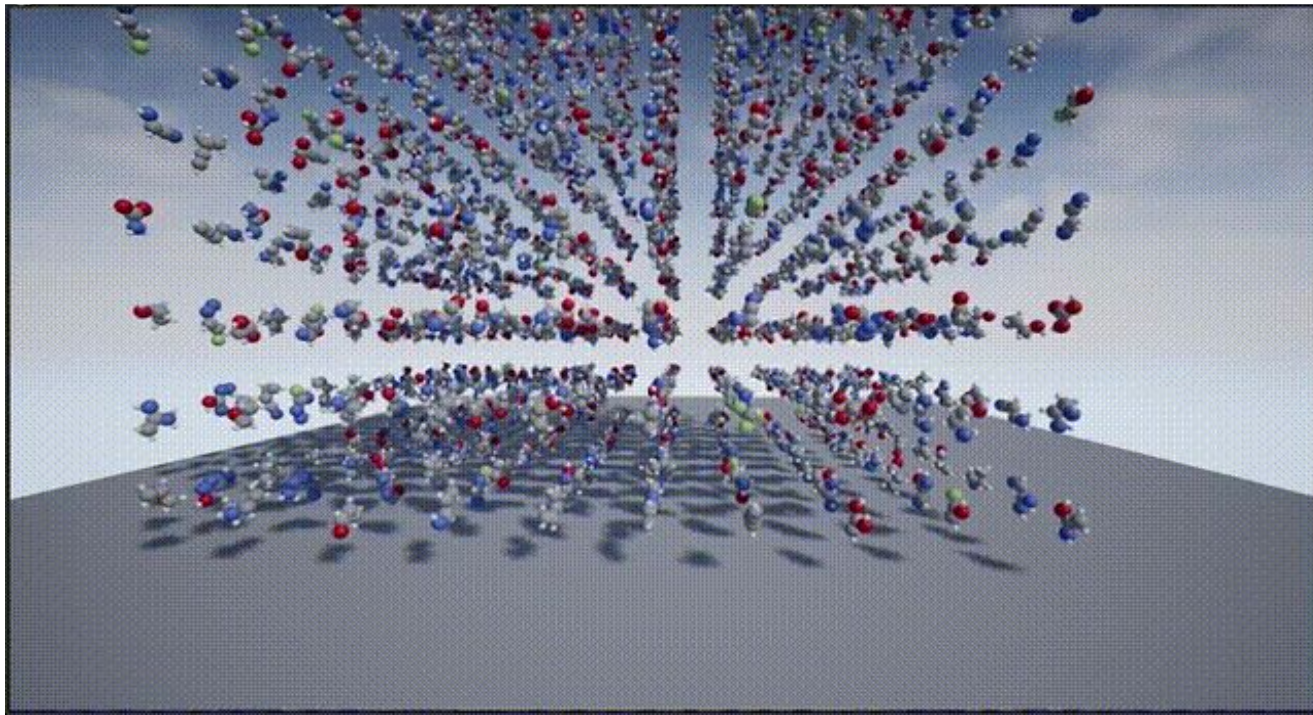
Physics + computer simulation +





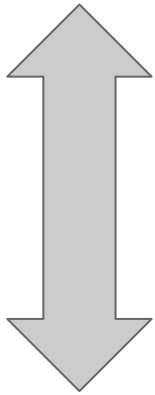
Quantum Machine Learning

'Quantum machine learning using atom-in-molecule-based fragments selected on the fly', Huang, von Lilienfeld, *Nature Chemistry* (2020)



The pillars of science

Theory



Experiment



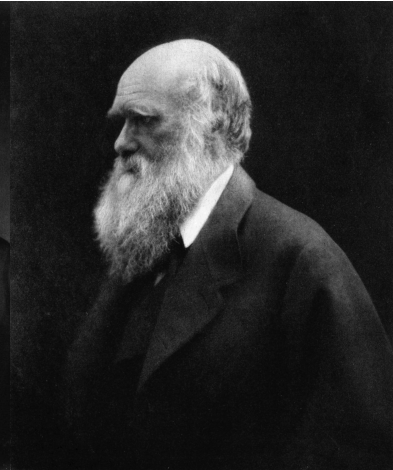
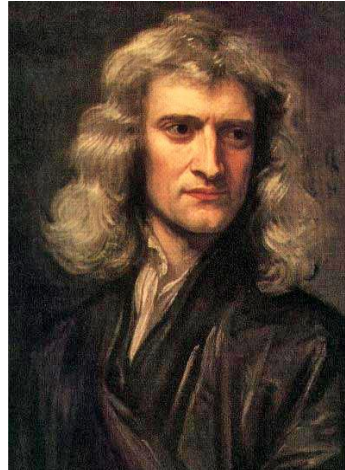
Εὐκλείδης
Eukleidēs



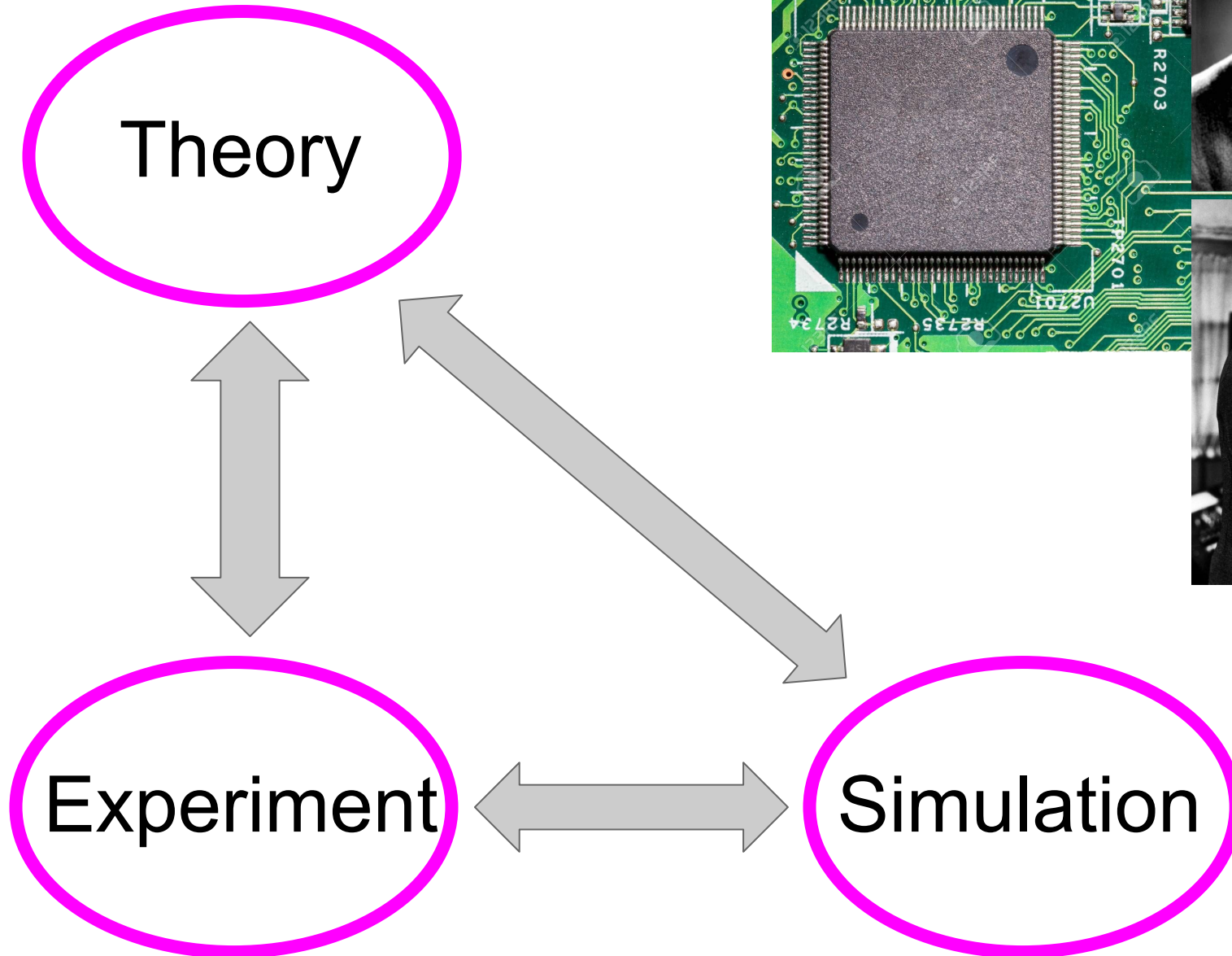
Πυθαγόρας
Pythagóras



Ἀρχιμήδης
Archimedes

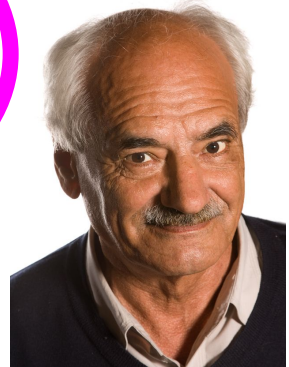


The pillars of science

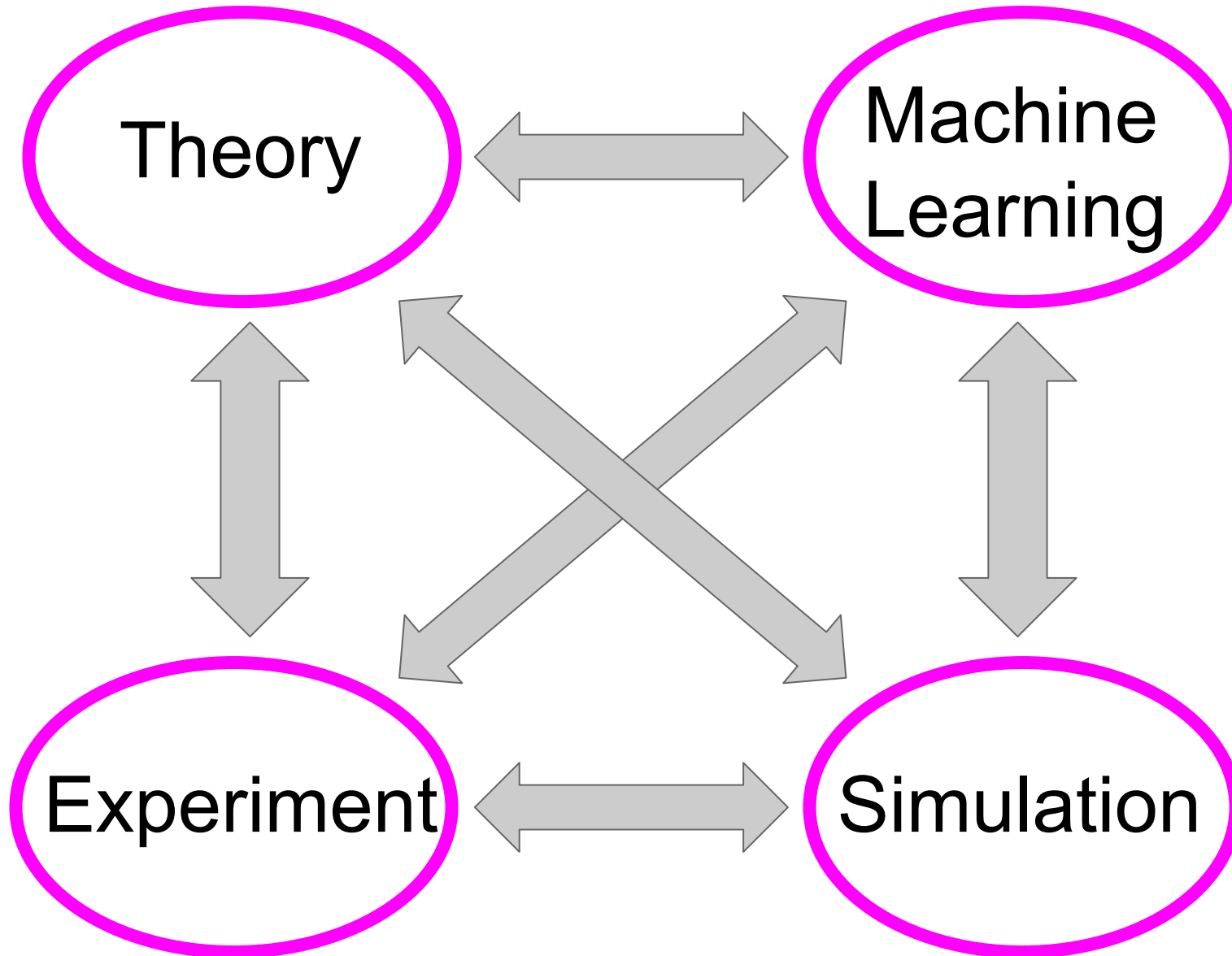


The pillars of science

Vapnik



Chervonenkis



Stoichiometry? → Mendeleev's table, est. in 1879: Well alive and kicking

hydrogen 1 H 1.0079																		helium 2 He 4.0026																	
lithium 3 Li 6.941		beryllium 4 Be 9.0122																boron 5 B 10.811		carbon 6 C 12.011		nitrogen 7 N 14.007		oxygen 8 O 15.999		fluorine 9 F 18.998		neon 10 Ne 20.180							
sodium 11 Na 22.990		magnesium 12 Mg 24.305																aluminum 13 Al 26.982		silicon 14 Si 28.086		phosphorus 15 P 30.974		sulfur 16 S 32.065		chlorine 17 Cl 35.453		argon 18 Ar 39.948							
potassium 19 K		calcium 20 Ca		scandium 21 Sc		titanium 22 Ti		vanadium 23 V		chromium 24 Cr		manganese 25 Mn		iron 26 Fe 55.845		cobalt 27 Co 58.933		nickel 28 Ni 58.693		copper 29 Cu 63.546		zinc 30 Zn 65.39		gallium 31 Ga 69.723		germanium 32 Ge 72.61		arsenic 33 As 74.922		selenium 34 Se 78.96		bromine 35 Br 79.904		krypton 36 Kr 83.80	
THE NEW YORKER														ruthenium 44 Ru 101.07		rhodium 45 Rh 102.91		palladium 46 Pd 106.42		silver 47 Ag 107.87		cadmium 48 Cd 112.41		indium 49 In 114.82		tin 50 Sn 118.71		antimony 51 Sb 121.76		tellurium 52 Te 127.60		iodine 53 I 126.90		xenon 54 Xe 131.29	
														osmium 76 Os 190.23		iridium 77 Ir 192.22		platinum 78 Pt 195.08		gold 79 Au 196.97		mercury 80 Hg 200.59		thallium 81 Tl 204.38		lead 82 Pb 207.2		bismuth 83 Bi 208.98		polonium 84 Po [209]		astatine 85 At [210]		radon 86 Rn [222]	
														hassium 108 Hs [269]		meitnerium 109 Mt [268]		unnilium 110 Uun [271]		ununium 111 Uuu [272]		ununium 112 Uub [277]		ununquadium 114 Uuq [289]											

ews

Books & Culture

Fiction & Poetry

Humor & Cartoons

Magazine

Crossword

Video

Pc

RIES HIDDEN IN THE

TABLE

Alternatives?

William Crookes (1832-1919)

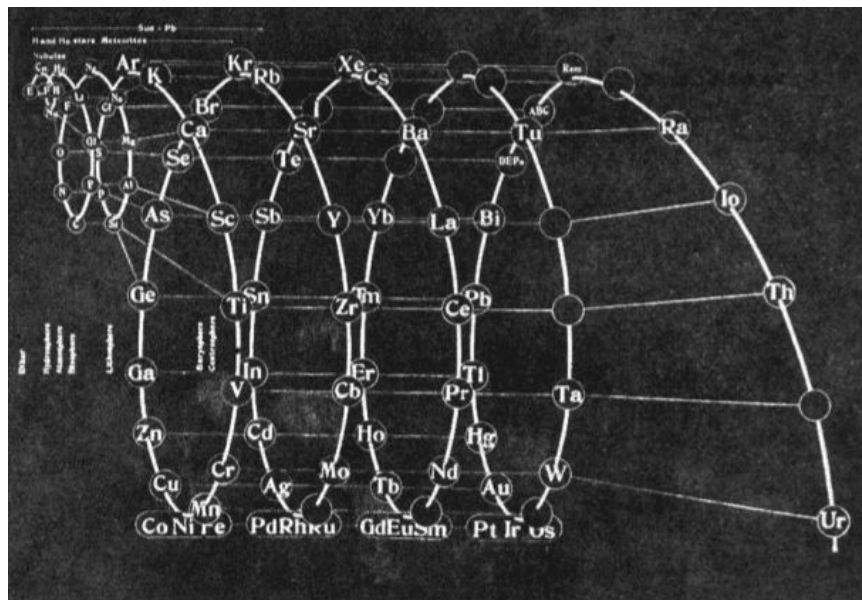
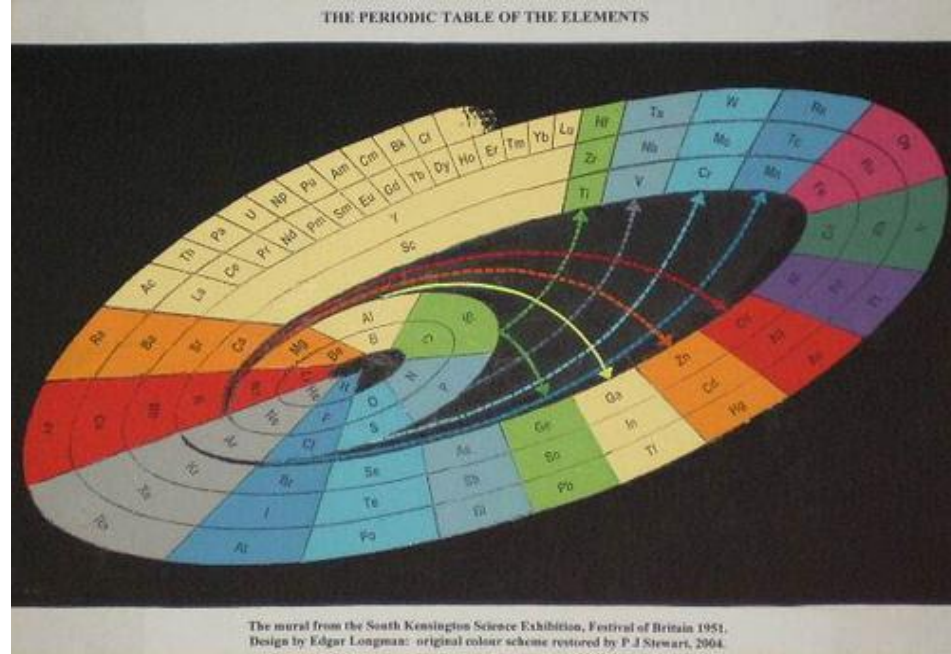
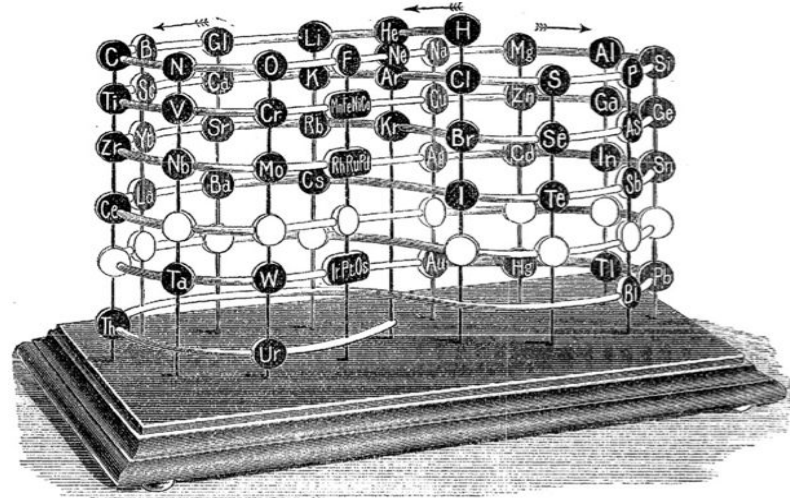
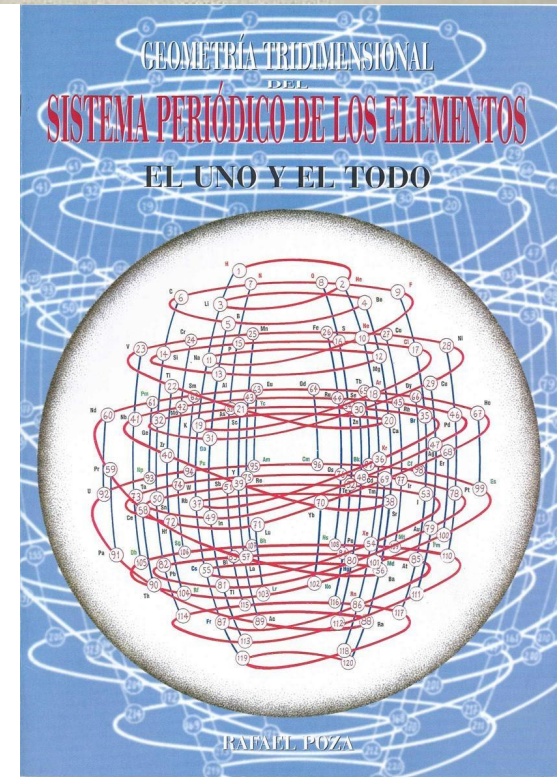


FIGURE 21.—EMERSON'S HELIX



Alternatives?

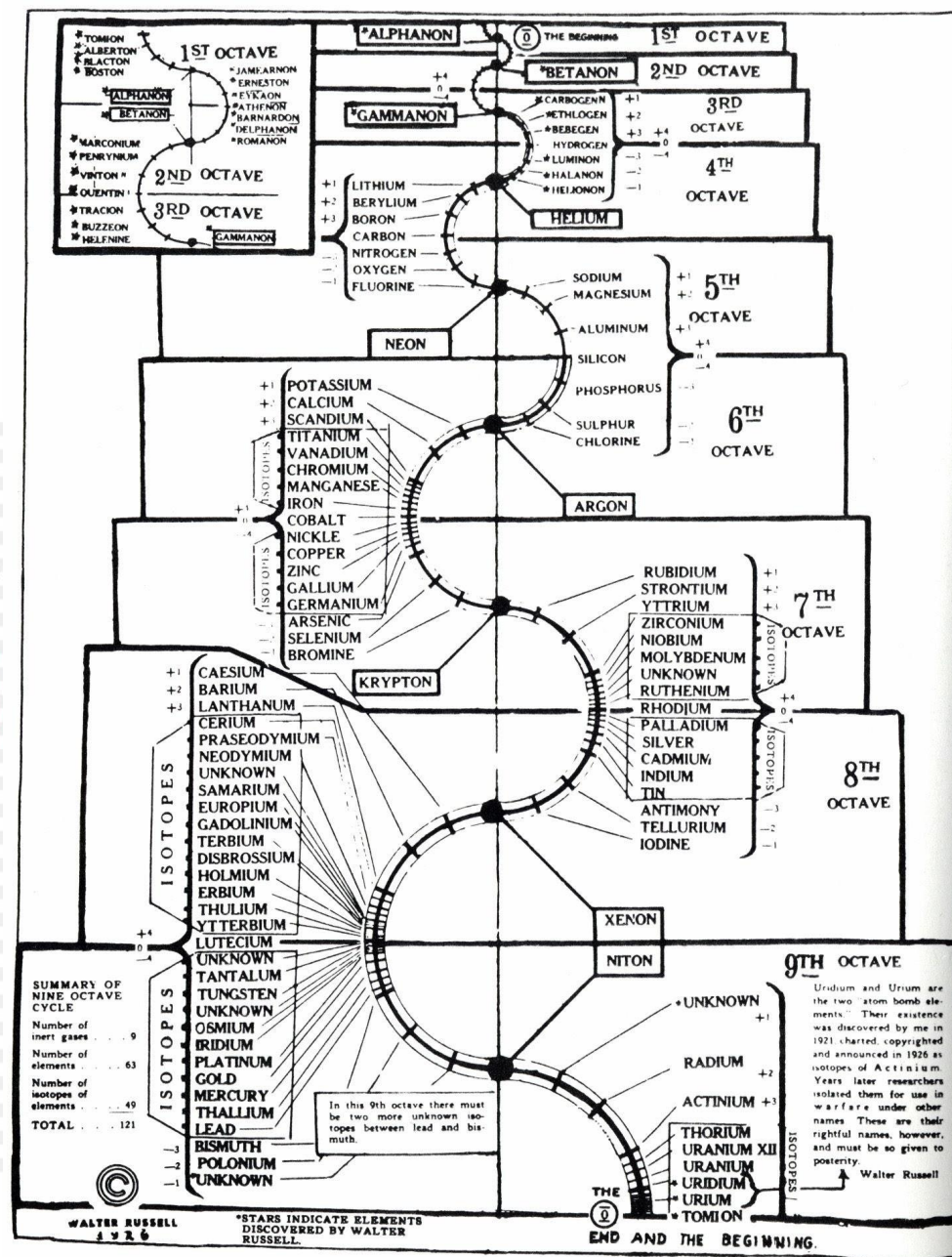
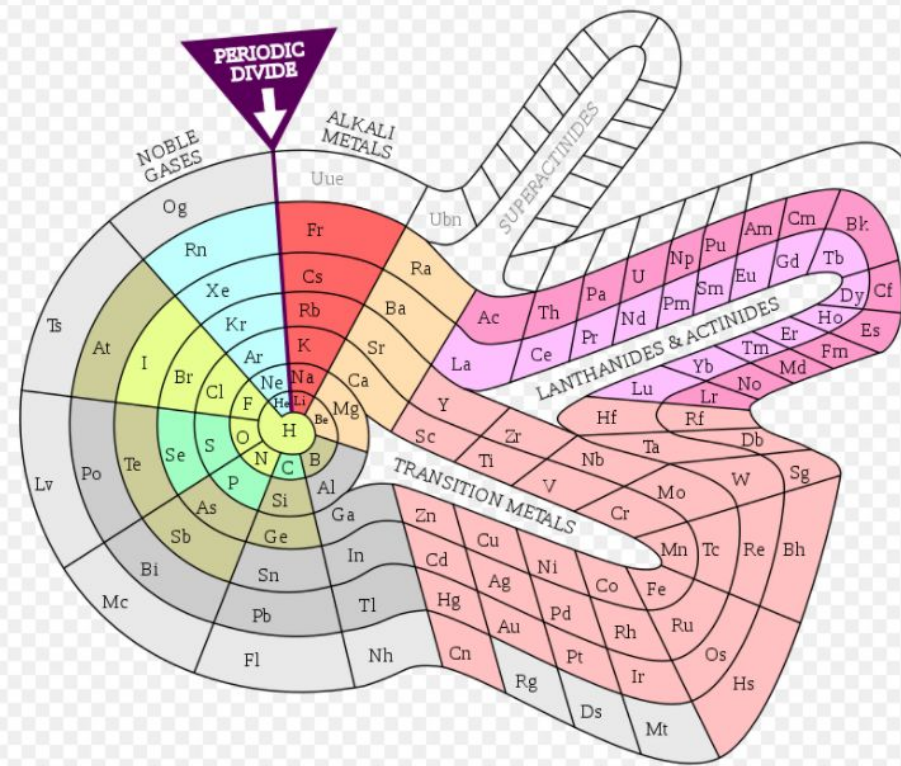


Figure 176. The Russell Periodic Chart of the Elements, No. 1

Alternatives?

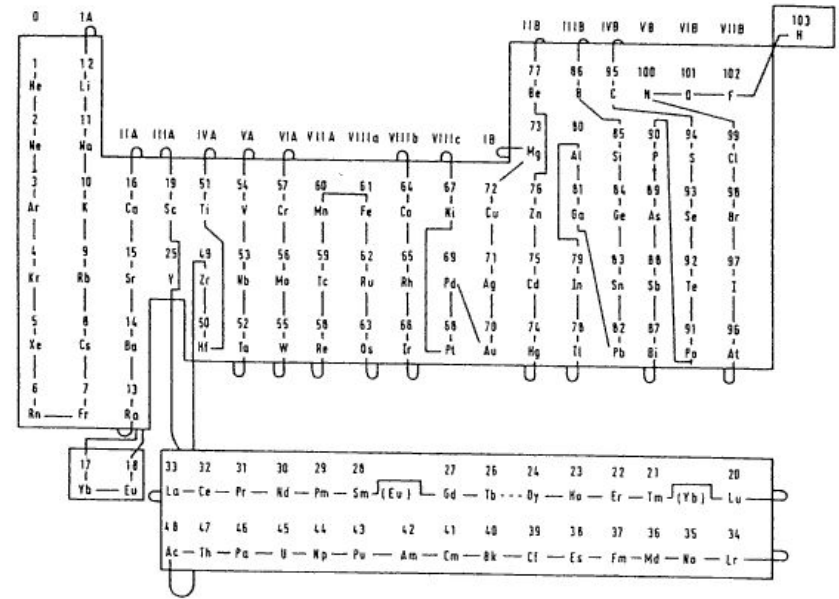
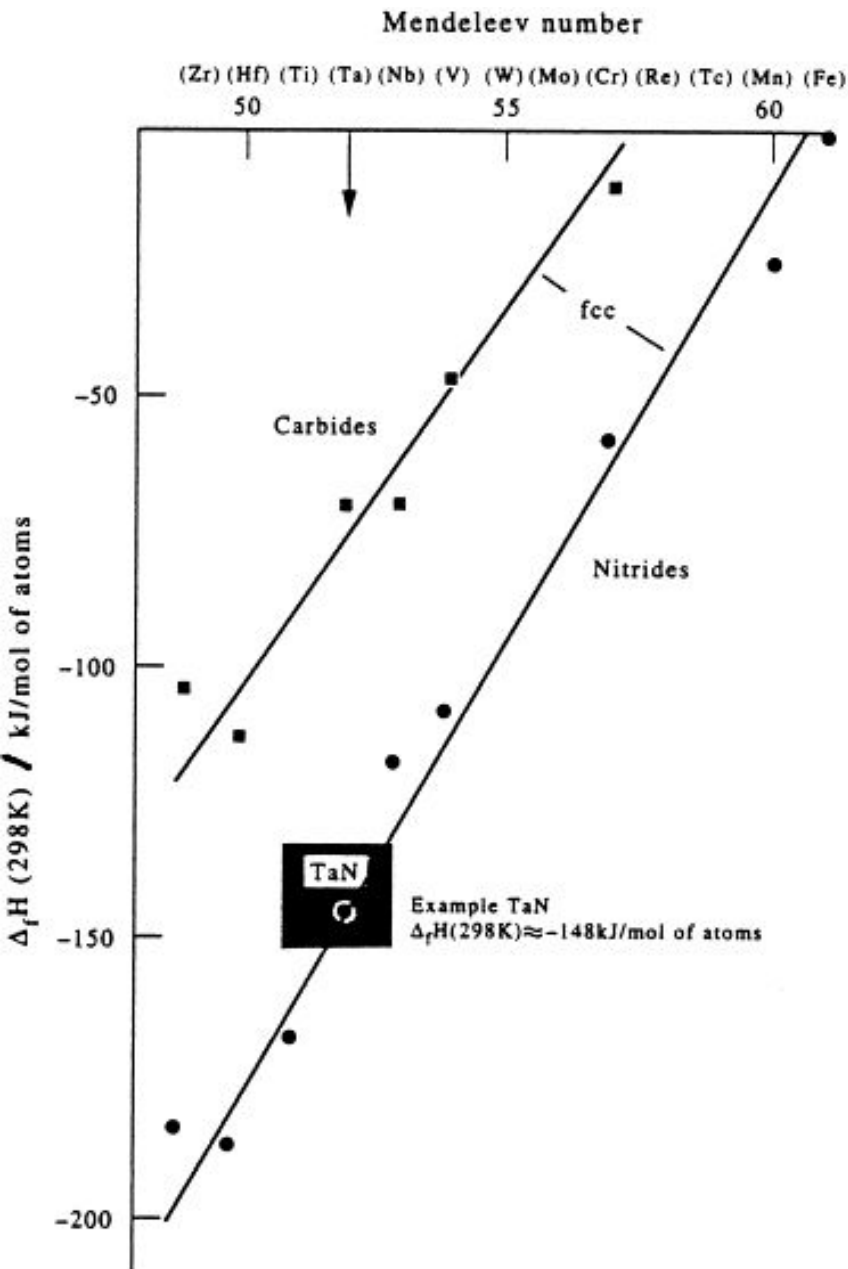


Fig. 1.8 The string running through this modified periodic table puts all the elements in sequential order, given by the relative ordering number $\mathcal{N}$. From Pettifor (1988).

Alternatives?

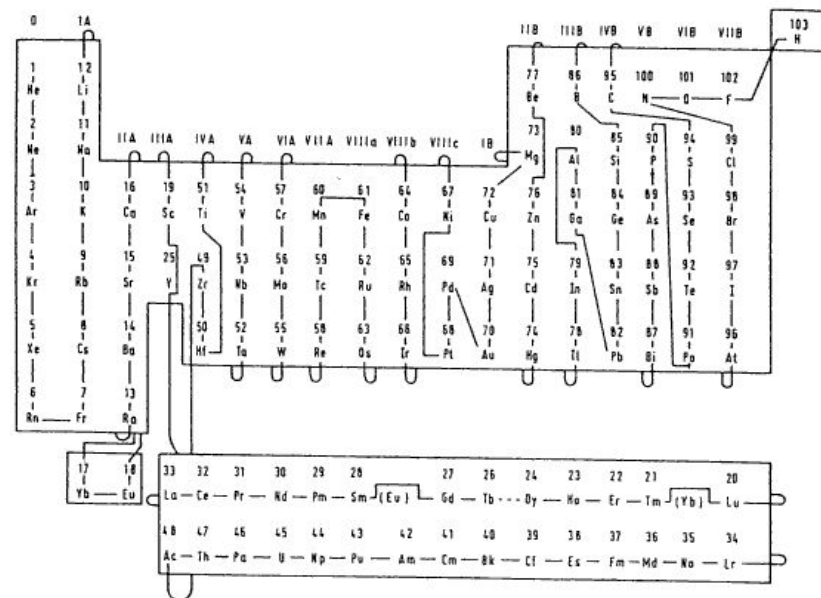
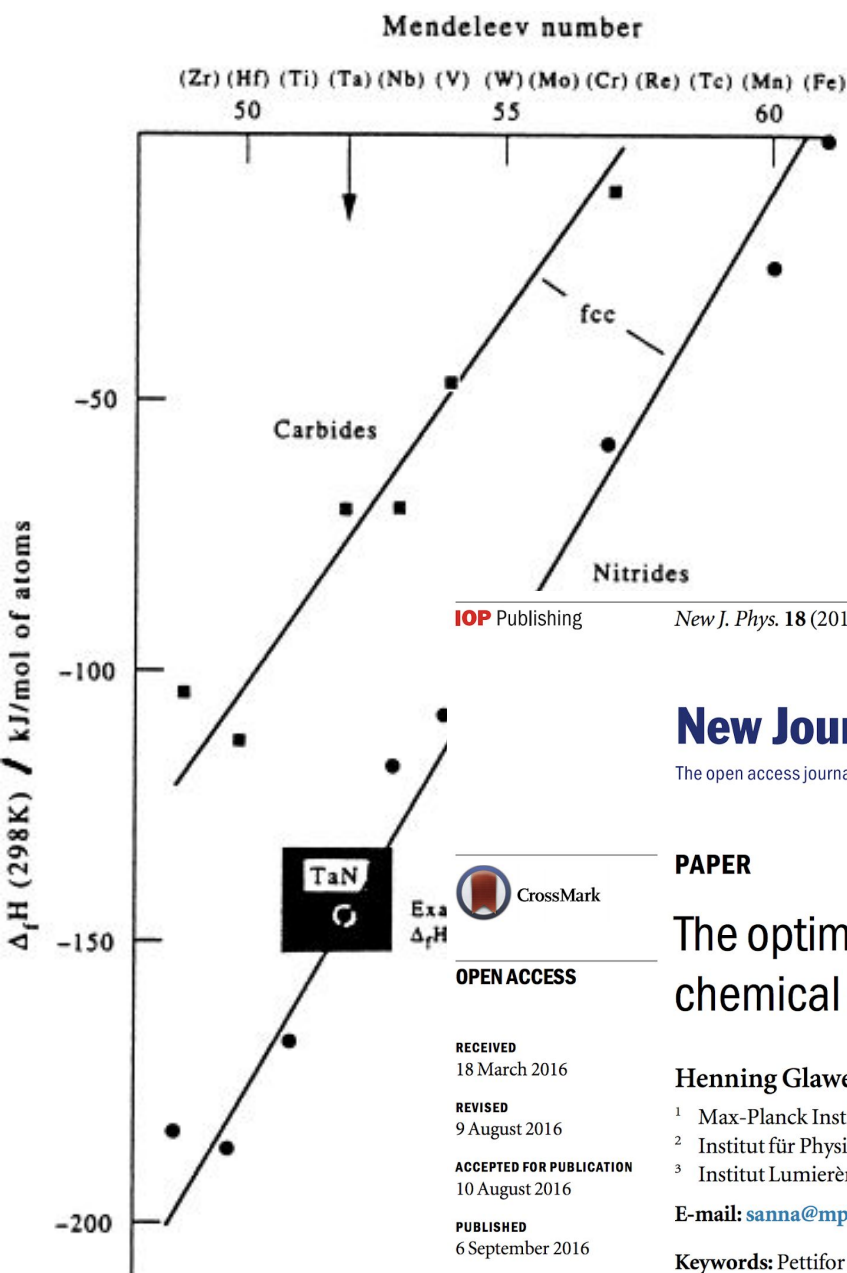


Fig. 1.8 The string running through this modified periodic table puts all the elements in sequential order, given by the relative ordering number $\mathcal{N}$. From Pettifor (1988).

IOP Publishing

New J. Phys. 18 (2016) 093011

doi:10.1088/1367-2630/18/9/093011

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PAPER

The optimal one dimensional periodic table: a modified Pettifor chemical scale from data mining

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E-mail: sanna@mpi-halle.mpg.de and miguel.marques@physik.uni-halle.de

Keywords: Pettifor Scale, chemical similarity, atomic substitution, crystal structures



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18 March 2016

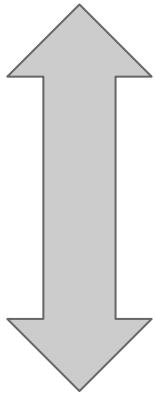
REVISED
9 August 2016

ACCEPTED FOR PUBLICATION
10 August 2016

PUBLISHED
6 September 2016

The pillars of science

Theory



Experiment



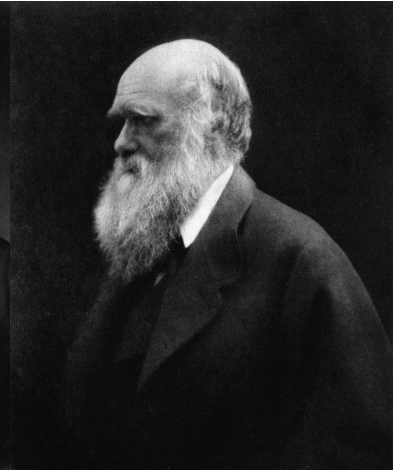
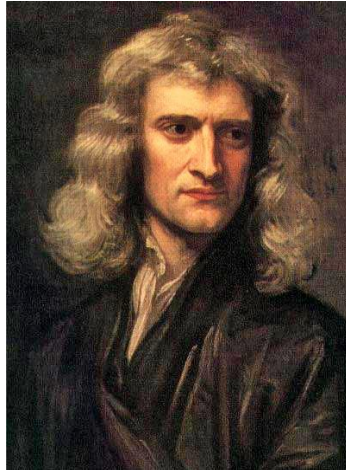
Εὐκλείδης
Eukleidēs



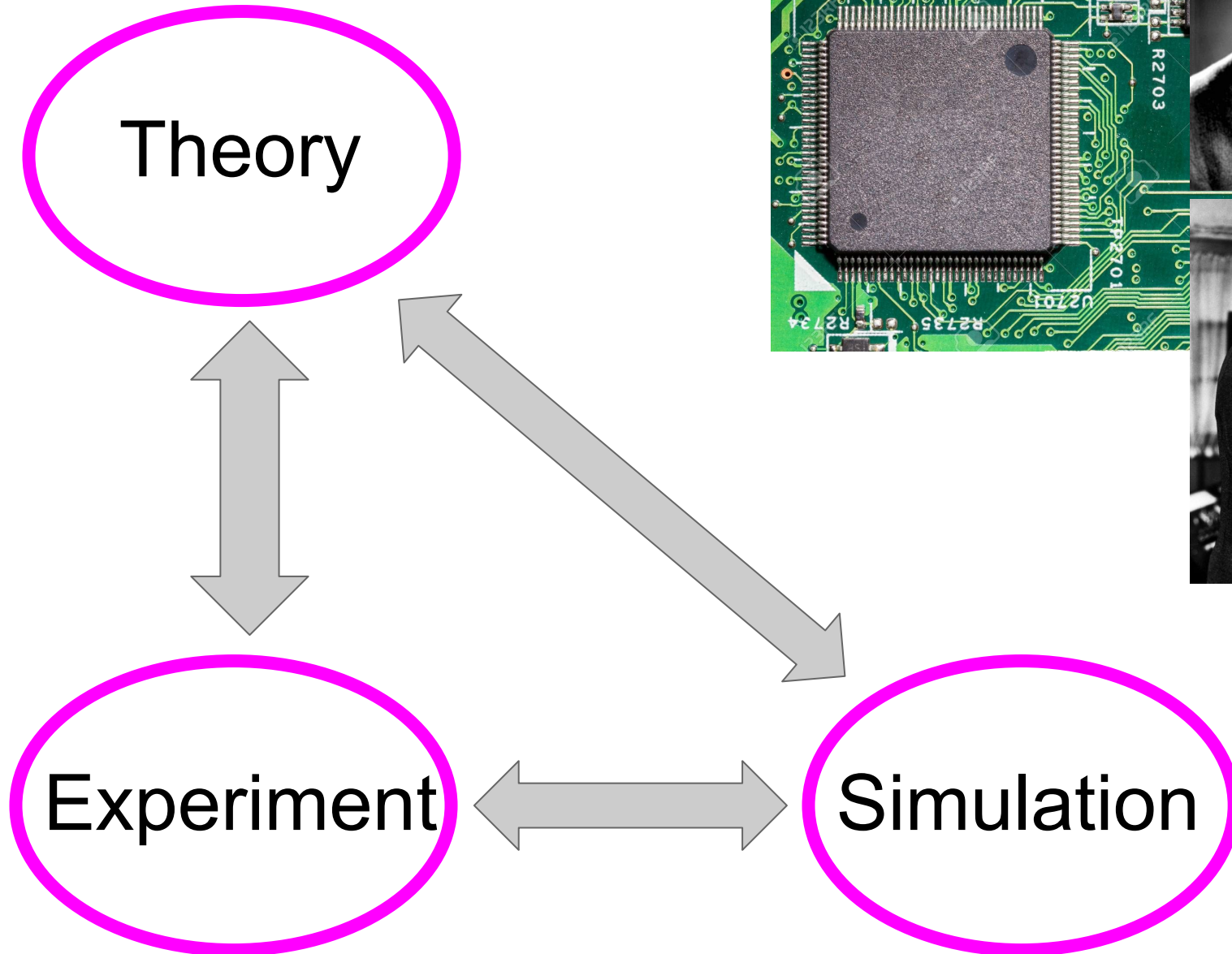
Πυθαγόρας
Pythagóras



Ἀρχιμήδης
Archimedes

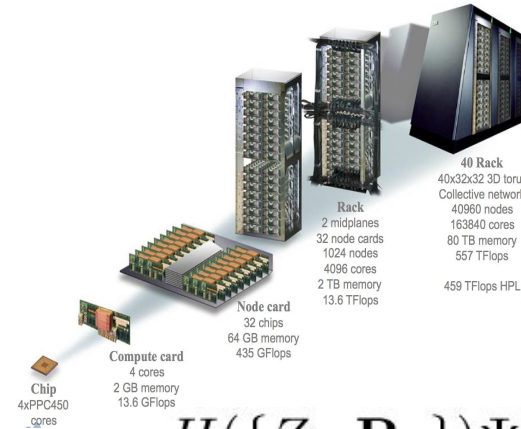
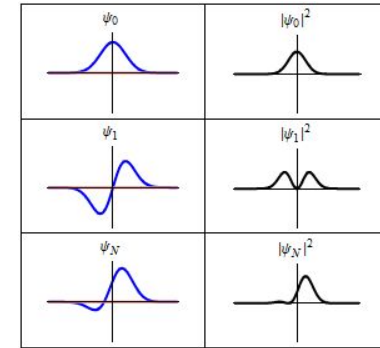
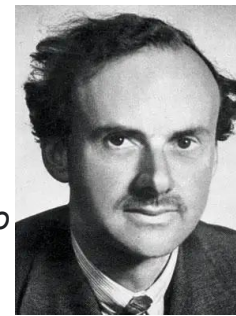


The pillars of science



The fundamental laws necessary for the mathematical treatment of a large part of physics and the whole of chemistry are thus completely known, and the difficulty lies only in the fact that application of these laws leads to equations that are too complex to be solved.

Dirac



$$H(\{Z_I, \mathbf{R}_I\})\Psi(\mathbf{r}) = E\Psi(\mathbf{r})$$

$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H} |\psi(t)\rangle$$



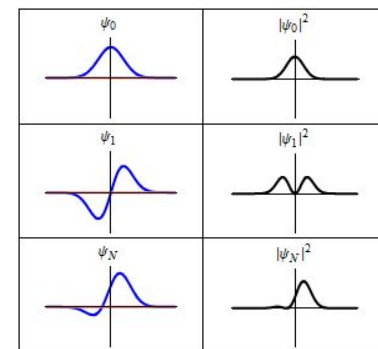
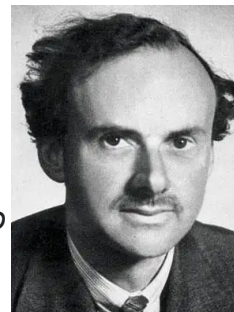
Schrödinger
1933

QML???

Error [Energy]

The fundamental laws necessary for the mathematical treatment of a large part of physics and the whole of chemistry are thus completely known, and the difficulty lies only in the fact that application of these laws leads to equations that are too complex to be solved.

Dirac



FF

SE

15 kcal/mol

HF

5 kcal/mol

MP2

1 kcal/mol

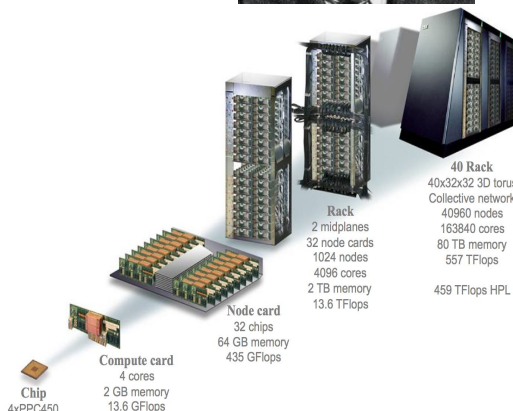
QMC
CCSD(T)



Schrödinger
1933

$$H(\{Z_I, \mathbf{R}_I\})\Psi(\mathbf{r}) = E\Psi(\mathbf{r})$$

$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H} |\psi(t)\rangle$$



Cost [CPU t]/compound

ms

min

h

d

yr

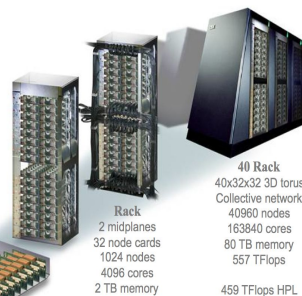
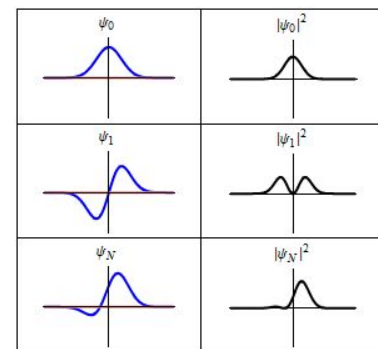
Error [Energy]

Model
chemistry

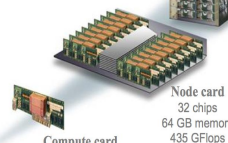


1998

Pople



40 Rack
40x32x32 3D torus
Collective network
40960 nodes
163840 cores
80 TB memory
557 TFlops
459 TFlops HPL

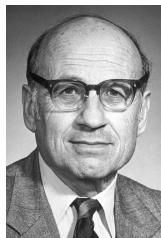


Chip
4xPPC450
cores

Compute card
4 cores
2 GB memory
13.6 GFlops

Node card
32 chips
64 GB memory
435 GFlops

DFTB



Kohn



DFT

HF

MP2

QMC
CCSD(T)



Schrödinger
1933

$$H(\{Z_I, \mathbf{R}_I\})\Psi(\mathbf{r}) = E\Psi(\mathbf{r})$$

$$i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle = \hat{H} |\psi(t)\rangle$$

15 kcal/mol

5 kcal/mol

1 kcal/mol

ms

min

h

d

yr

Cost [CPU t]/compound

Ab initio view on chemical space

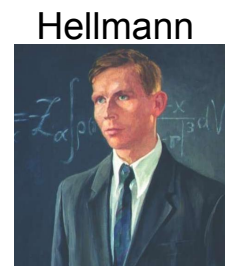
$$H(\{Z_I, \mathbf{R}_I\})\Psi(\mathbf{r}) = E\Psi(\mathbf{r})$$



Schrödinger



Feynman



Hellmann



Fukui

Alchemy

perturbation (extrapolate)

QML

machine
algorithms
data
statistical
learning
graphs
clustering
correlation
analysis
properties
similarity
becomes
Machine
urgent

correlation (interpolate)

$$\{Z_I, \mathbf{R}_I\} \xrightarrow{H\Psi} E$$

supervised
learning

$$\{Z_I, \mathbf{R}_I\} \xrightarrow{\text{ML}} E$$



Vapnik

$$E(H(\lambda)) = E(H_i + \lambda(H_f - H_i))$$

$$\frac{\partial E[H]}{\partial \lambda} = \left\langle \Psi \left| \frac{\partial H(\lambda)}{\partial \lambda} \right| \Psi \right\rangle$$

$$E_t = \sum_{n=0}^{\infty} \frac{1}{n!} \frac{\partial^n}{\partial \lambda^n} \left\langle \psi_\lambda \left| \hat{H}(\lambda) \right| \psi_\lambda \right\rangle \Big|_{\lambda=0} = E_r + \sum_{n=1}^{\infty} \frac{1}{n!} \frac{\partial^n E(\lambda)}{\partial \lambda^n} \Big|_{\lambda=0}$$

$$\frac{\partial E[H]}{\partial R_{Ix}} = \left\langle \Psi \left| \frac{\partial H}{\partial R_{Ix}} \right| \Psi \right\rangle \quad \frac{\partial E[H]}{\partial Z_I} = \left\langle \Psi \left| \frac{\partial H}{\partial Z_I} \right| \Psi \right\rangle$$

$$E_t = E_r + \Delta E^{\text{NN}} + \int_{\Omega} d\mathbf{r} \sum_{n=0}^{\infty} \frac{1}{(n+1)!} \Delta v \frac{\partial^n \rho_{\lambda}(\mathbf{r})}{\partial \lambda^n} \Big|_{\lambda=0}$$

von Rudorff, von Lilienfeld, *Phys Rev Res* (2020)



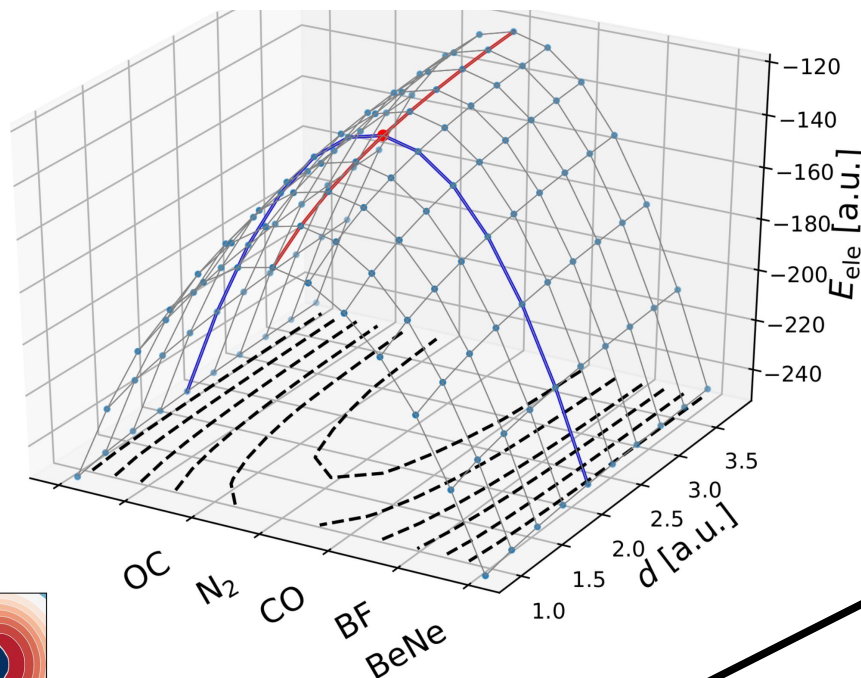
AI

vs.

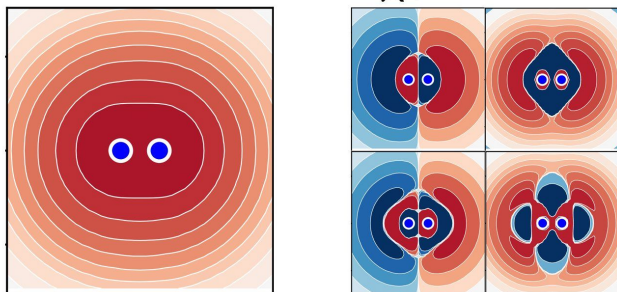
Physics

N_e Fias, Chang, von Lilienfeld, *J Phys Chem Lett* (2019), <https://arxiv.org/abs/1809.03302>

$$\text{CCS} \sim O(4N_I + 1)$$
$$0 < N_I < 10^6$$

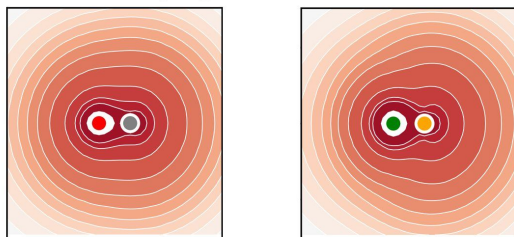


$$\text{N}_2 + \partial_{\lambda}^n \rho$$



CO

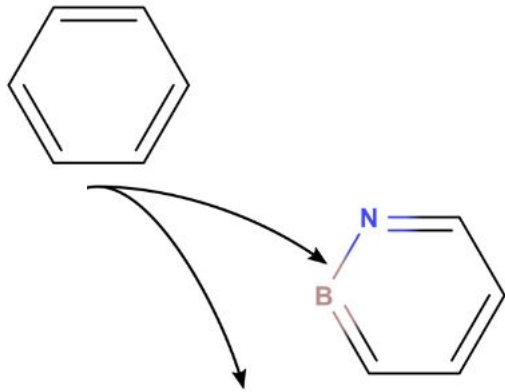
BF



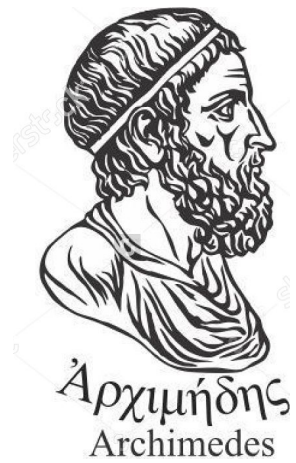
$$\text{QM: } M \mapsto f(M)$$

“First principles view on chemical space”, von Lilienfeld, *Int J Quantum Chem* (2013)von Rudorff, von Lilienfeld, *Phys Rev Research* (2020), *Science Advances* (2021) Z

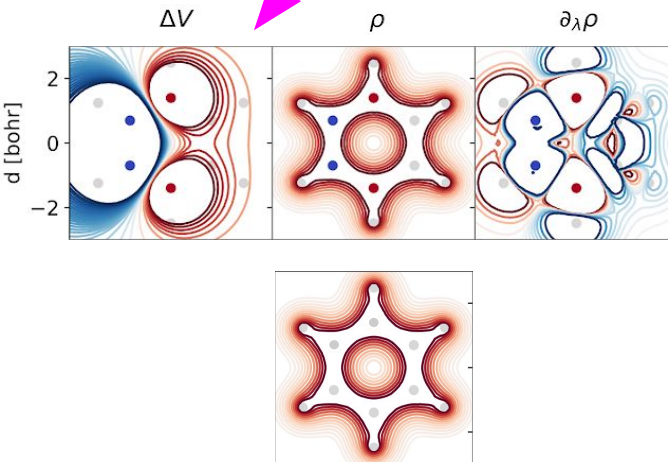
Alchemical Chirality



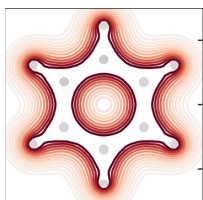
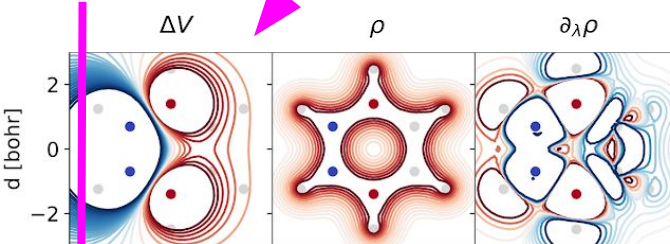
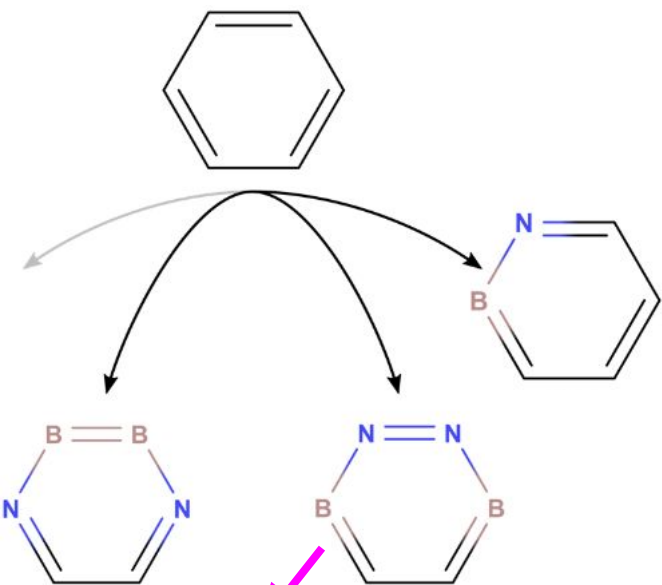
"Give me a lever and a place to stand
and I will move the earth." Archimedes



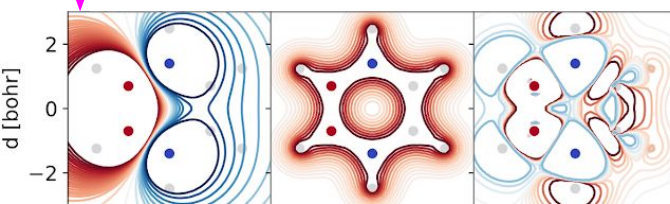
$$E_t - E_r = \int_{\Omega} d\mathbf{r} \Delta v(\mathbf{r}) \sum_{n=1}^{\infty} \frac{1}{n!} \frac{\partial^{n-1} \rho(\mathbf{r})}{\partial \lambda^{n-1}}$$



Alchemical Chirality



$$\Delta E_{ij}^{\text{sym}} \approx \sum_{n=1}^{\infty} \frac{1}{n!} \int_{-\infty}^{+\infty} d\mathbf{r} \Delta v_{ri}(\mathbf{r}) \left(\frac{\partial^{n-1} \rho_r(\mathbf{r})}{\partial \lambda_i^{n-1}} + \frac{\partial^{n-1} \rho_r(\mathbf{r})}{\partial \lambda_j^{n-1}} \right)$$



"Give me a lever and a place to stand and I will move the earth." Archimedes

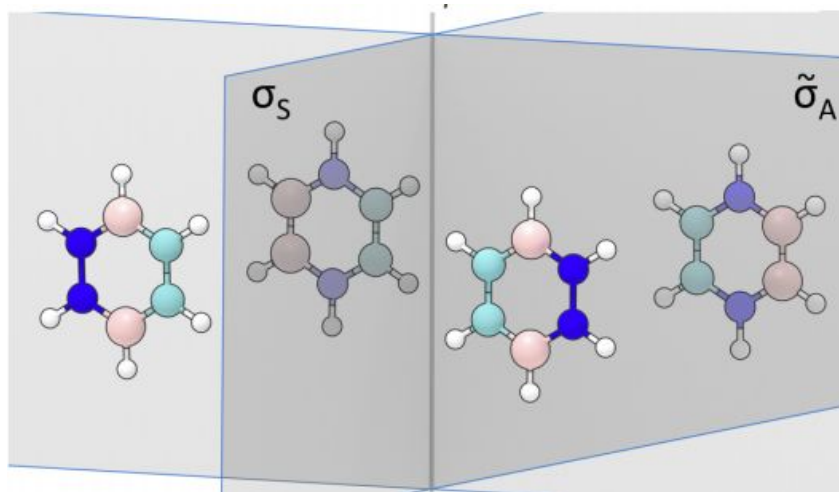


Fig. 1: Illustration of alchemical chirality (from Ref. 7)



Ἀρχιμήδης
Archimedes

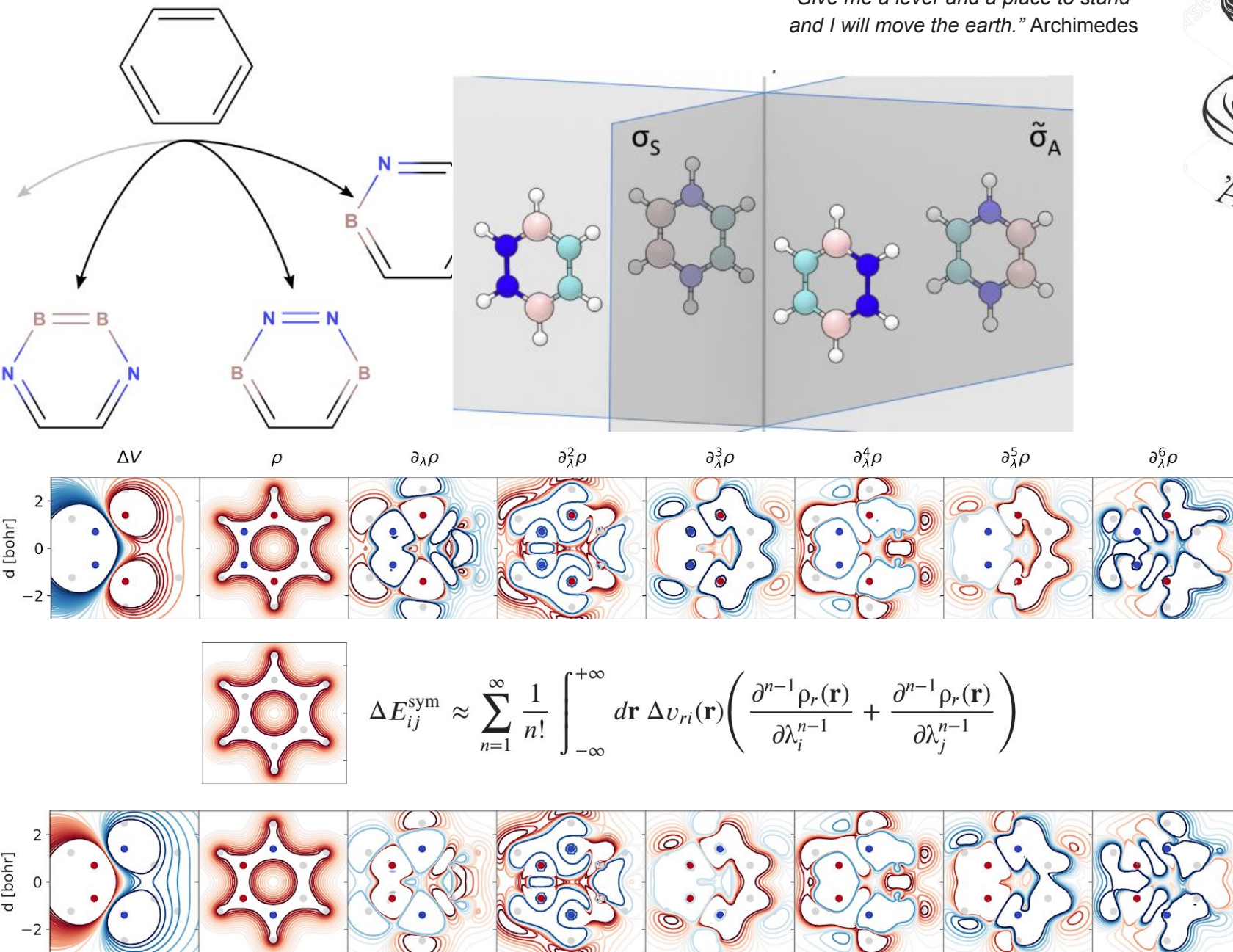
von Rudorff, von Lilienfeld, *Science Advances* (2021)

Alchemical Chirality

"Give me a lever and a place to stand
and I will move the earth." Archimedes



Ἀρχιμήδης
Archimedes

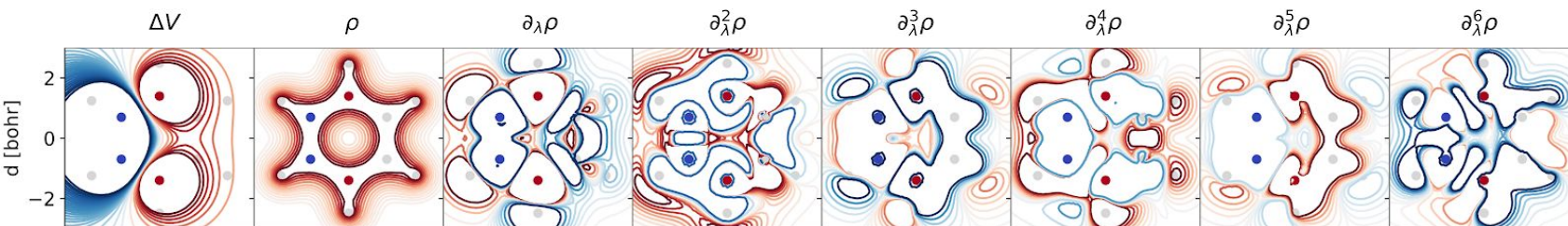
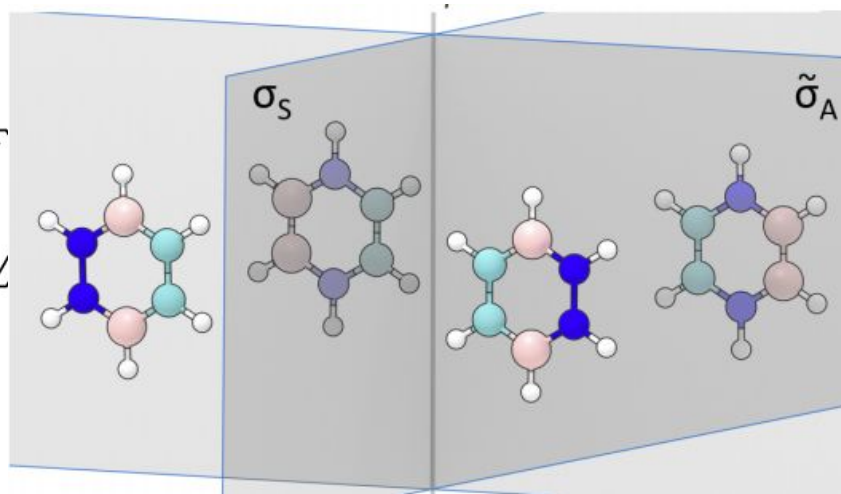
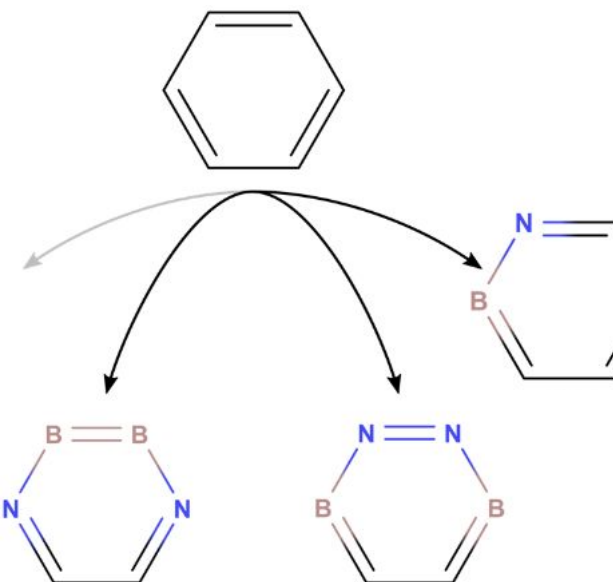


Alchemical Chirality

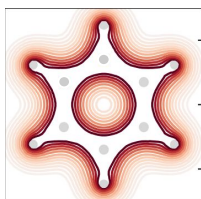
"Give me a lever and a place to stand and I will move the earth." Archimedes



Ἀρχιμήδης
Archimedes

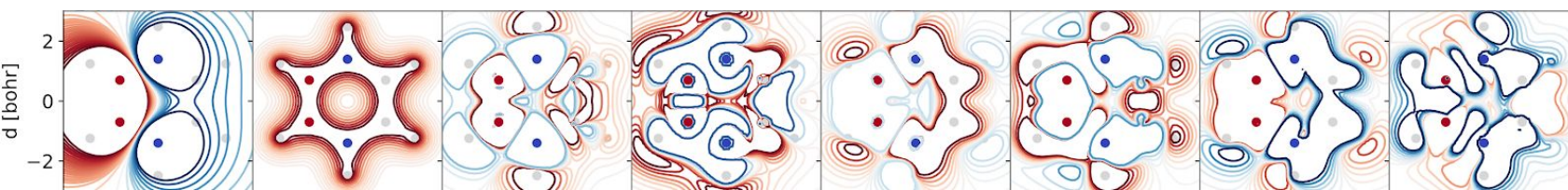


NN+2BC
+CC+2NB



$$\Delta E_{ij}^{\text{sym}} \approx \sum_{n=1}^{\infty} \frac{1}{n!} \int_{-\infty}^{+\infty} d\mathbf{r} \Delta v_{ri}(\mathbf{r}) \left(\frac{\partial^{n-1} \rho_r(\mathbf{r})}{\partial \lambda_i^{n-1}} + \frac{\partial^{n-1} \rho_r(\mathbf{r})}{\partial \lambda_j^{n-1}} \right) \rightarrow \text{NC} \sim \text{BC} + 0.5 * (\text{NN} - \text{BB})$$

von Rudorff, von Lilienfeld, *Science Advances* (2021)



BB+2NC
+CC+2NB

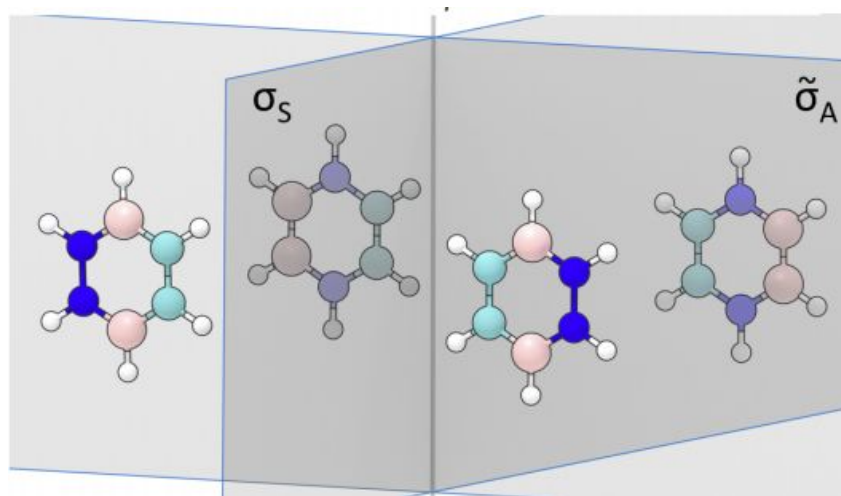
Alchemical Chirality

"Give me a lever and a place to stand
and I will move the earth." Archimedes

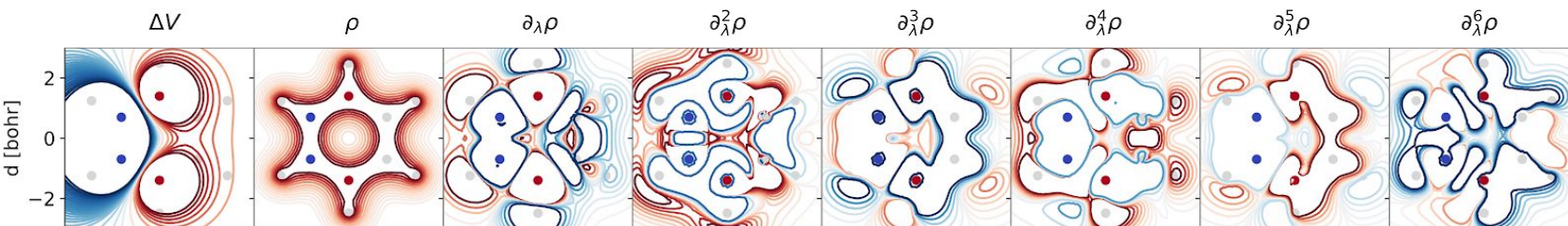


Ἀρχιμήδης
Archimedes

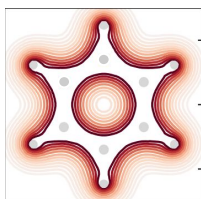
					VIIIA
Q	R	S			
IIIA	IVA	VA	VIA	VIIA	
5 B	6 C	7 N	8 O	9 F	2 He
13 Al	14 Si	15 P	16 S	17 Cl	10 Ne
31 Ga	32 Ge	33 As	34 Se	35 Br	18 Ar
49 In	50 Sn	51 Sb	52 Te	53 I	36 Kr
					54 Xe



$$\rightarrow \text{SR} \sim \text{QR} + 0.5 \cdot (\text{SS} - \text{QQ})$$

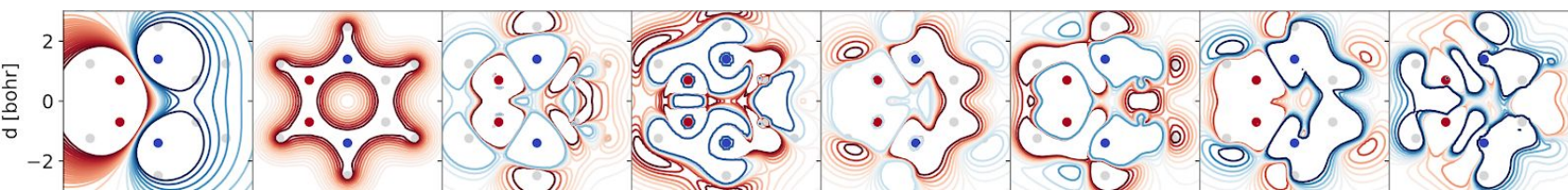


$$\text{NN} + 2\text{BC} + \text{CC} + 2\text{NB}$$



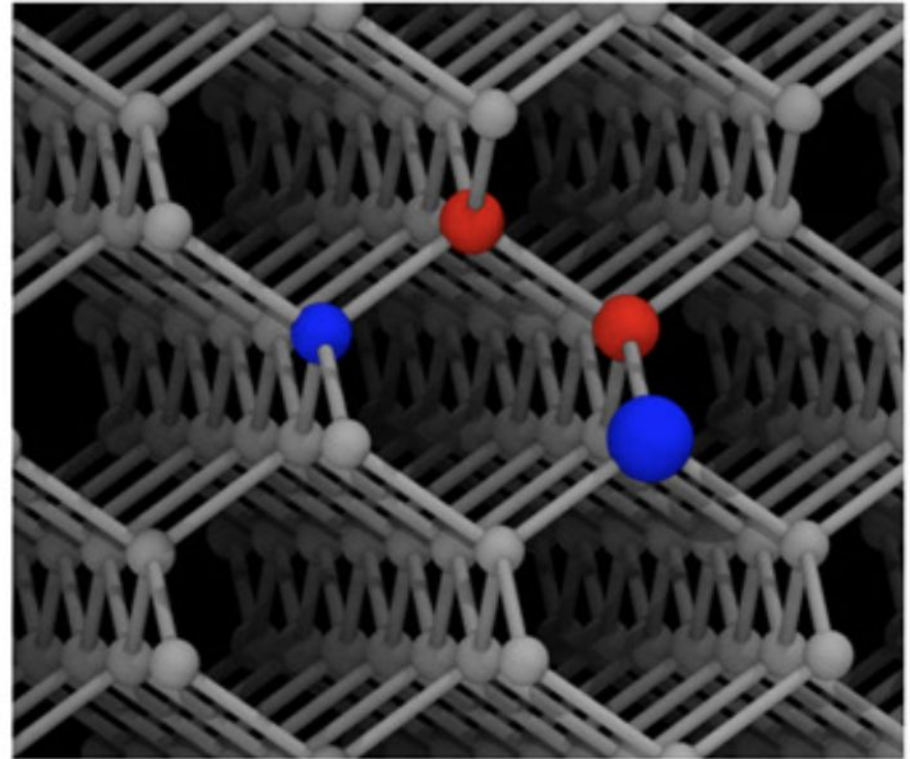
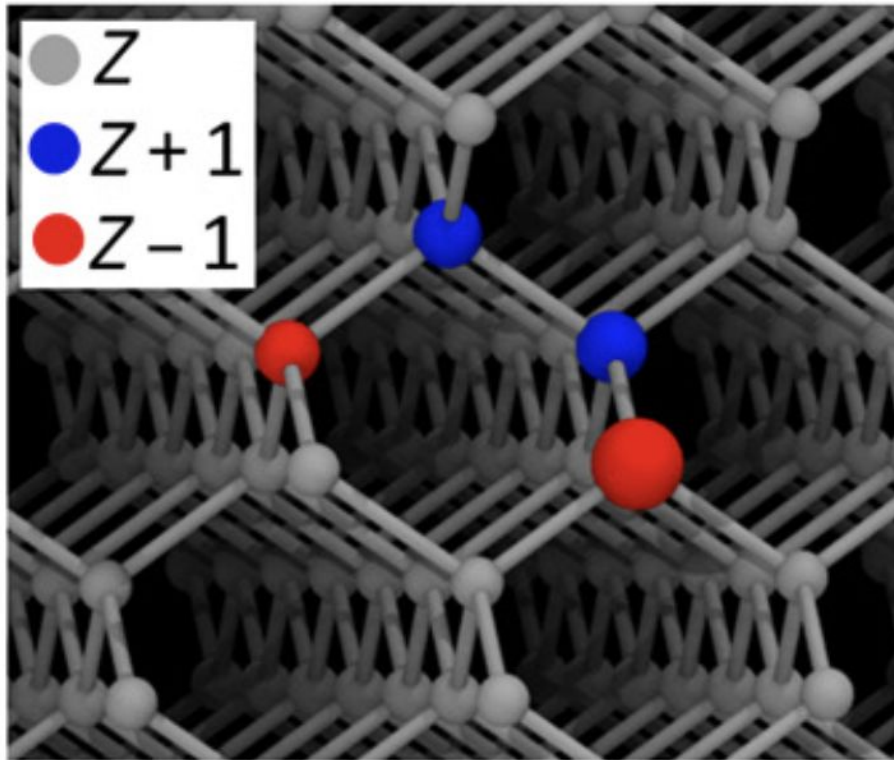
$$\Delta E_{ij}^{\text{sym}} \approx \sum_{n=1}^{\infty} \frac{1}{n!} \int_{-\infty}^{+\infty} d\mathbf{r} \Delta v_{ri}(\mathbf{r}) \left(\frac{\partial^{n-1} \rho_r(\mathbf{r})}{\partial \lambda_i^{n-1}} + \frac{\partial^{n-1} \rho_r(\mathbf{r})}{\partial \lambda_j^{n-1}} \right) \rightarrow \text{NC} \sim \text{BC} + 0.5 \cdot (\text{NN} - \text{BB})$$

von Rudorff, von Lilienfeld, *Science Advances* (2021)



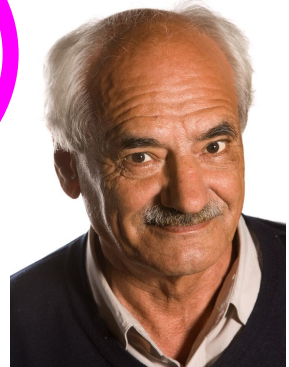
$$\text{BB} + 2\text{NC} + \text{CC} + 2\text{NB}$$

Alchemical Chirality

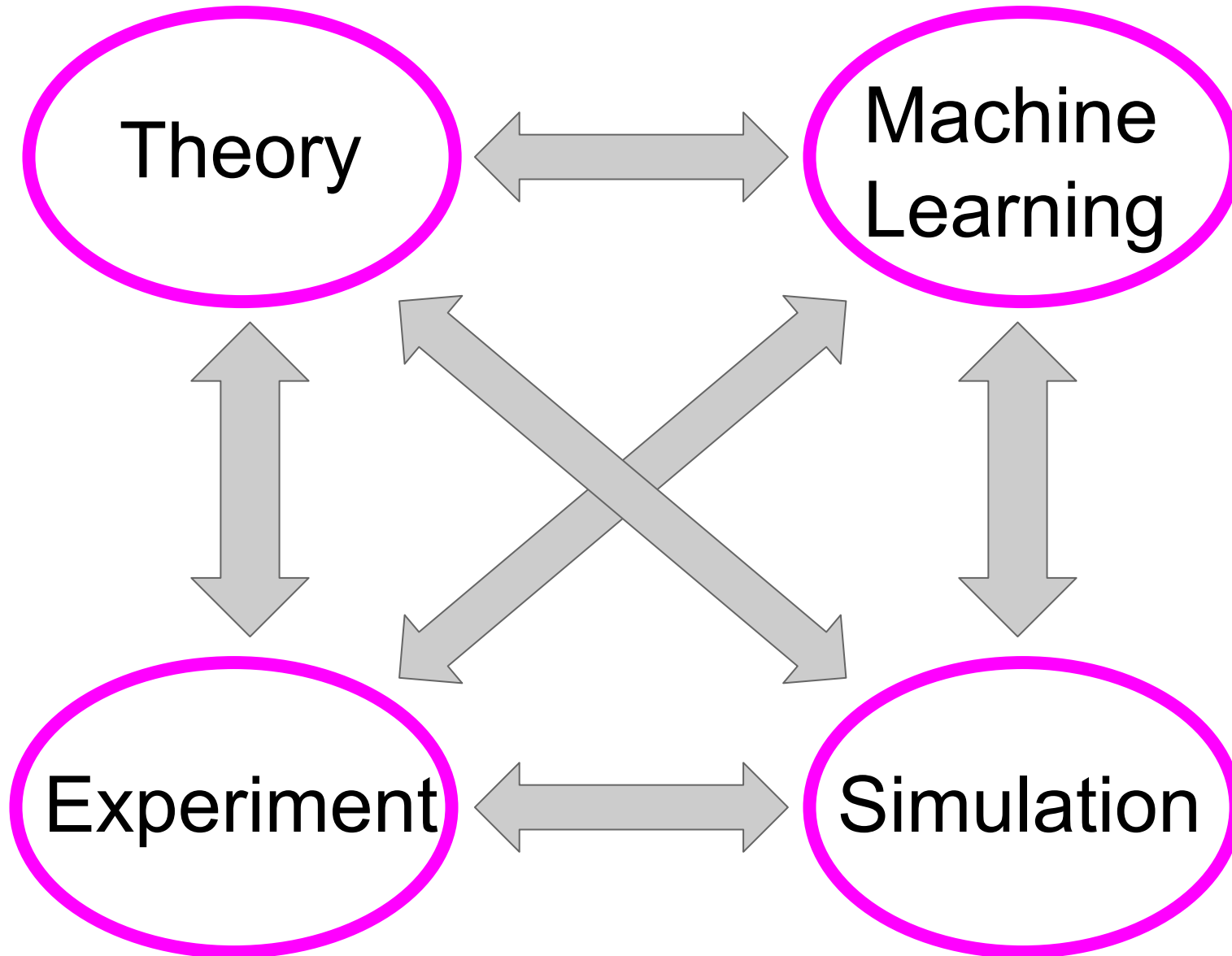


The pillars of science

Vapnik



Chervonenkis

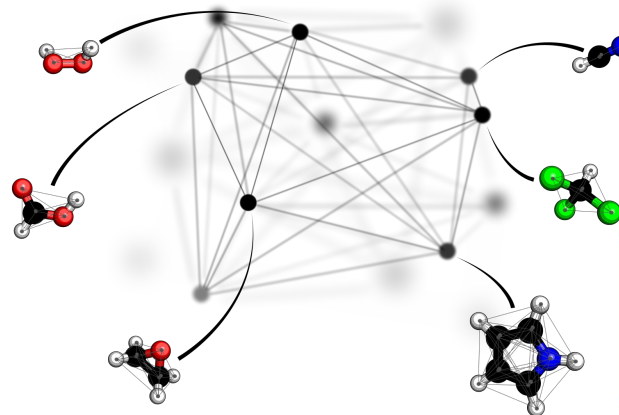




AI

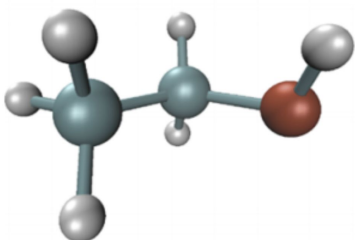
vs.

Physics



$$P^{\text{est}}(\mathbf{M}) = \sum_i \alpha_i k(\mathbf{M}, \mathbf{M}_i)$$

$$\vec{\alpha} = \mathbf{K}^{-1} \vec{P}^{\text{ref}}$$



	O	C	C	H	H	H	H	H	H
O	O	OC	OC	OH	OH	OH	OH	OH	OH
C	OC	C	CC	CH	CH	CH	CH	CH	CH
C	OC	CC	C	CH	CH	CH	CH	CH	CH
H	OH	CH	CH	H	HH	HH	HH	HH	HH
H	OH	CH	CH	HH	H	HH	HH	HH	HH
H	OH	CH	CH	HH	HH	H	HH	HH	HH
H	OH	CH	CH	HH	HH	HH	H	HH	HH
H	OH	CH	CH	HH	HH	HH	HH	H	HH
H	OH	CH	CH	HH	HH	HH	HH	H	H



K.-R. Müller
TU Berlin



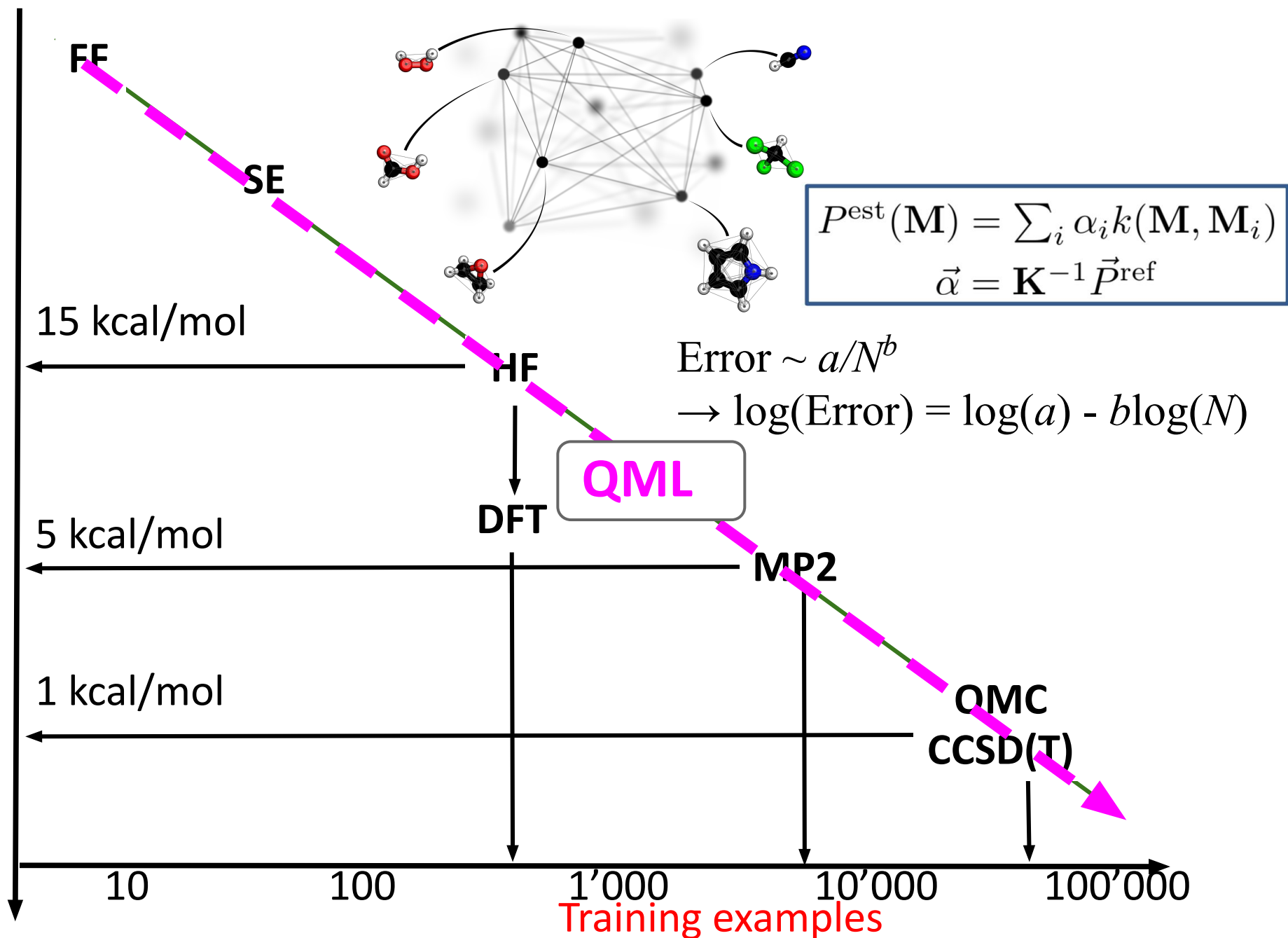
A. Tkatchenko
UofLuxembourg



M. Rupp
UofKonstanz

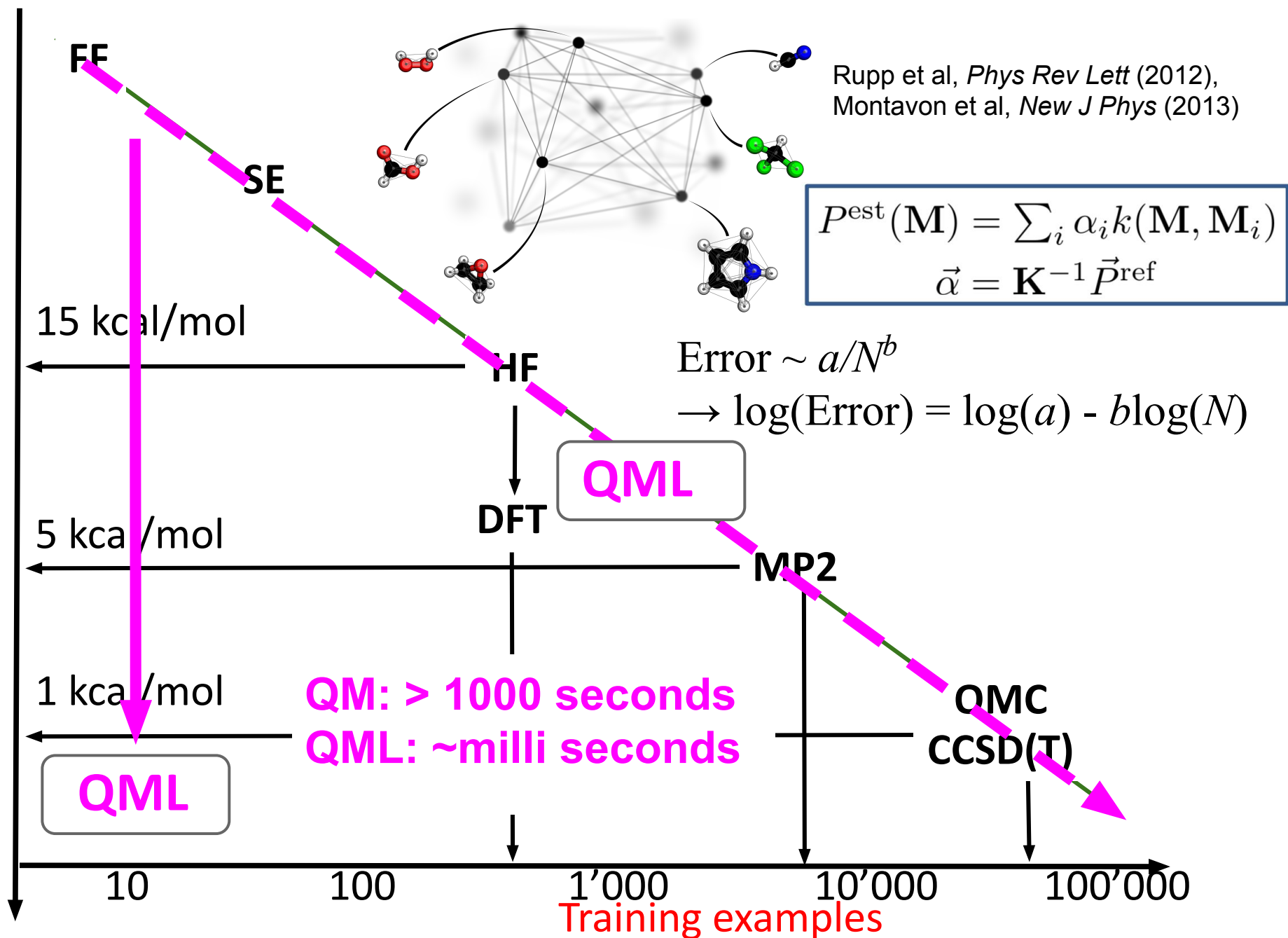
Error [Energy]

Vapnik, *The Nature of Statistical Learning Theory*, Springer (1995)



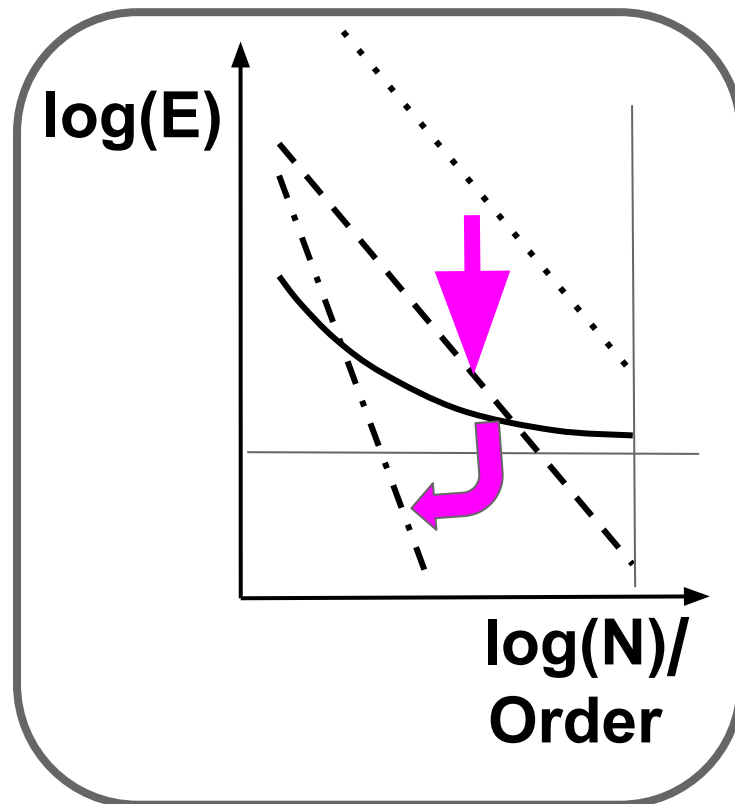
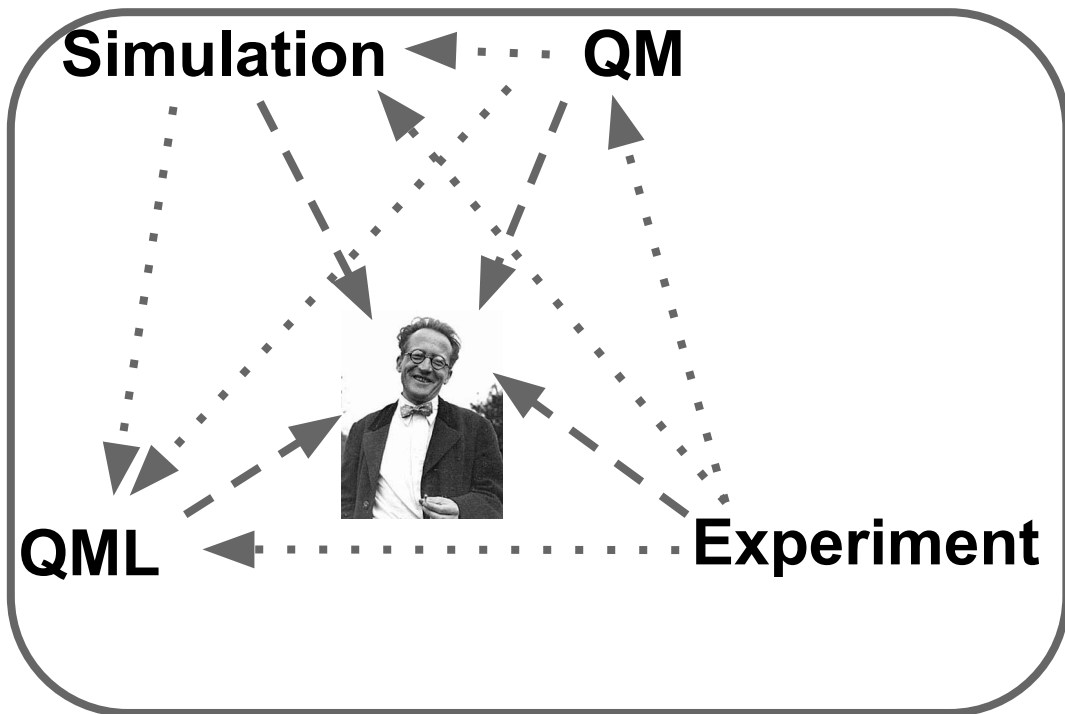
Error [Energy]

Vapnik, *The Nature of Statistical Learning Theory*, Springer (1995)



Summary

$$H(\{Z_I, \mathbf{R}_I\})\Psi(\mathbf{r}) = E\Psi(\mathbf{r})$$



'First principles view on chemical space', *Int. J. Quantum Chem.* (2013)

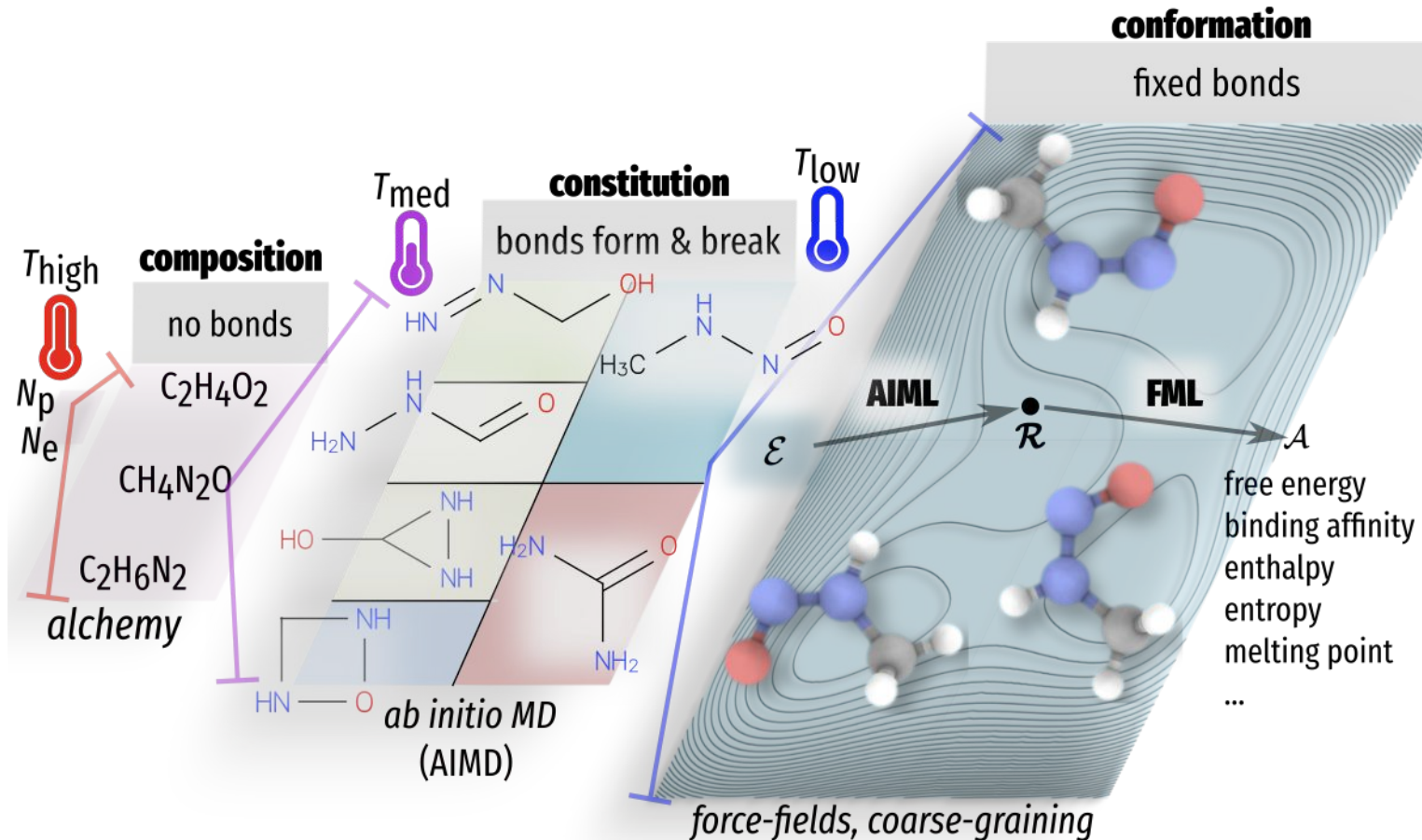
'Quantum Machine Learning', *Angew. Chem. Int. Ed.* (2018)

Evolution or Revolution???

Control accuracy & speed-up

Ab initio view on chemical space

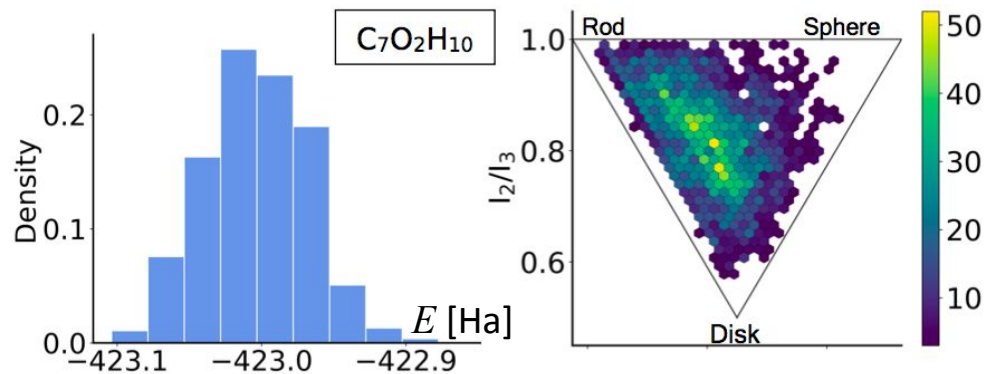
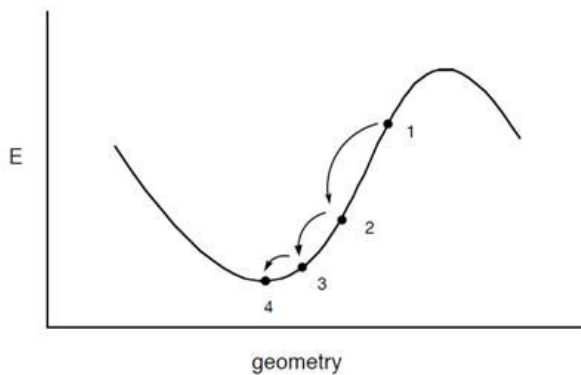
Weinreich et al, *Ab initio machine learning of phase space averages*, *J Chem Phys* (2022)



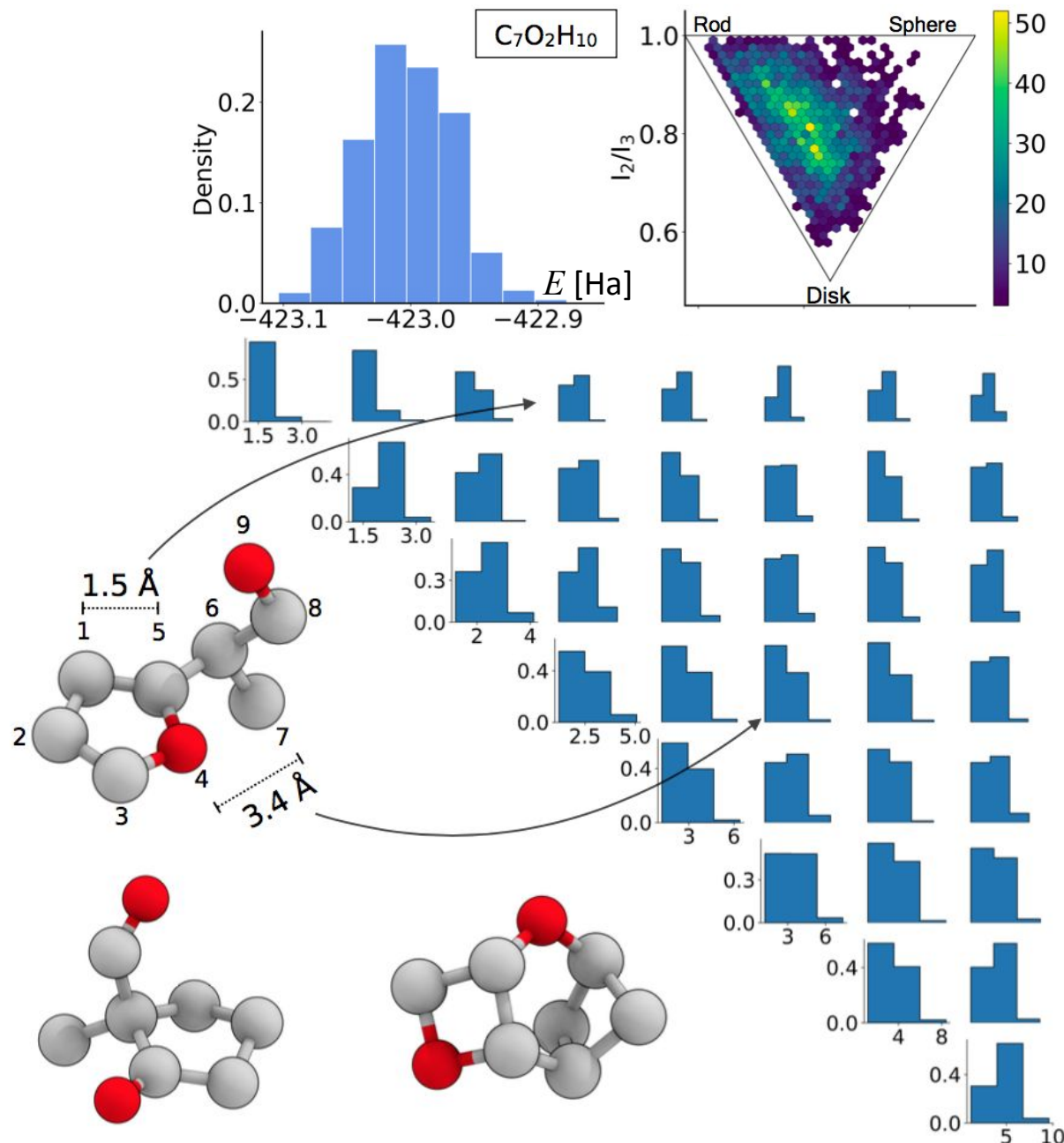
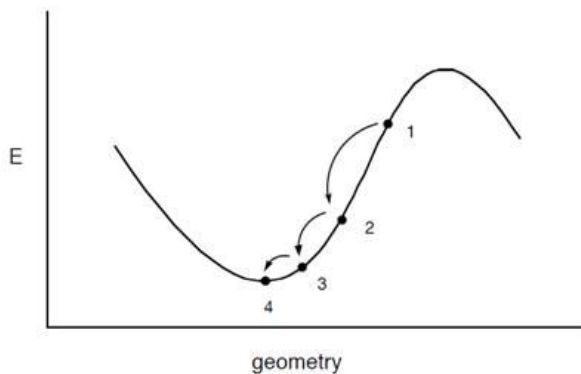
Predicting

1. structure (*Nat Commun* 2021)
2. reactivity (*J Chem Phys* 2021, *J Chem Phys* 2022)
3. Free energy (*J Chem Phys* 2021, *J Chem Phys* 2022)

Structure

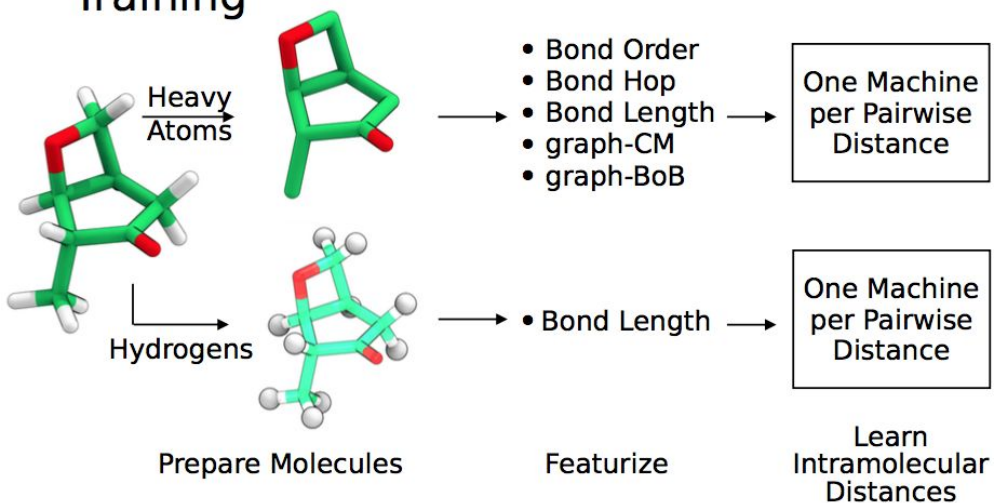


Structure

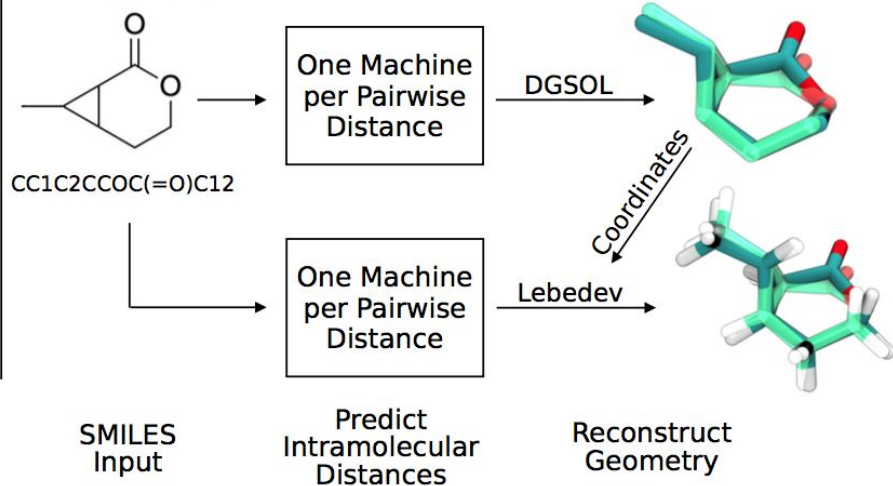


Graph to Structure (G2S)

Training

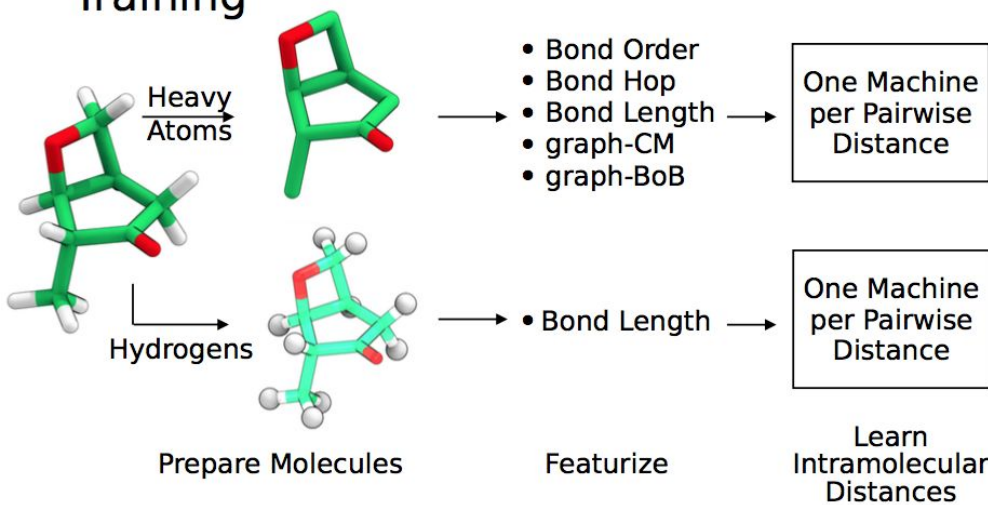


Prediction

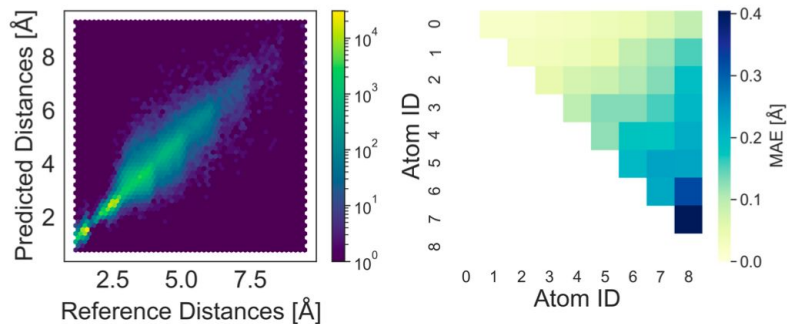
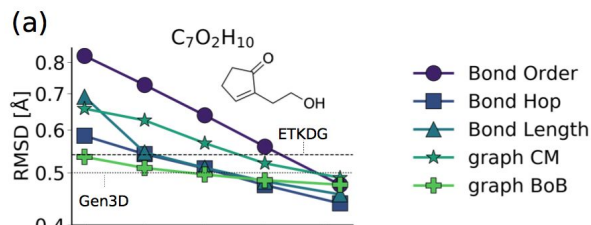
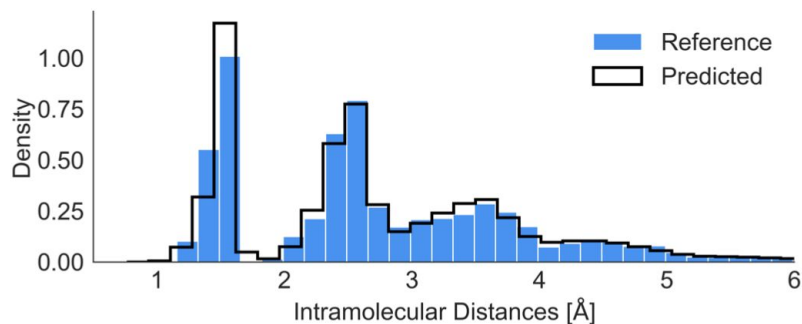
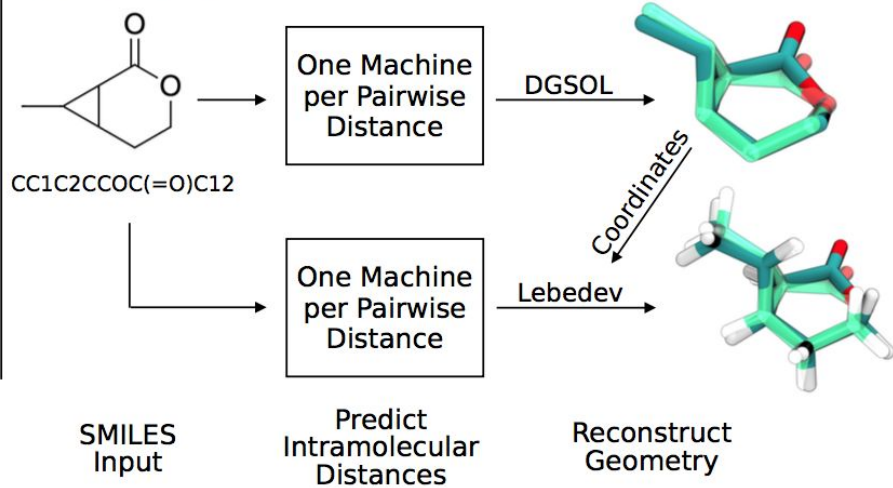


Graph to Structure (G2S)

Training

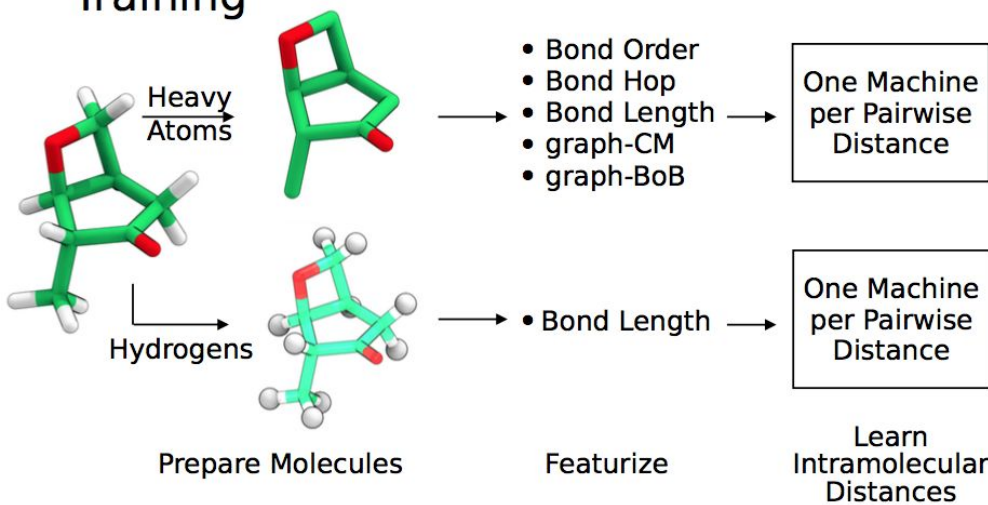


Prediction

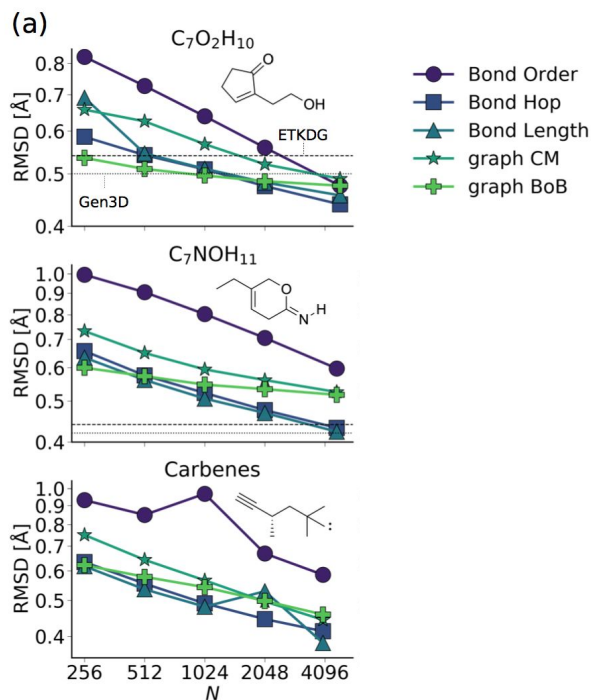
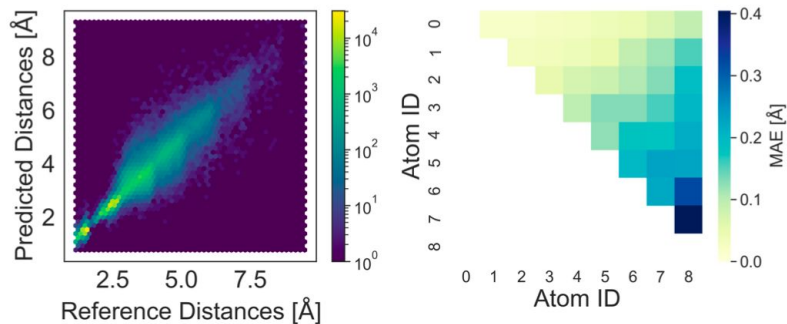
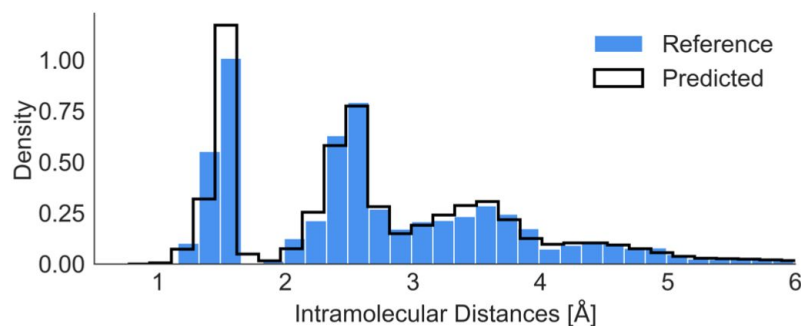
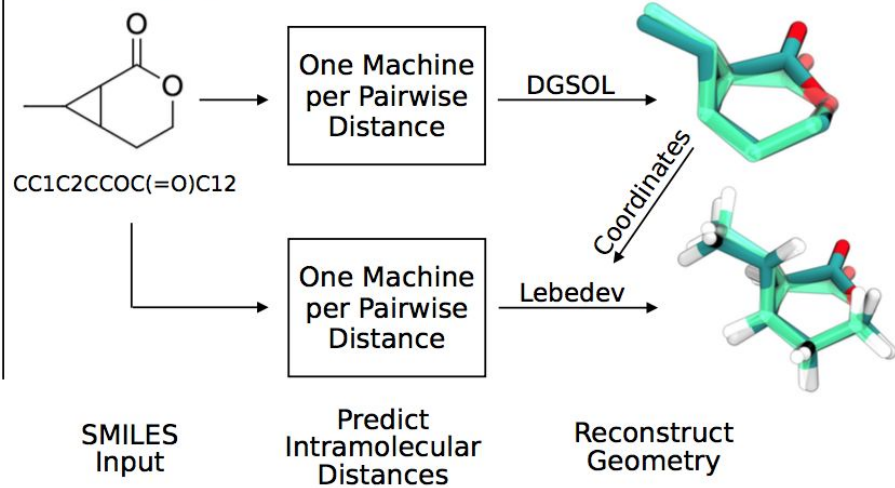


Graph to Structure (G2S)

Training

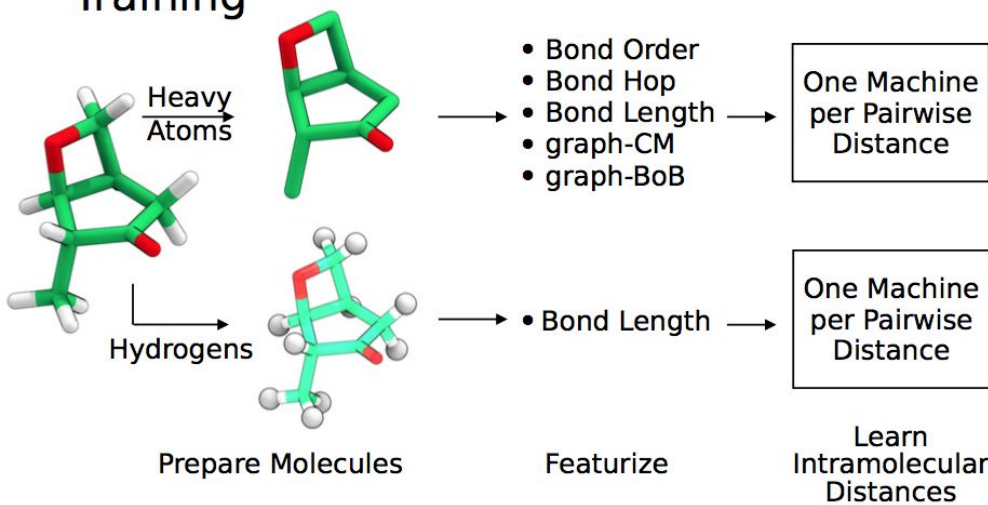


Prediction

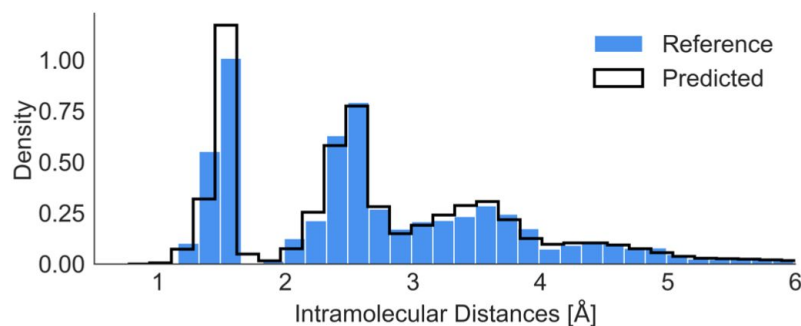
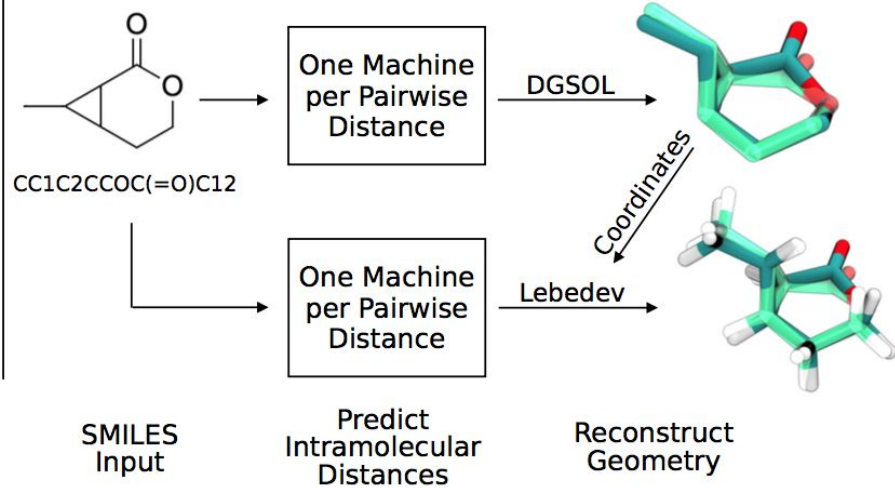


Graph to Structure (G2S)

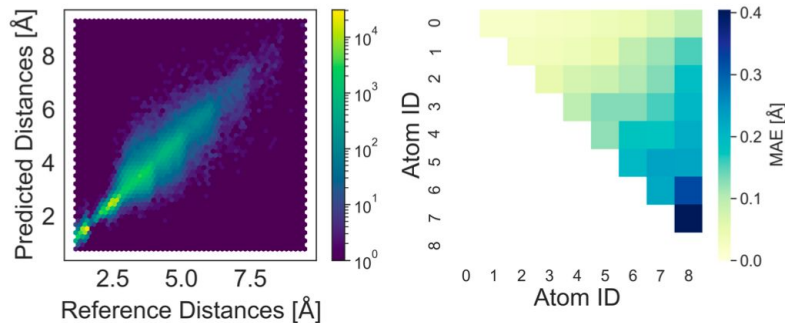
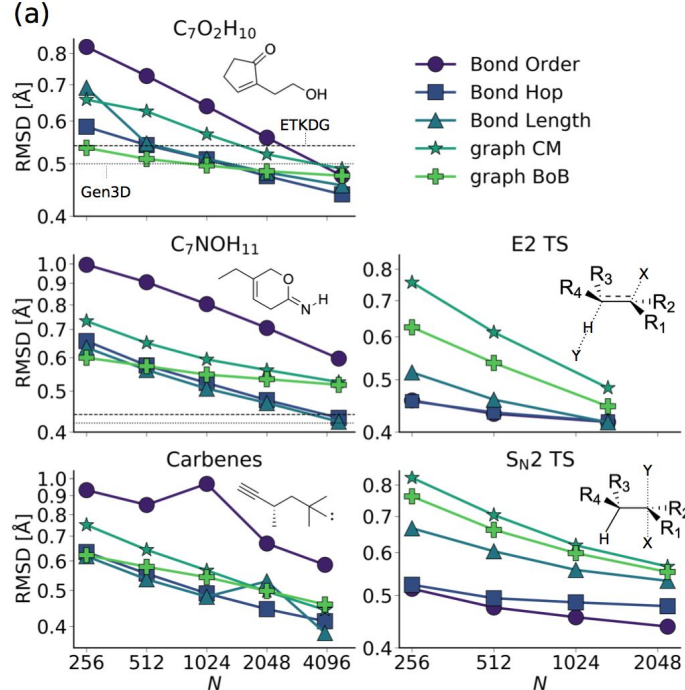
Training



Prediction

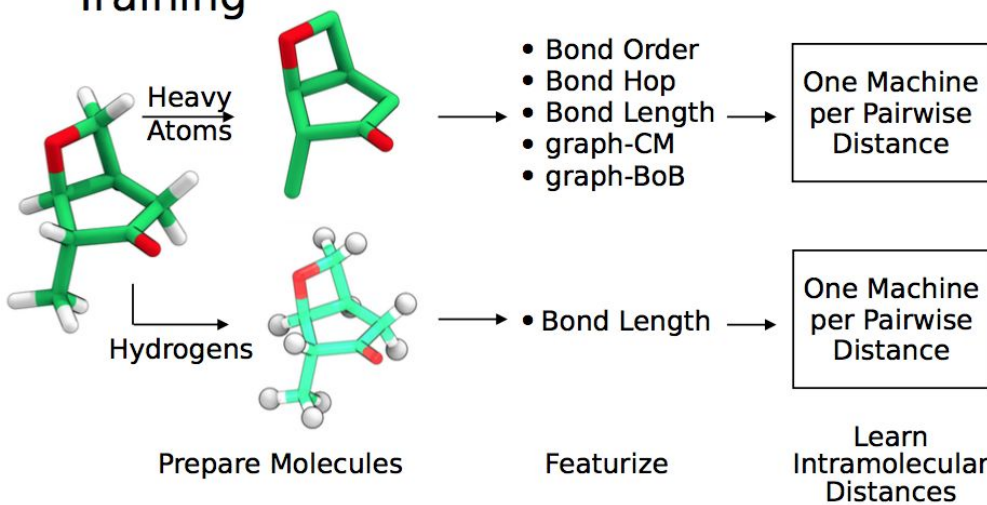


(a)

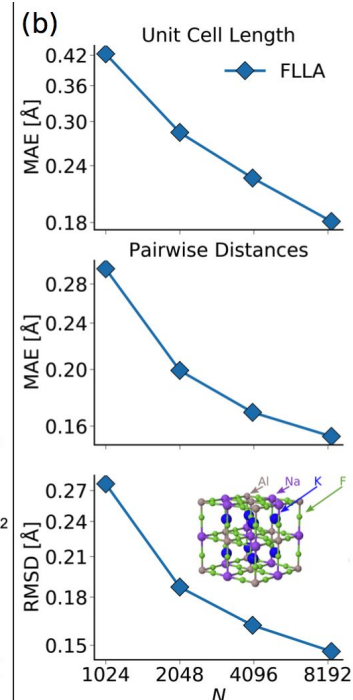
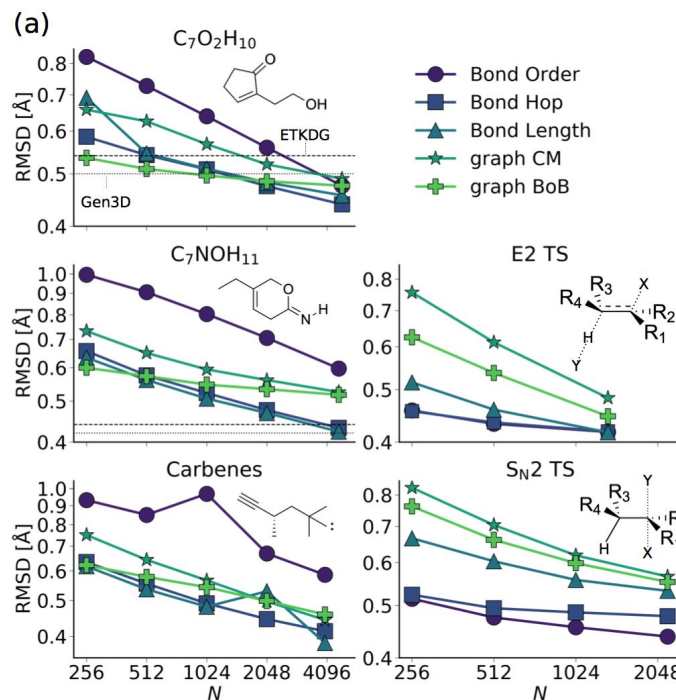
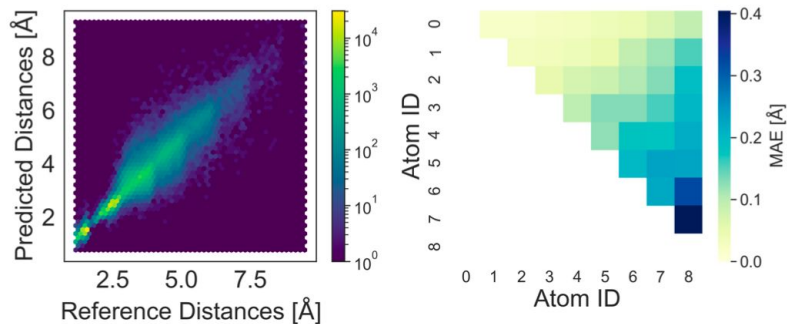
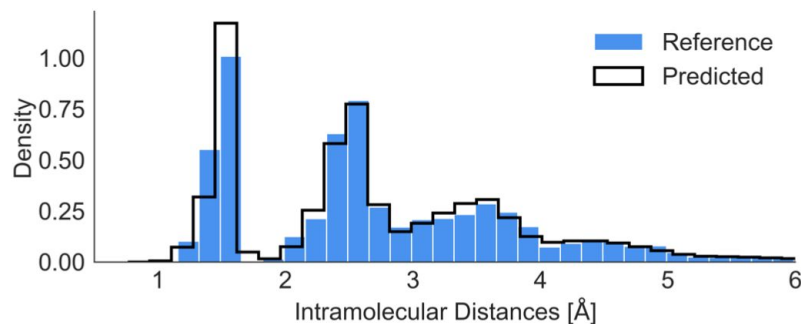
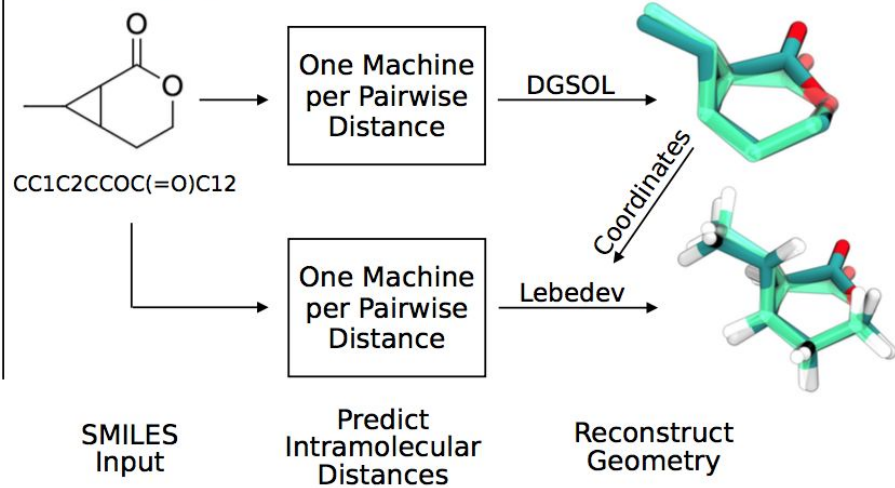


Graph to Structure (G2S)

Training

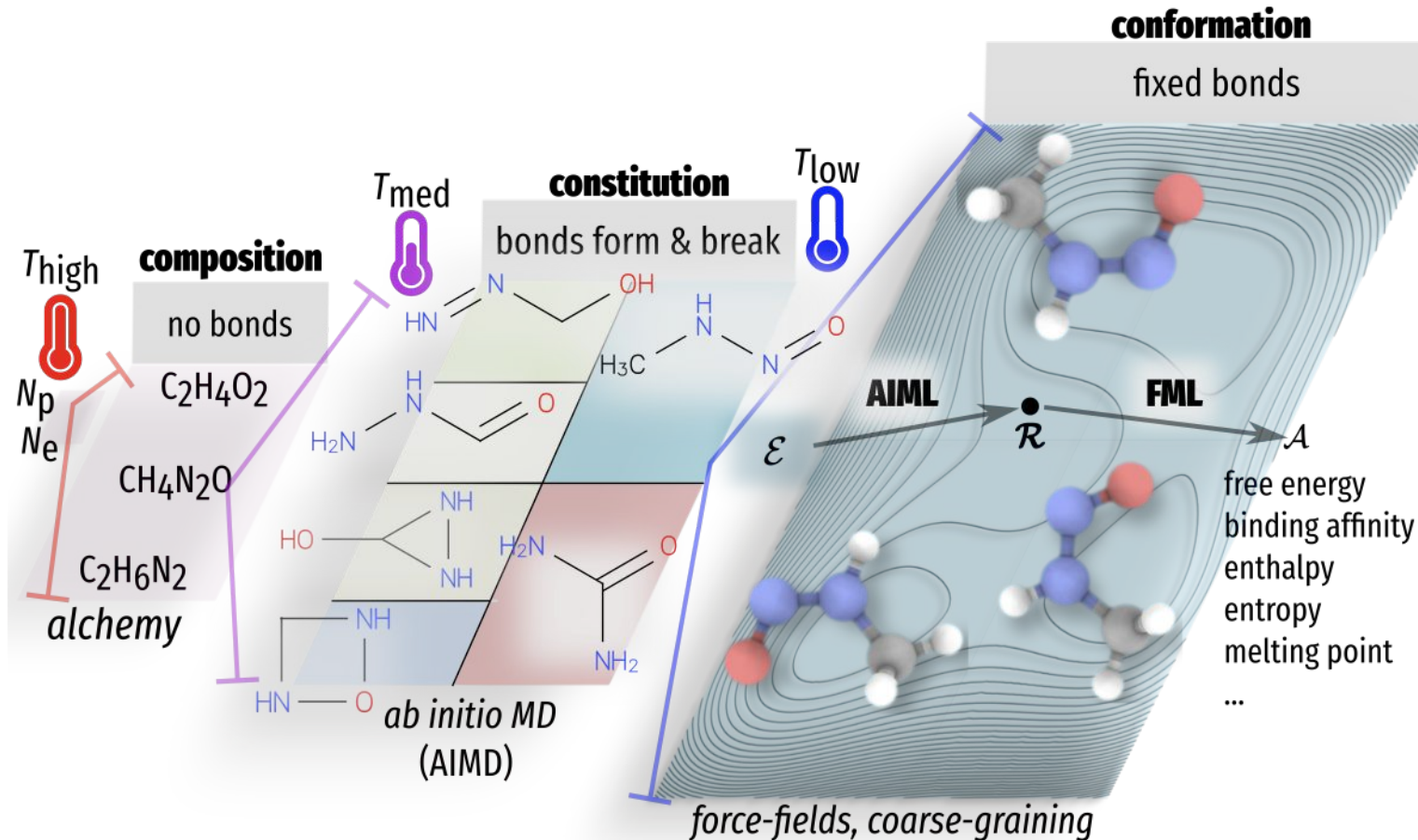


Prediction



Ab initio view on chemical space

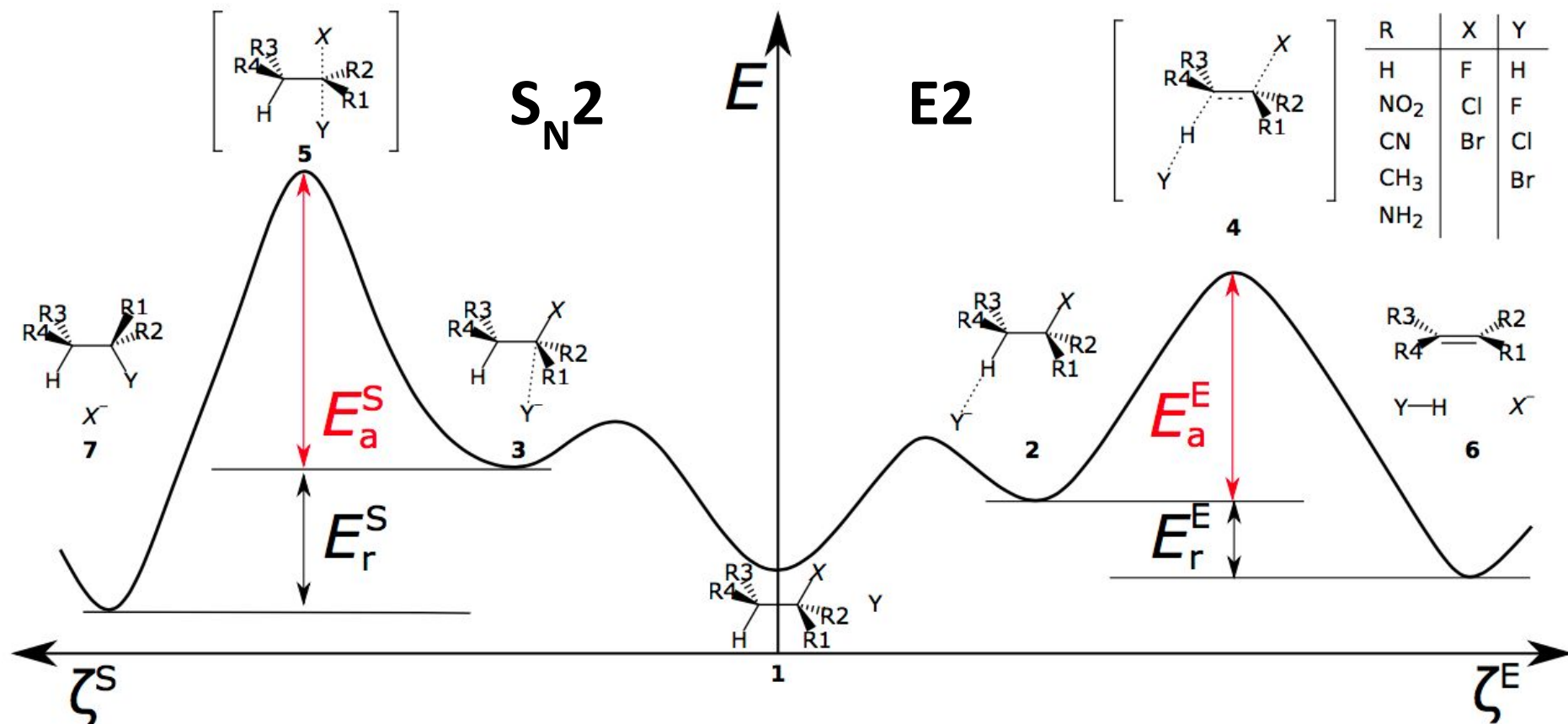
Weinreich et al, *Ab initio machine learning of phase space averages*, *J Chem Phys* (2022)



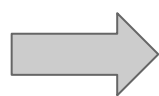
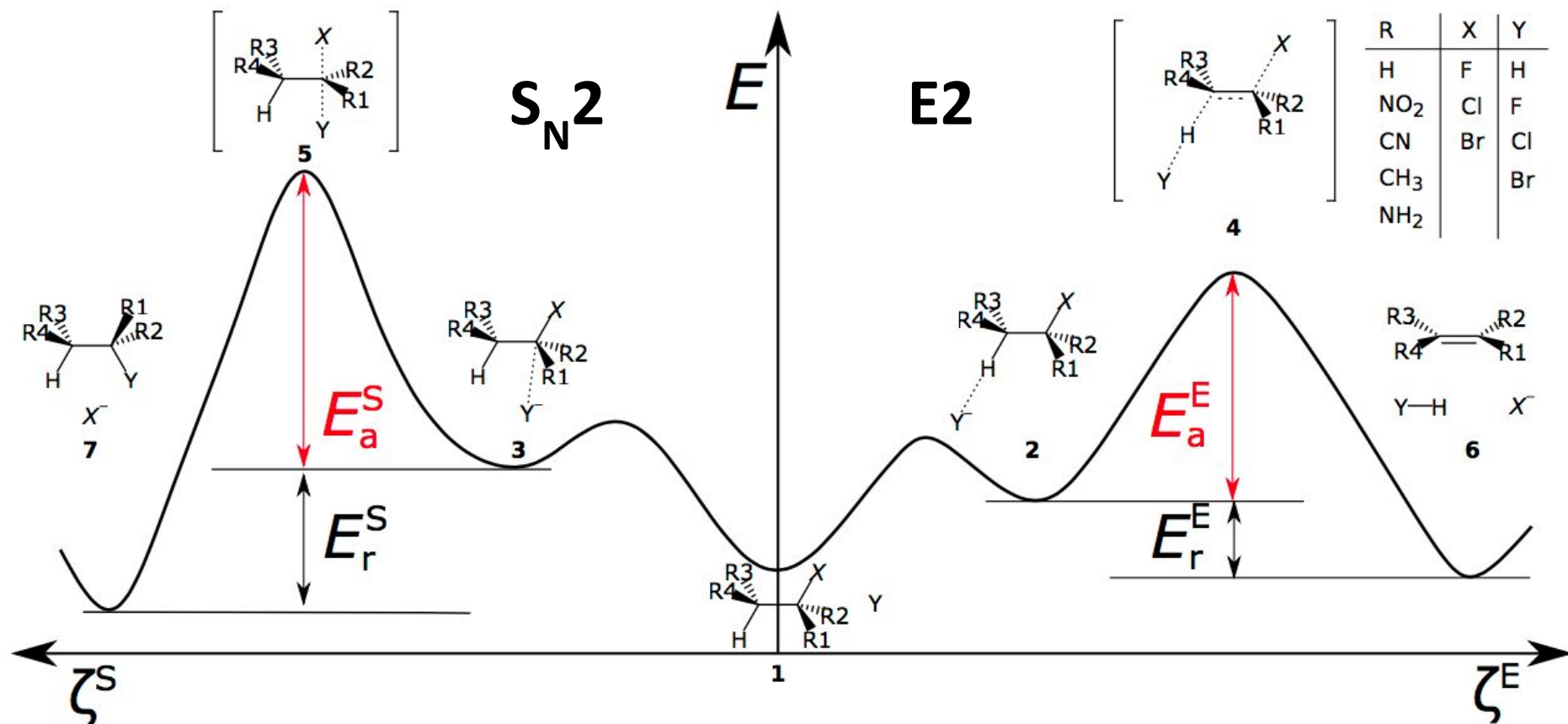
Predicting

1. structure (*Nat Commun* 2021)
2. reactivity (*J Chem Phys* 2021, *J Chem Phys* 2022)
3. Free energy (*J Chem Phys* 2021, *J Chem Phys* 2022)

RXN



RXN



Which is more frequent, E2 or S_N2?
Does Hammond's postulate hold?

Data: QMrxn

MACHINE
LEARNING
Science and Technology



OPEN ACCESS

RECEIVED
31 May 2020

REVISED
7 July 2020

ACCEPTED FOR PUBLICATION
21 July 2020

PUBLISHED
28 October 2020

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PAPER

Thousands of reactants and transition states for competing E2 and S_N2 reactions

Guido Falk von Rudorff , Stefan N Heinen , Marco Bragato and O Anatole von Lilienfeld

Institute of Physical Chemistry and National Center for Computational Design and Discovery of Novel Materials (MARVEL),
Department of Chemistry, University of Basel, Klingelbergstrasse 80, CH-4056 Basel, Switzerland

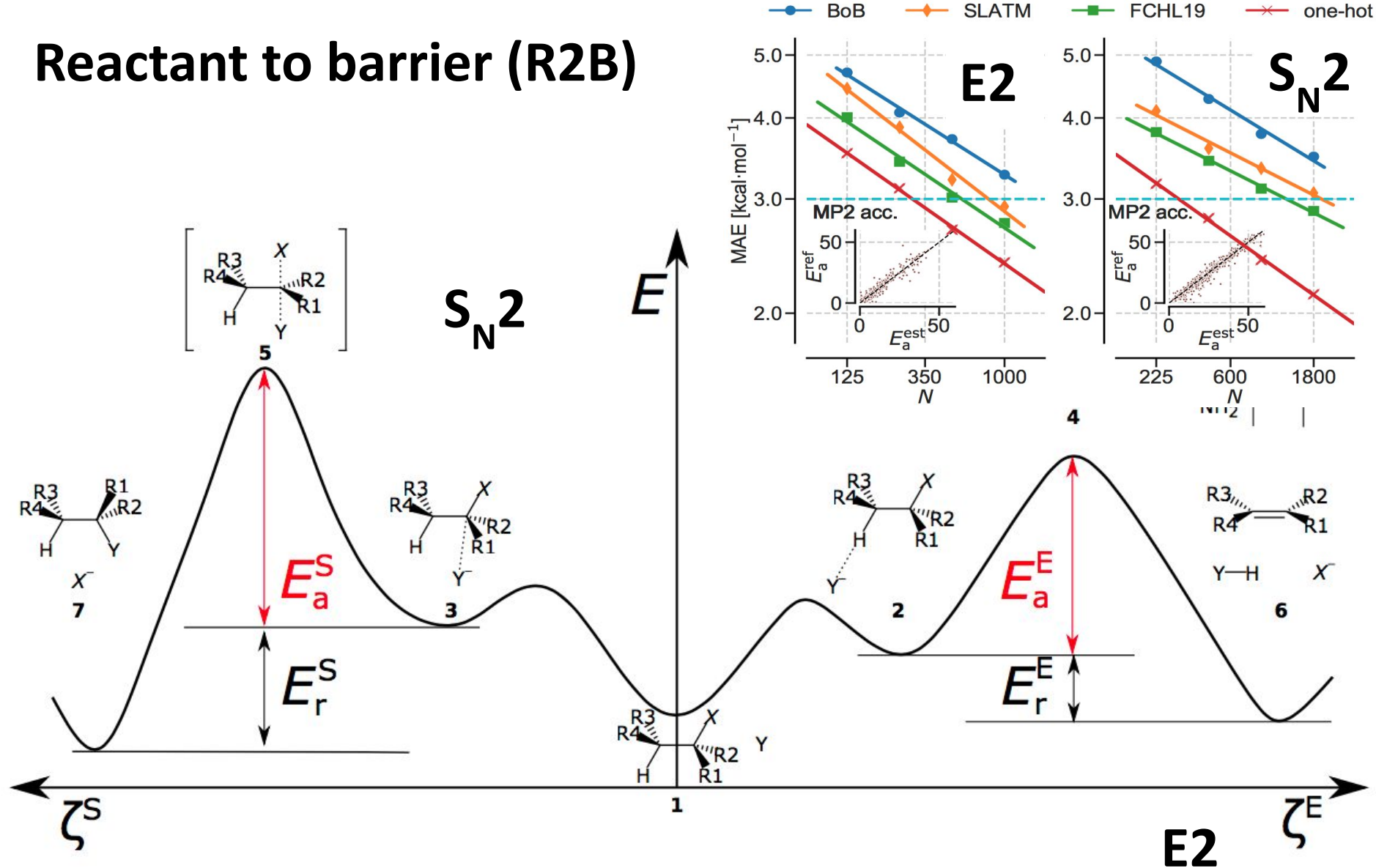
E-mail: anatole.vonlilienfeld@unibas.ch

Keywords: reactions, chemical space, competing reaction channels

Abstract

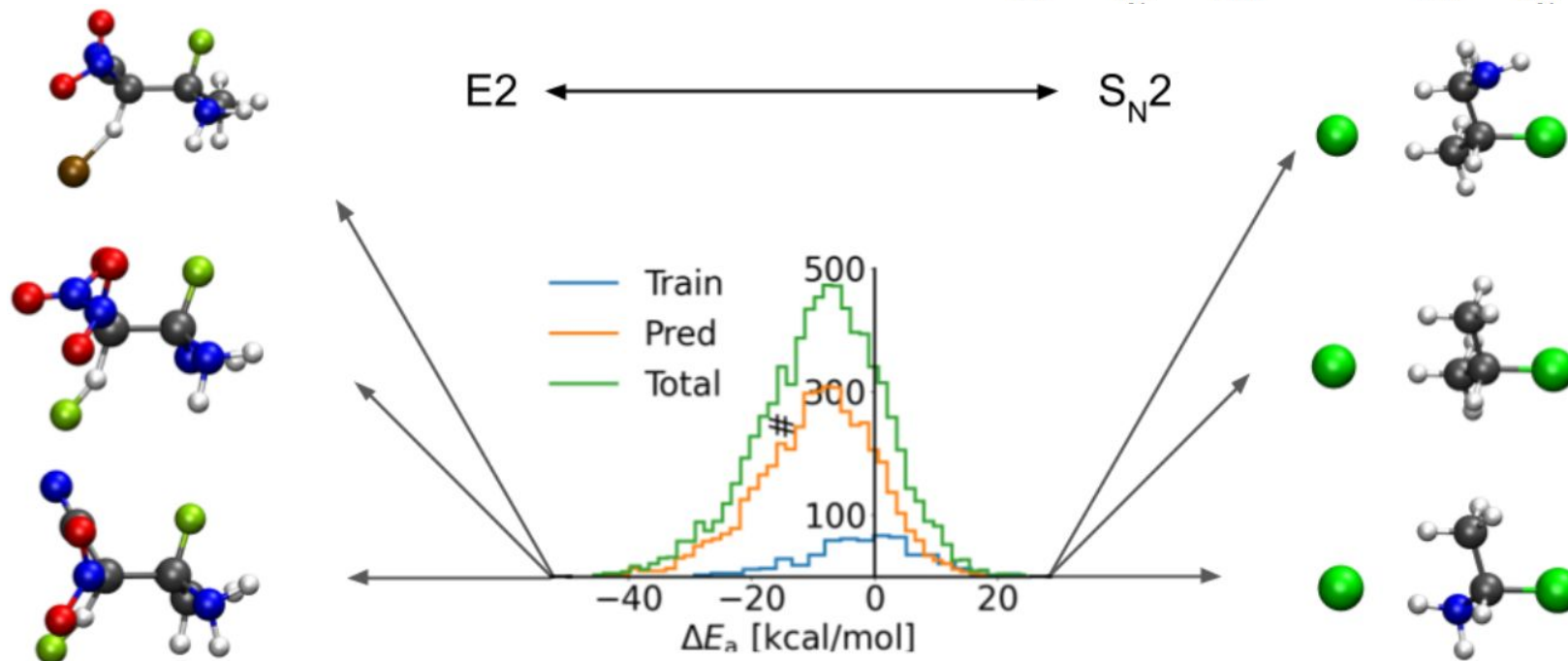
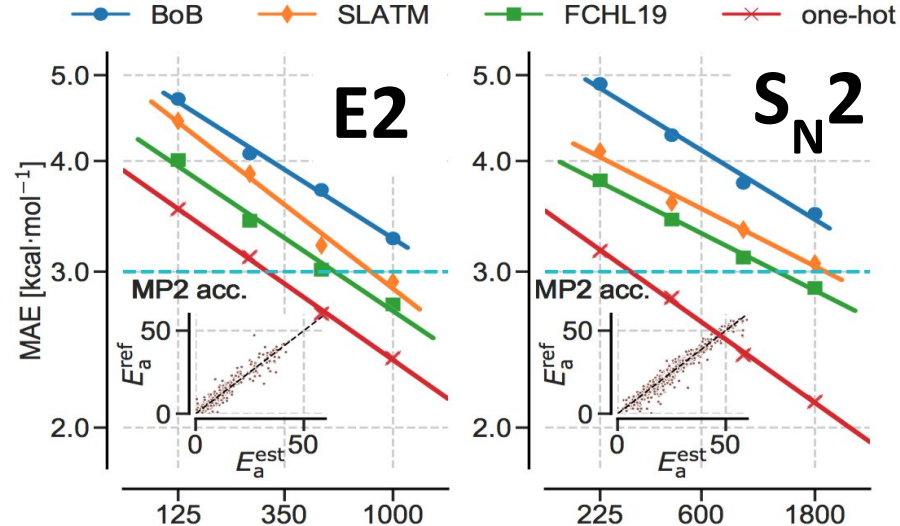
Reaction barriers are a crucial ingredient for first principles based computational retro-synthesis efforts as well as for comprehensive reactivity assessments throughout chemical compound space. While extensive databases of experimental results exist, modern quantum machine learning applications require atomistic details which can only be obtained from quantum chemistry protocols. For competing E2 and S_N2 reaction channels we report 4,466 transition state and 143,200 reactant complex geometries and energies at MP2/6-311G(d) and single point DF-LCCSD/cc-pVTZ level of theory, respectively, covering the chemical compound space spanned by the substituents NO₂, CN, CH₃, and NH₂ and early halogens (F, Cl, Br) and hydrogen as nucleophiles and early halogens as leaving groups. Reactants are chosen such that the activation energy of the competing E2 and S_N2 reactions are of comparable magnitude. The correct concerted motion for each of the one-step reactions has been validated for all transition states. We demonstrate how quantum machine learning models can support data set extension, and discuss the distribution of key internal coordinates of the transition states.

Reactant to barrier (R2B)



Which is more frequent, E2 or S_N2 ?
 ~11k R2B estimates: $\frac{3}{4}$ E2 vs $\frac{1}{4}$ S_N2

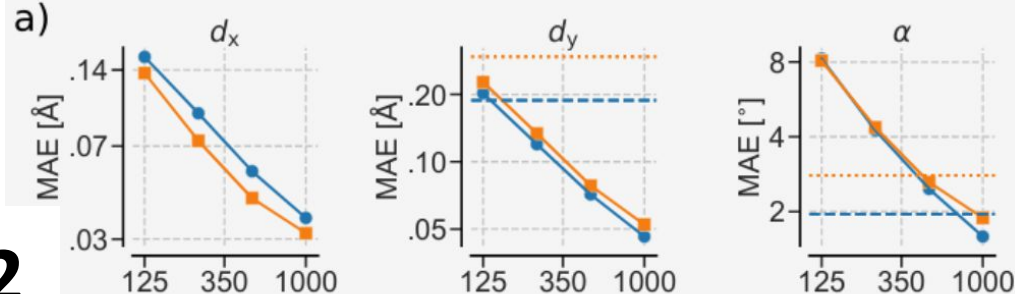
Reactant to barrier (R2B)



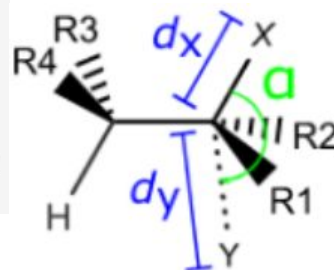
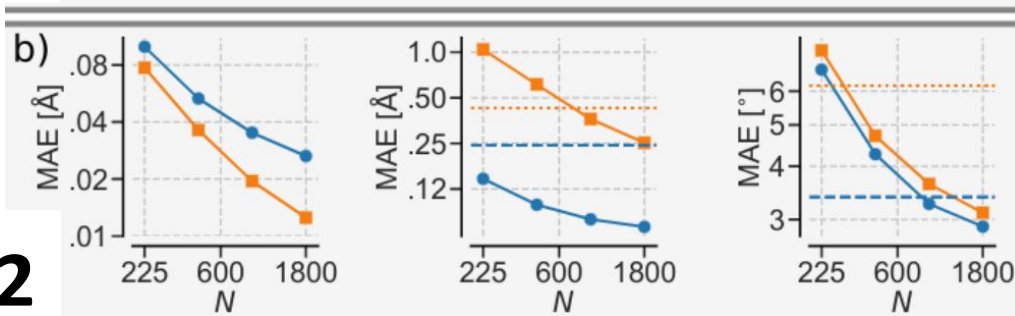
Which is more frequent, E2 or S_N2?
 ~11k R2B estimates: $\frac{3}{4}$ E2 vs $\frac{1}{4}$ S_N2

R2B

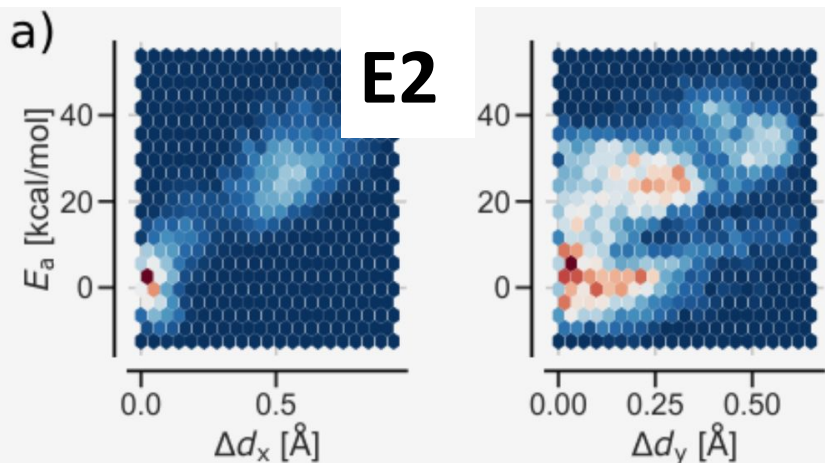
E2



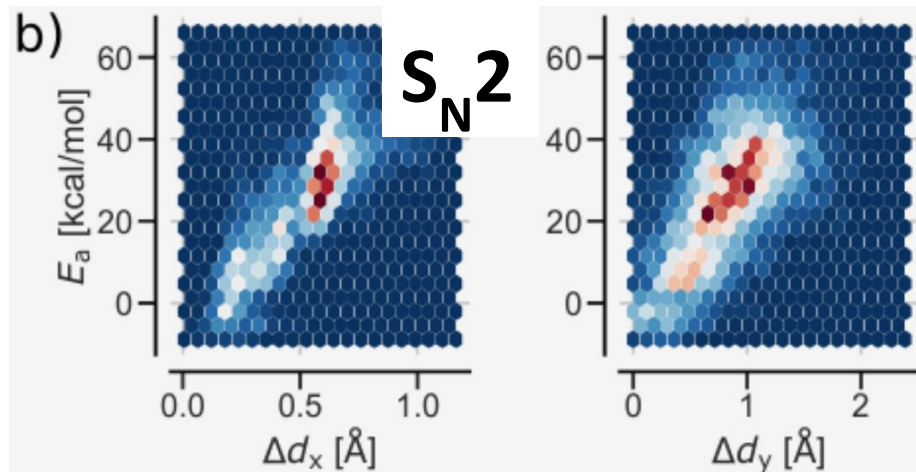
S_N2



E2

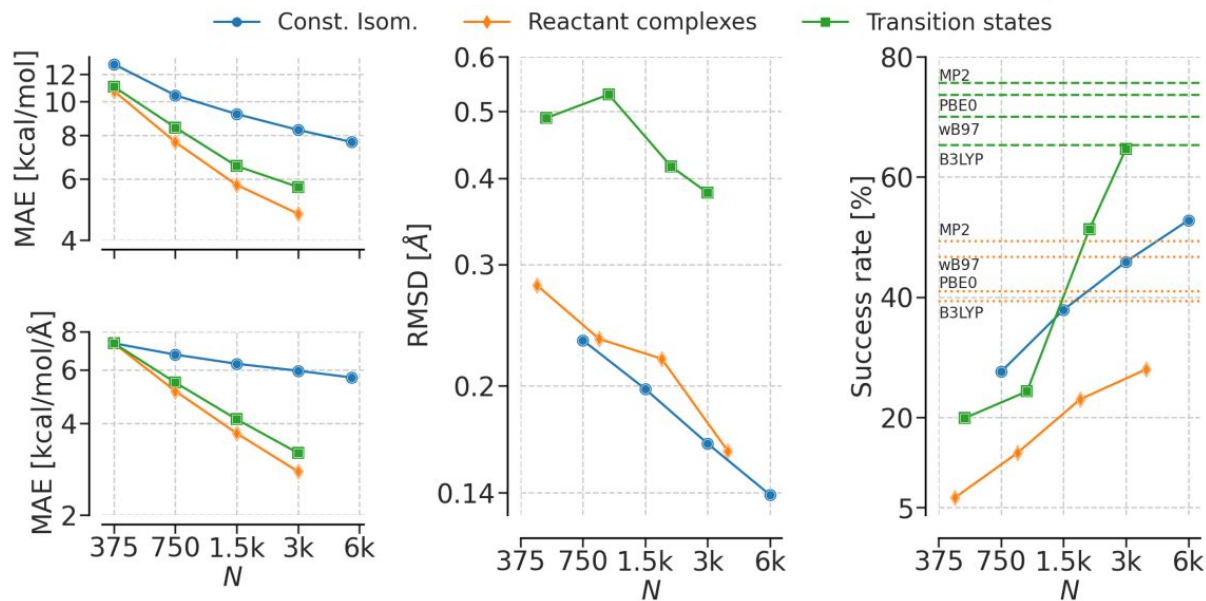
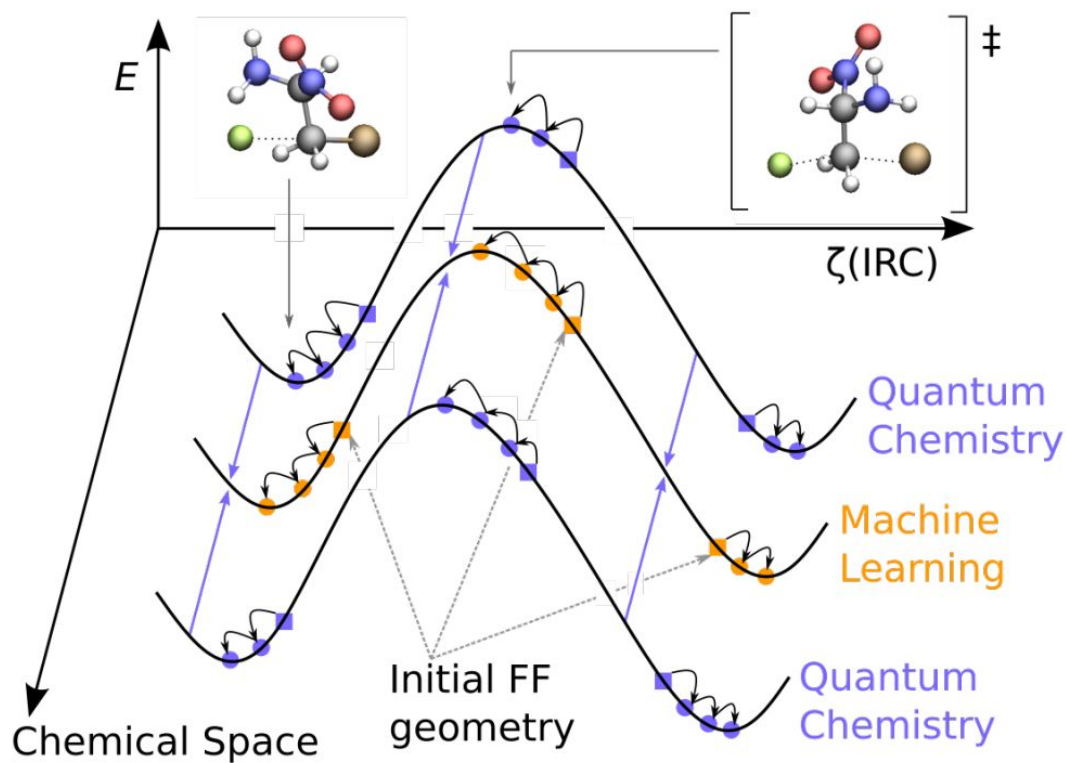


S_N2

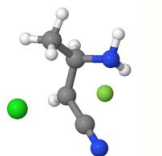
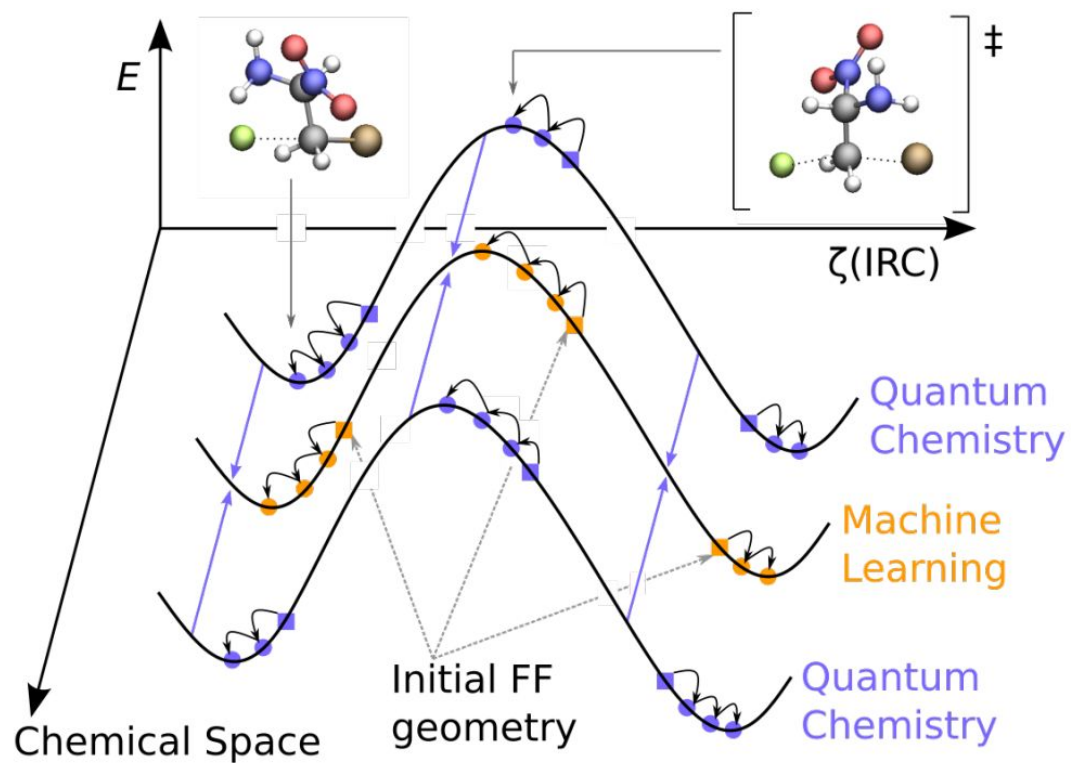
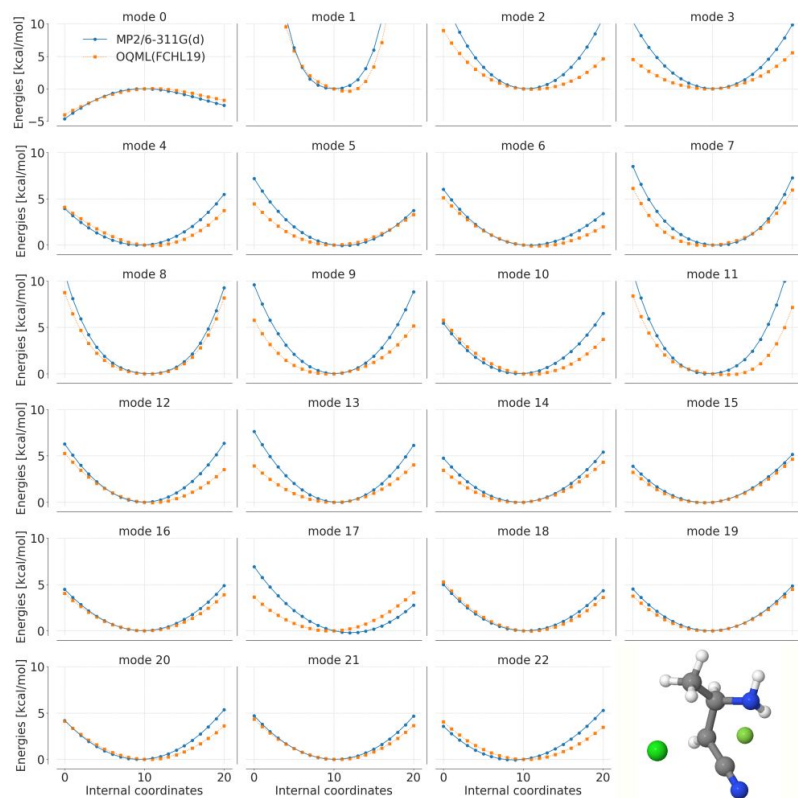


Hammond's postulate?
Yes for S_N2 , No for E2

TS search S_N2

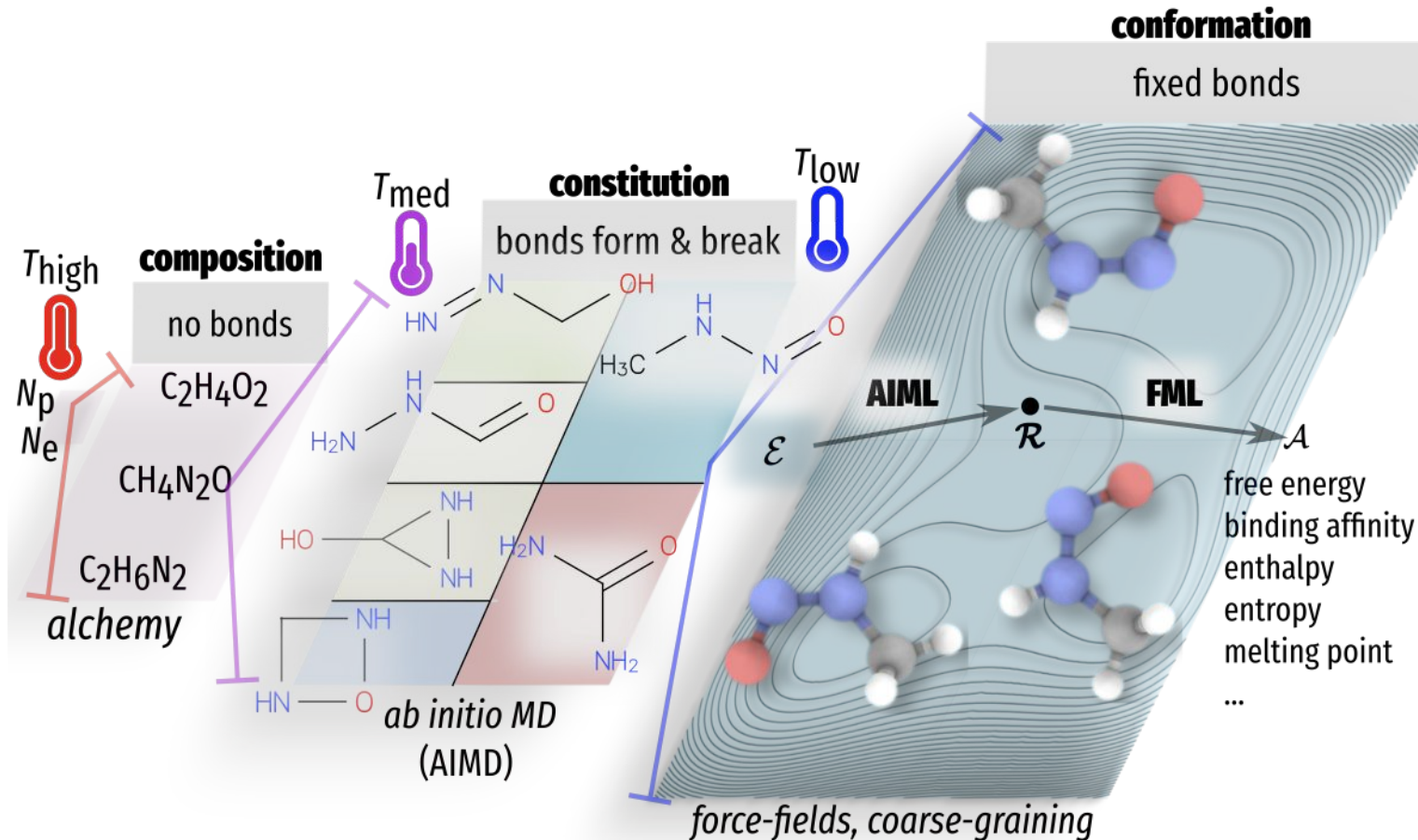


TS search S_N2



Ab initio view on chemical space

Weinreich et al, *Ab initio machine learning of phase space averages*, *J Chem Phys* (2022)



Predicting

1. structure (*Nat Commun* 2021)
2. reactivity (*J Chem Phys* 2021, *J Chem Phys* 2022)
3. Free energy (*J Chem Phys* 2021, *J Chem Phys* 2022)

Free energy

$$p_q = p(\mathbf{X}_q) = \sum_i^N \alpha_i K(\mathbf{X}_i^{\text{train.}}, \mathbf{X}_q)$$

$$K(\mathbf{X}_i, \mathbf{X}_j) = \exp\left(-\frac{\|\mathbf{X}_i - \mathbf{X}_j\|_2^2}{2\sigma^2}\right)$$

$$\alpha = (\mathbf{K} + \lambda \cdot \mathbf{1})^{-1} \mathbf{p}$$

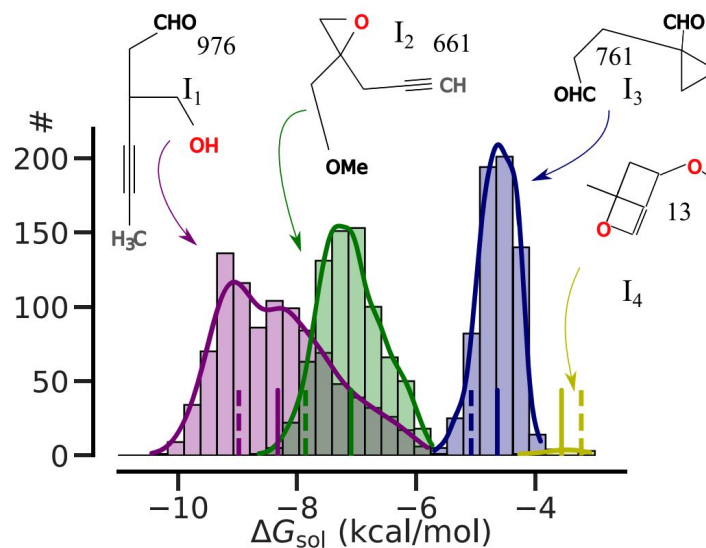
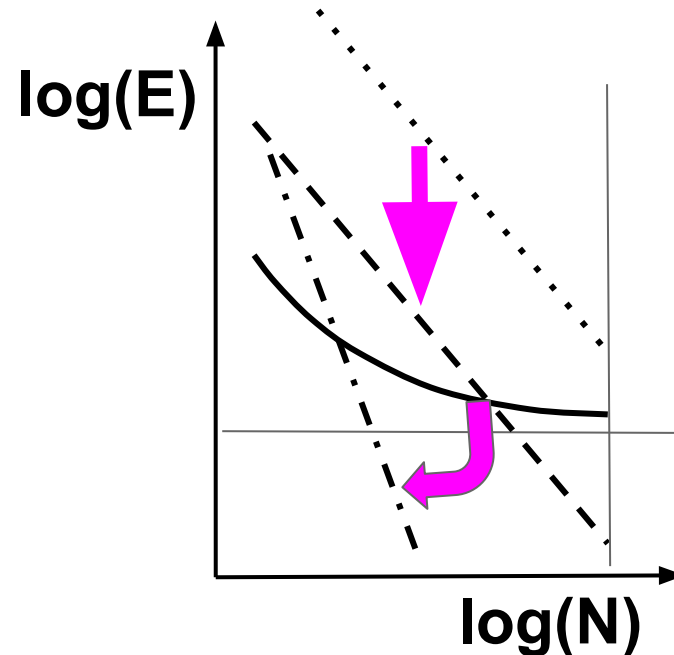


FIG. 4. Distribution of hydration free energies of conformers at 298K estimated by QML for four constitutional isomers ($\text{C}_7\text{H}_{10}\text{O}_2$). Corresponding FML estimates, as well as averages, are denoted by solid and dashed vertical lines, respectively. Insets show molecular graphs of corresponding constitutional isomers and number of conformers.

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$$\alpha = (\mathbf{K} + \lambda \cdot \mathbf{1})^{-1} \mathbf{p}$$

$$\bar{A} = \frac{\int A e^{-\beta H(q_1, q_2, \dots, q_M, p_1, p_2, \dots, p_N)} d\tau}{\int e^{-\beta H(q_1, q_2, \dots, q_M, p_1, p_2, \dots, p_N)} d\tau}$$

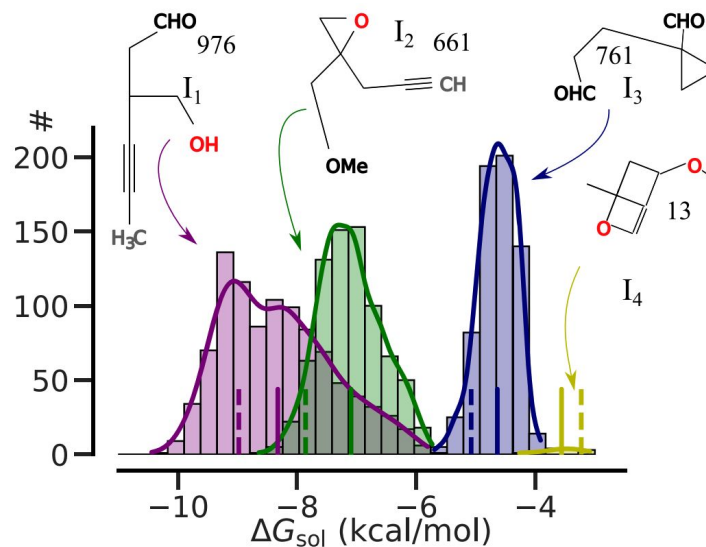
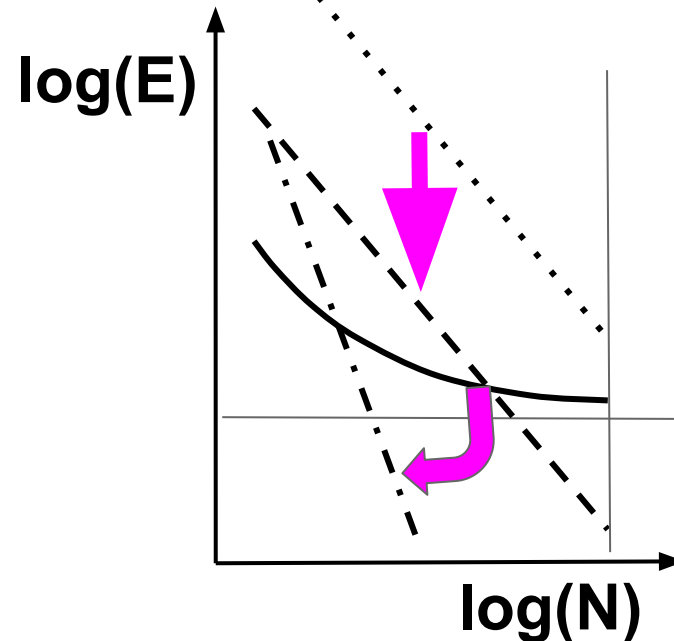


FIG. 4. Distribution of hydration free energies of conformers at 298K estimated by QML for four constitutional isomers ($\text{C}_7\text{H}_{10}\text{O}_2$). Corresponding FML estimates, as well as averages, are denoted by solid and dashed vertical lines, respectively. Insets show molecular graphs of corresponding constitutional isomers and number of conformers.

Free energy ML (FML)

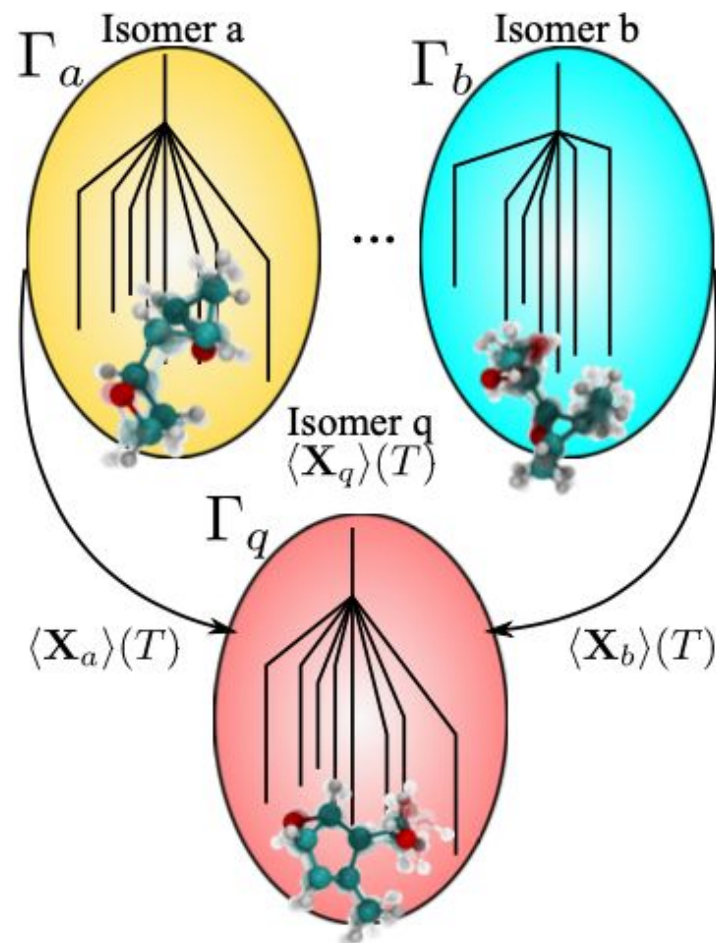
$$p_q = p(\mathbf{X}_q) = \sum_i^N \alpha_i K(\mathbf{X}_i^{\text{train.}}, \mathbf{X}_q)$$

$$K(\mathbf{X}_i, \mathbf{X}_j) = \exp\left(-\frac{\|\mathbf{X}_i - \mathbf{X}_j\|_2^2}{2\sigma^2}\right)$$

$$\alpha = (\mathbf{K} + \lambda \cdot \mathbf{1})^{-1} \mathbf{p}$$

$$\bar{A} = \frac{\int A e^{-\beta H(q_1, q_2, \dots, q_M, p_1, p_2, \dots, p_N)} d\tau}{\int e^{-\beta H(q_1, q_2, \dots, q_M, p_1, p_2, \dots, p_N)} d\tau}$$

$$\begin{aligned} \langle \mathbf{X} \rangle(T) &= \frac{1}{Z} \int_{\Gamma(T)} \mathbf{X}(\{\mathbf{r}_i\}) e^{-\beta E} d\Gamma \\ &\approx \frac{1}{N_s} \sum_i^{N_s} \mathbf{X}_i, \end{aligned}$$



FML

Training and Test: FreeSolv data base from:
G. Duarte Ramos Matos, D. Y. Kyu, H. H. Loeffler,
J. D. Chodera, M. R. Shirts, and D. L. Mobley, *J. Chem. Eng. Data* **62**, 1559 (2017).

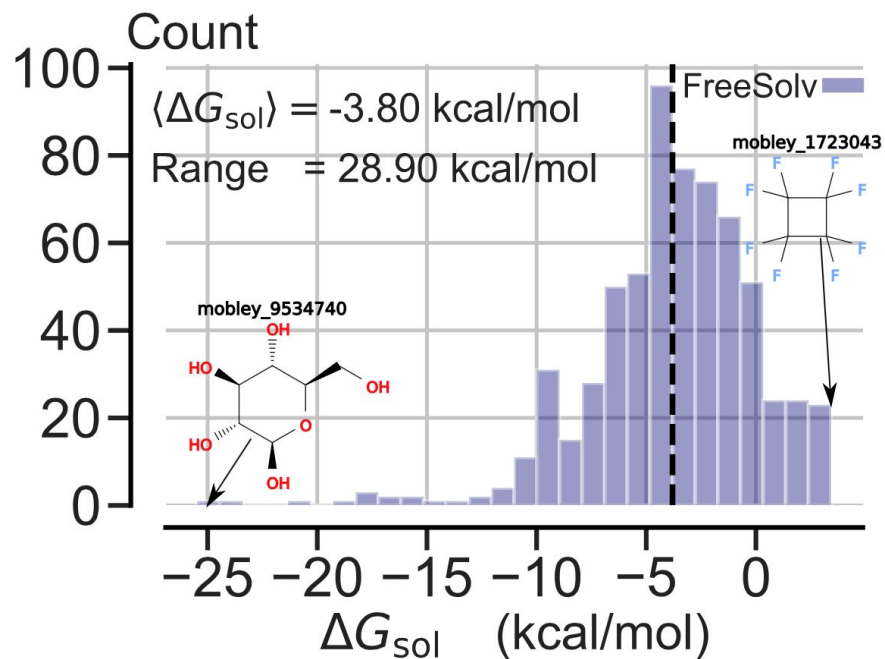


FIG. 3. Distribution of the experimental free energies of solvation provided by the FreeSolv database¹. The mean value of the free energies is indicated by a vertical line. The most and least soluble molecules and their identifier in the FreeSolv database are also shown.

FML

Training and Test: FreeSolv data base from:
 G. Duarte Ramos Matos, D. Y. Kyu, H. H. Loeffler,
 J. D. Chodera, M. R. Shirts, and D. L. Mobley, *J. Chem. Eng. Data* **62**, 1559 (2017).

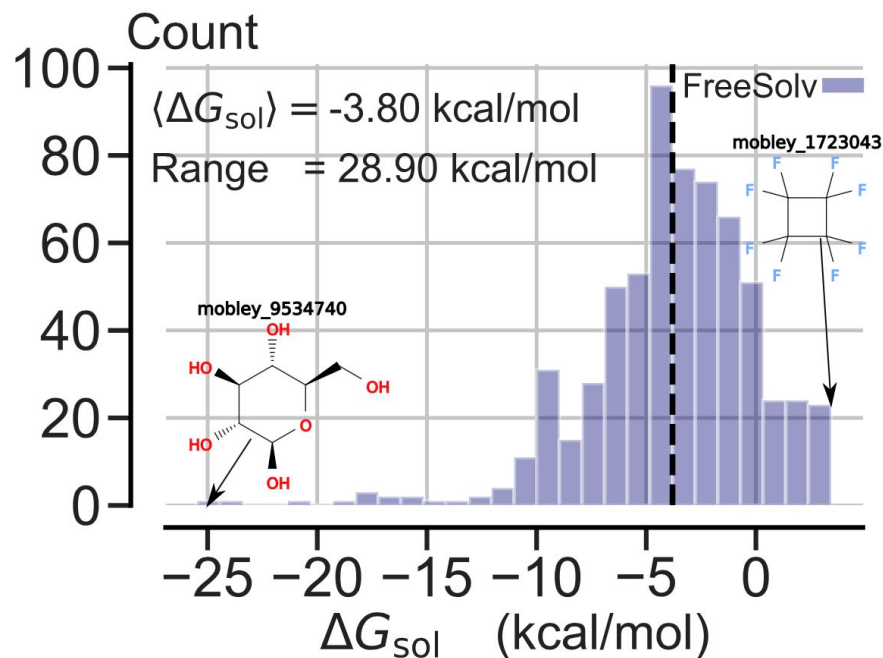
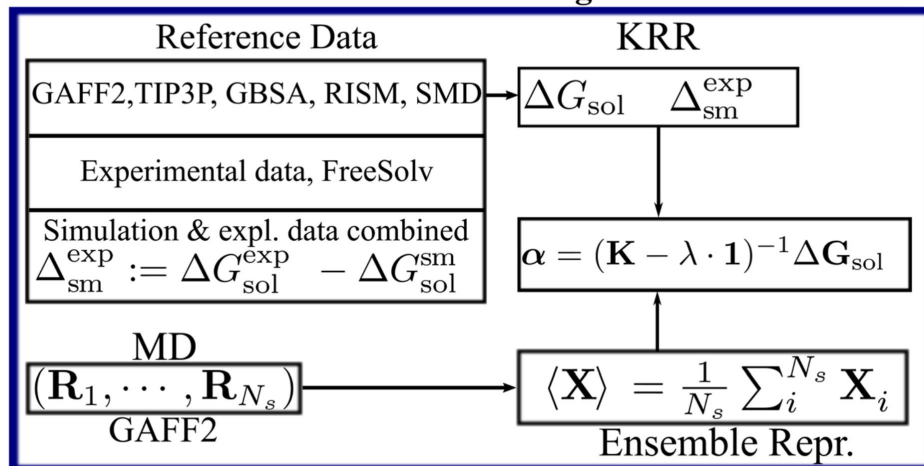
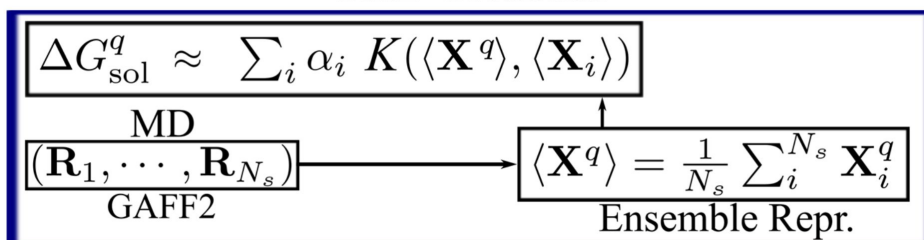


FIG. 3. Distribution of the experimental free energies of solvation provided by the FreeSolv database¹. The mean value of the free energies is indicated by a vertical line. The most and least soluble molecules and their identifier in the FreeSolv database are also shown.

FML - Training



FML - Prediction



FML

Training and Test: FreeSolv data base from:
G. Duarte Ramos Matos, D. Y. Kyu, H. H. Loeffler,
J. D. Chodera, M. R. Shirts, and D. L. Mobley, *J. Chem. Eng. Data* **62**, 1559 (2017).

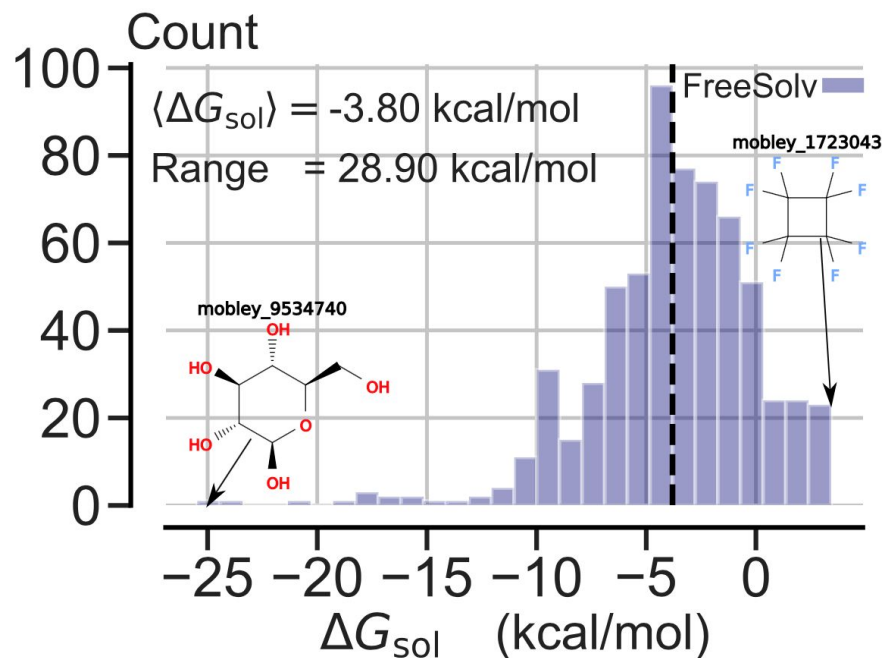
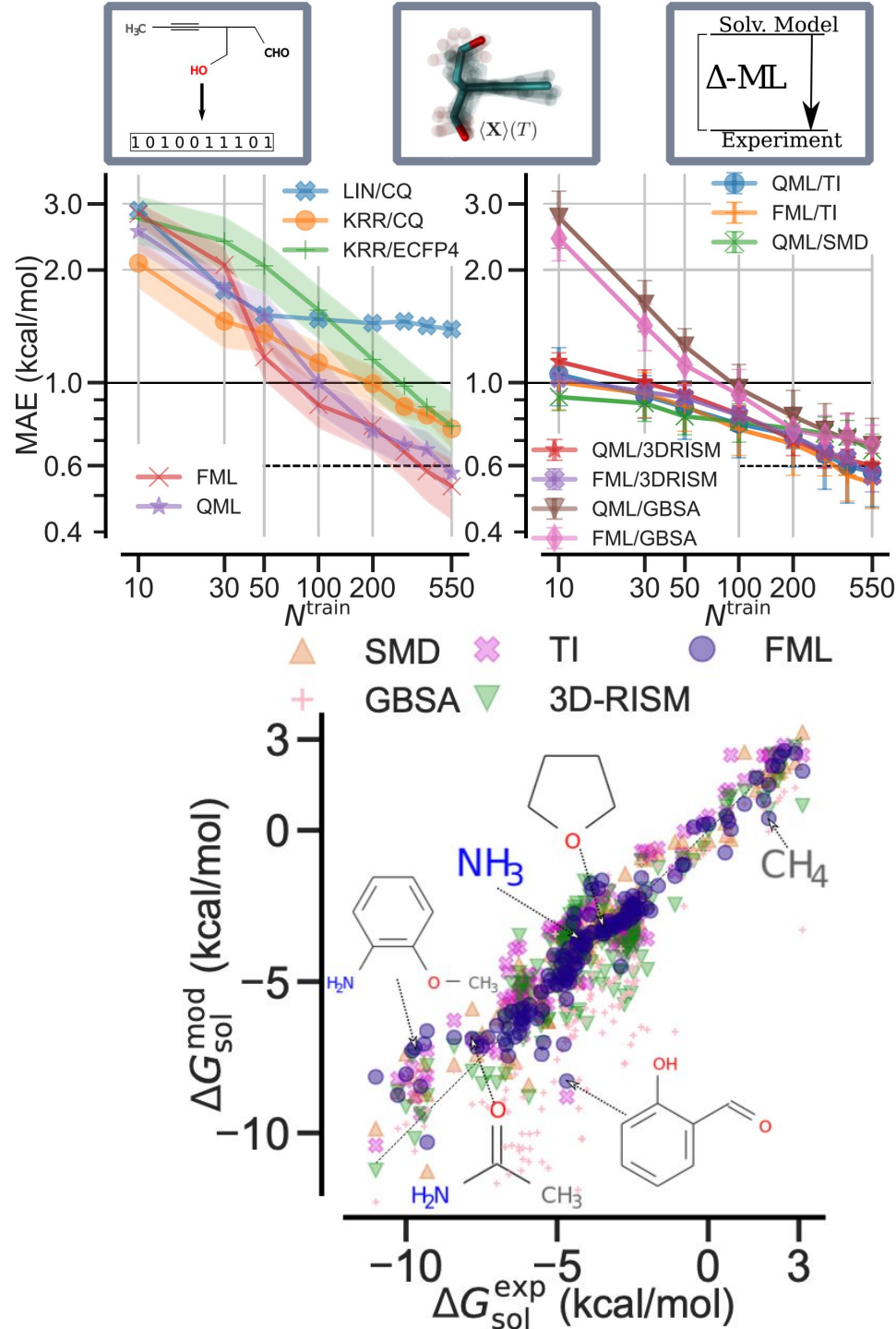


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FML

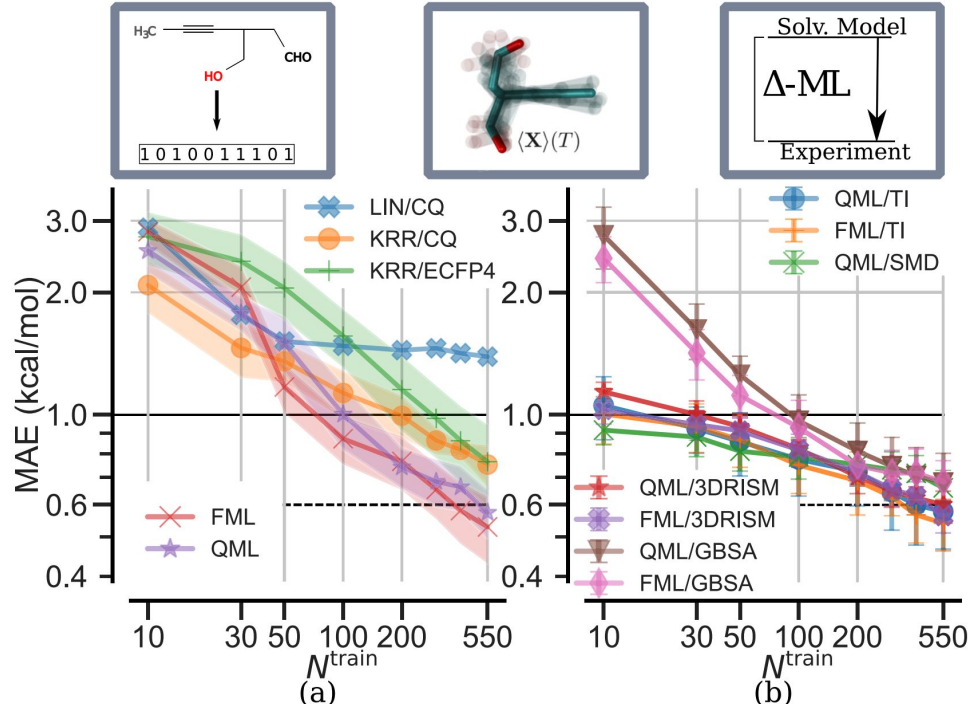


TABLE I. Comparison of MAEs, Pearson's r , and estimated order of CPU time per solute prediction for various solvation models and FML. Approximate number of training molecules N^{train} needed for FML to reach the MAE of each respective method. The conversion factor from GPU to CPU $c = \frac{t_{\text{CPU}}}{t_{\text{GPU}}}$ may vary substantially between ~ 10 and 60 depending on hardware/MD code (here OpenMM⁵⁸). g is the number of grid points for TI, typically ~ 10 .

Class	Model	MAE (kcal/mol)	r	N^{train}	$\sim$ CPU h/solute	References	Year of publication
DFT	SMD	0.61 ¹⁴	0.96	400	<i>High</i>	8 and 71	2009
	COSMO	1.94	0.90	20	10^{-1}	9, 10, and 72	1993
	COSMO-RS	0.52 ⁷⁸	0.91	...	10^{-1}	11, 72, 76, and 78	2000
	DCOSMO-RS	0.94 ⁷⁸	0.87	100	10^{-1}	79	2006
FF	3D-RISM	0.99 ¹⁴	0.90	100	10^{-1}	12 and 13	1998
	TI	0.93 ⁵⁵	0.94	100	$g \times c \times 10^{-1}$	55	2017
	GBSA	2.41	0.84	20	10^{-2}	63 and 64	2004
ML	FML	0.57	0.95	490	10^{-2}	This work	2020

FML

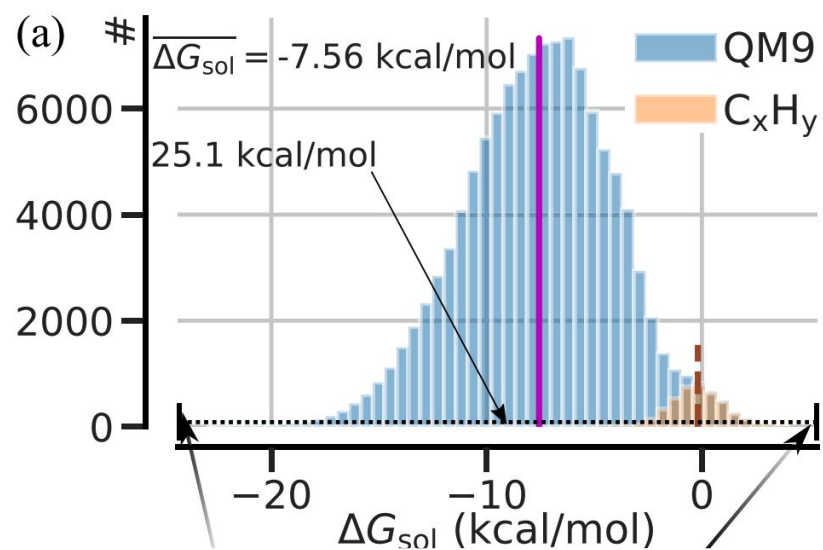


FIG. 7. Free energy distribution of 116k molecules predicted by FML in (a); small histogram corresponds to a subset of 4907 hydrocarbons with averages shown as solid and dashed lines, respectively. Four molecules with most negative (b) and positive (c) ΔG_{sol} in clockwise order. The mean of ΔG_{sol} for simple descriptors such as number of H-bond donors H_d (d), NH/OH groups (e), oxygen atoms O in stoichiometry $\text{C}_{n_C}\text{H}_{n_H}\text{O}_{n_O}$ (f), and heavy atoms h (g).

FML

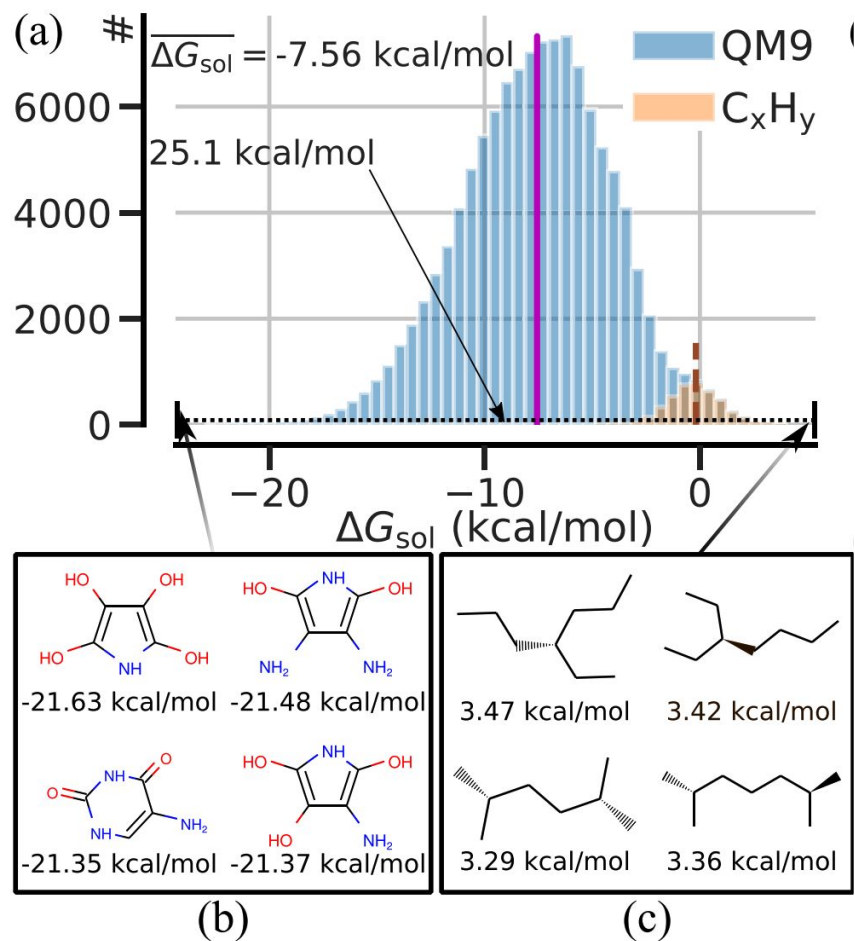


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FML

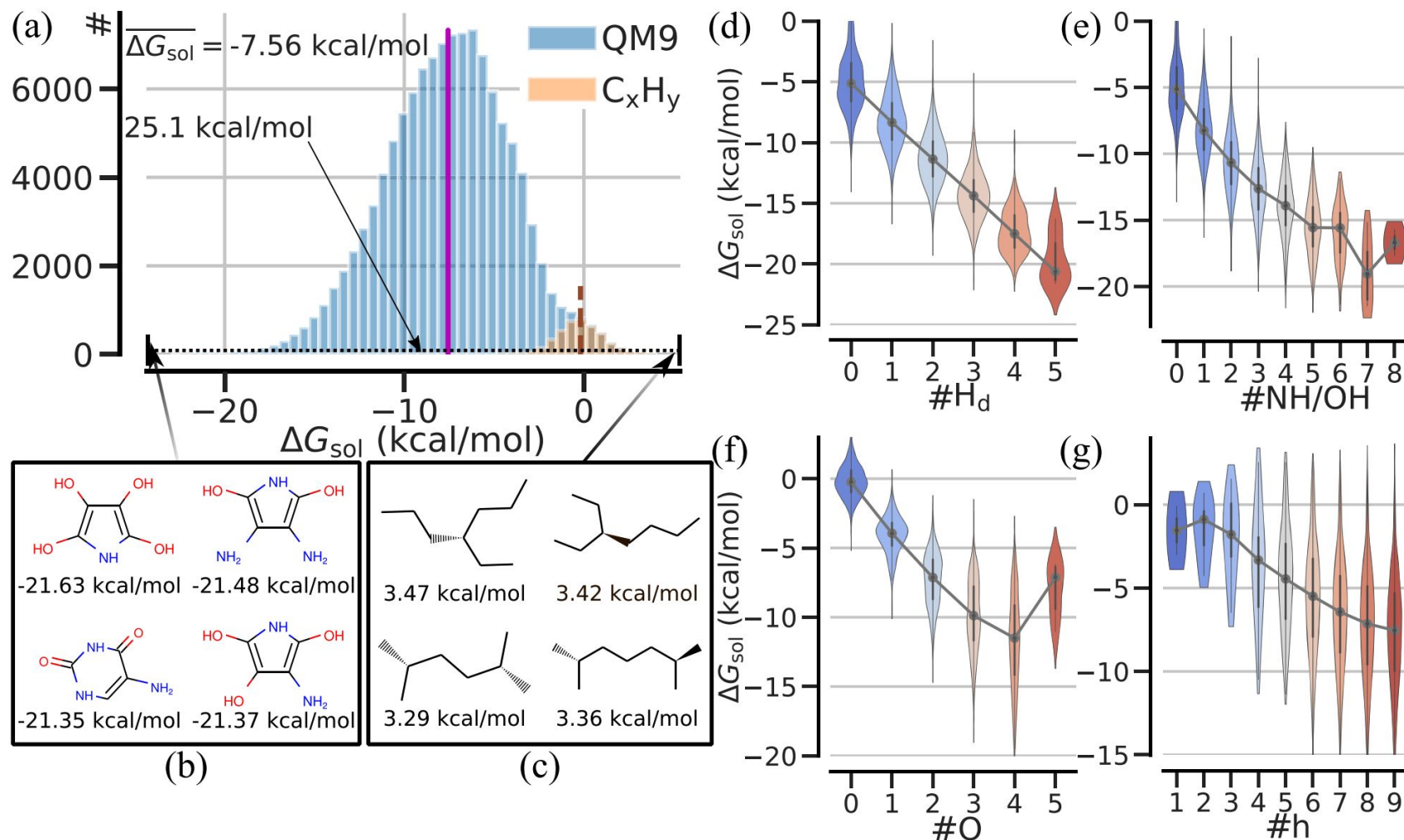
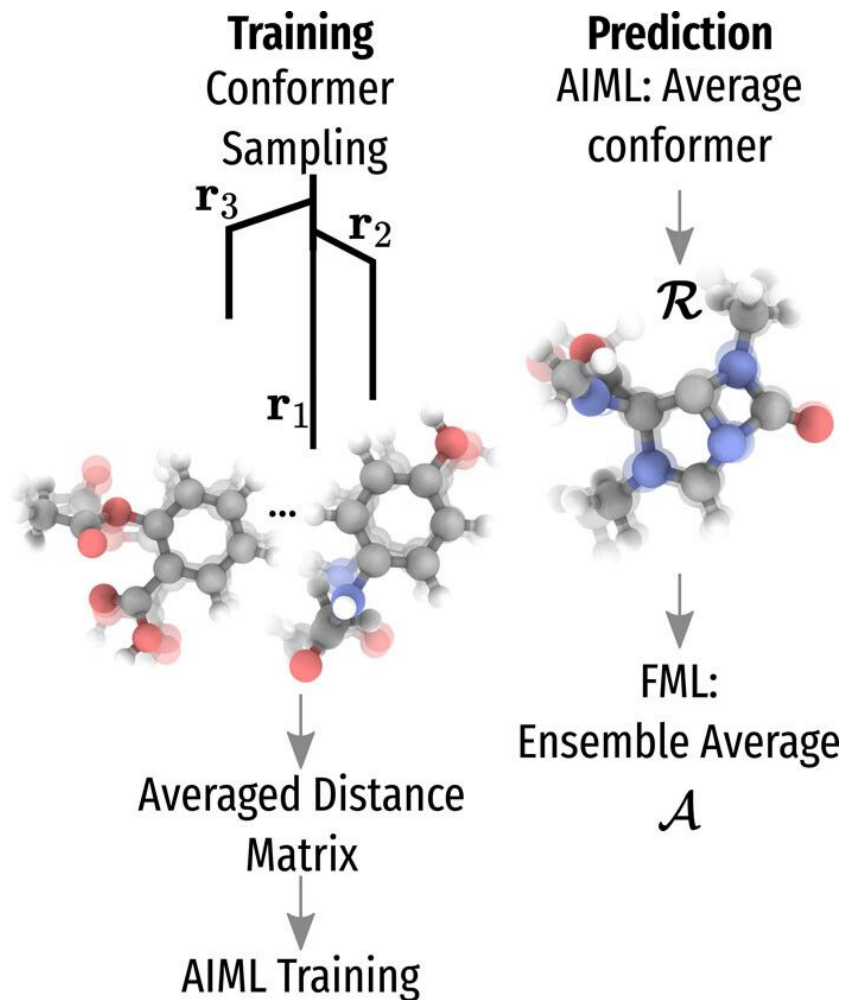
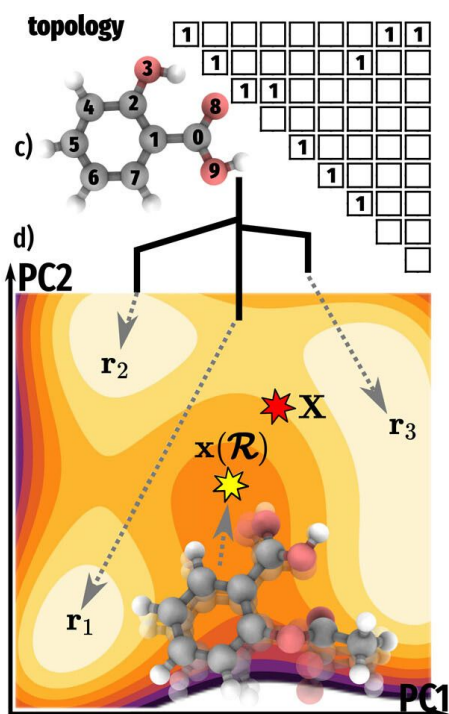
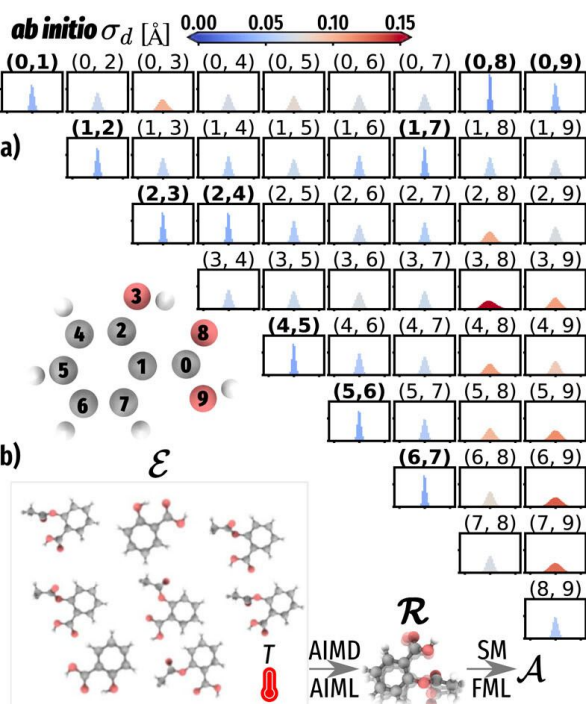


FIG. 7. Free energy distribution of 116k molecules predicted by FML in (a); small histogram corresponds to a subset of 4907 hydrocarbons with averages shown as solid and dashed lines, respectively. Four molecules with most negative (b) and positive (c) ΔG_{sol} in clockwise order. The mean of ΔG_{sol} for simple descriptors such as number of H-bond donors H_d (d), NH/OH groups (e), oxygen atoms O in stoichiometry $\text{C}_{n_C}\text{H}_{n_H}\text{O}_{n_O}$ (f), and heavy atoms h (g).

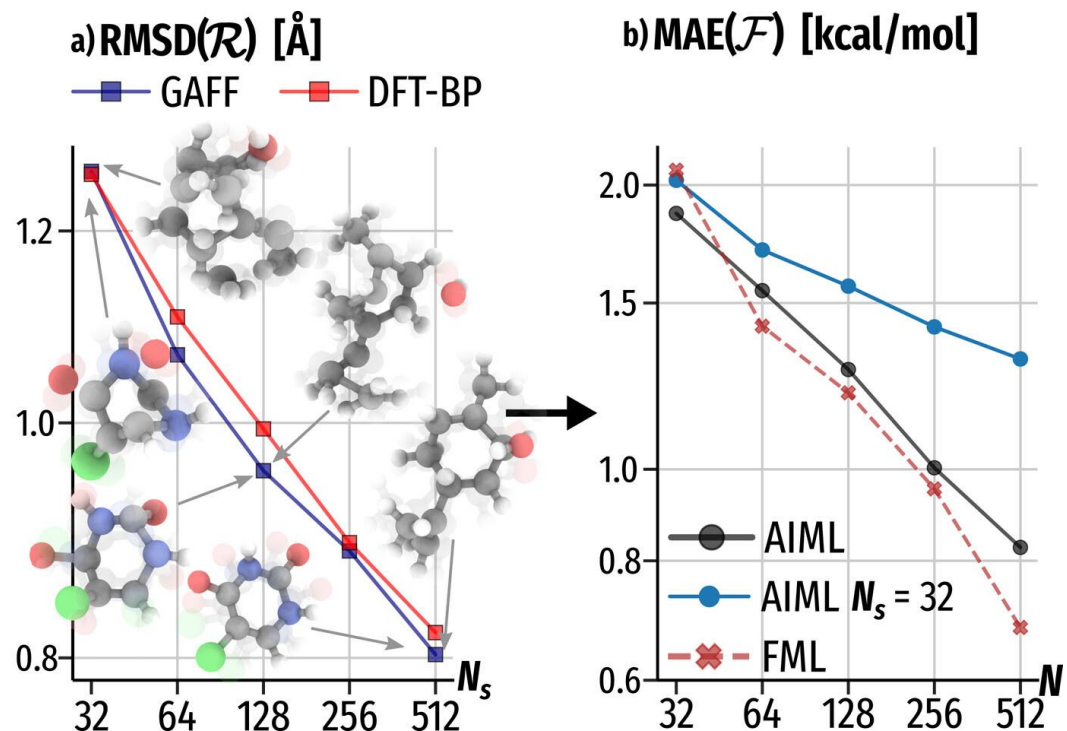
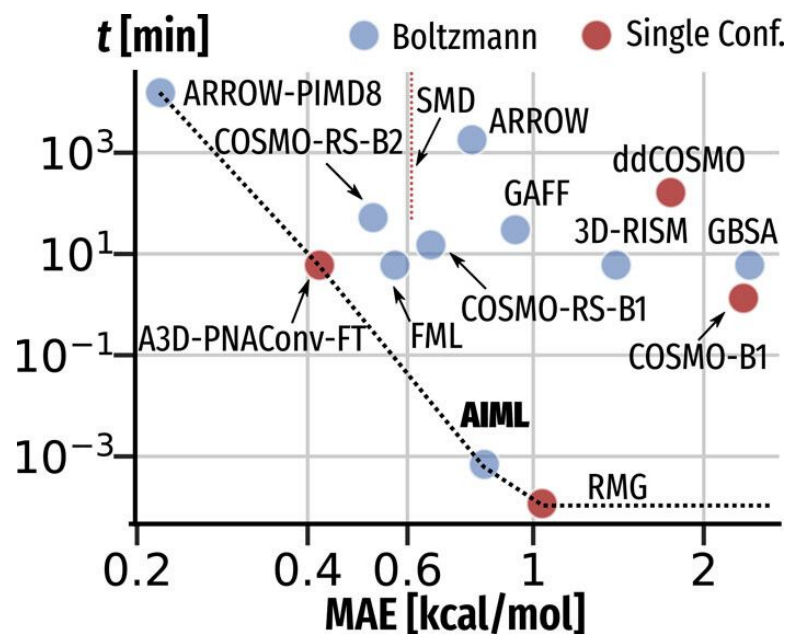
AIML of <...>

$$\mathcal{A} = \frac{1}{Z} \int a(\mathbf{r}, \mathbf{p}) e^{-\beta E(\mathbf{r}, \mathbf{p})} d\mathbf{r} d\mathbf{p} \approx \mathcal{A}^{\text{ML}}(\mathcal{R})$$

$$\mathcal{E} \rightarrow \mathcal{R} \rightarrow \mathcal{A}$$



AIML of <...>



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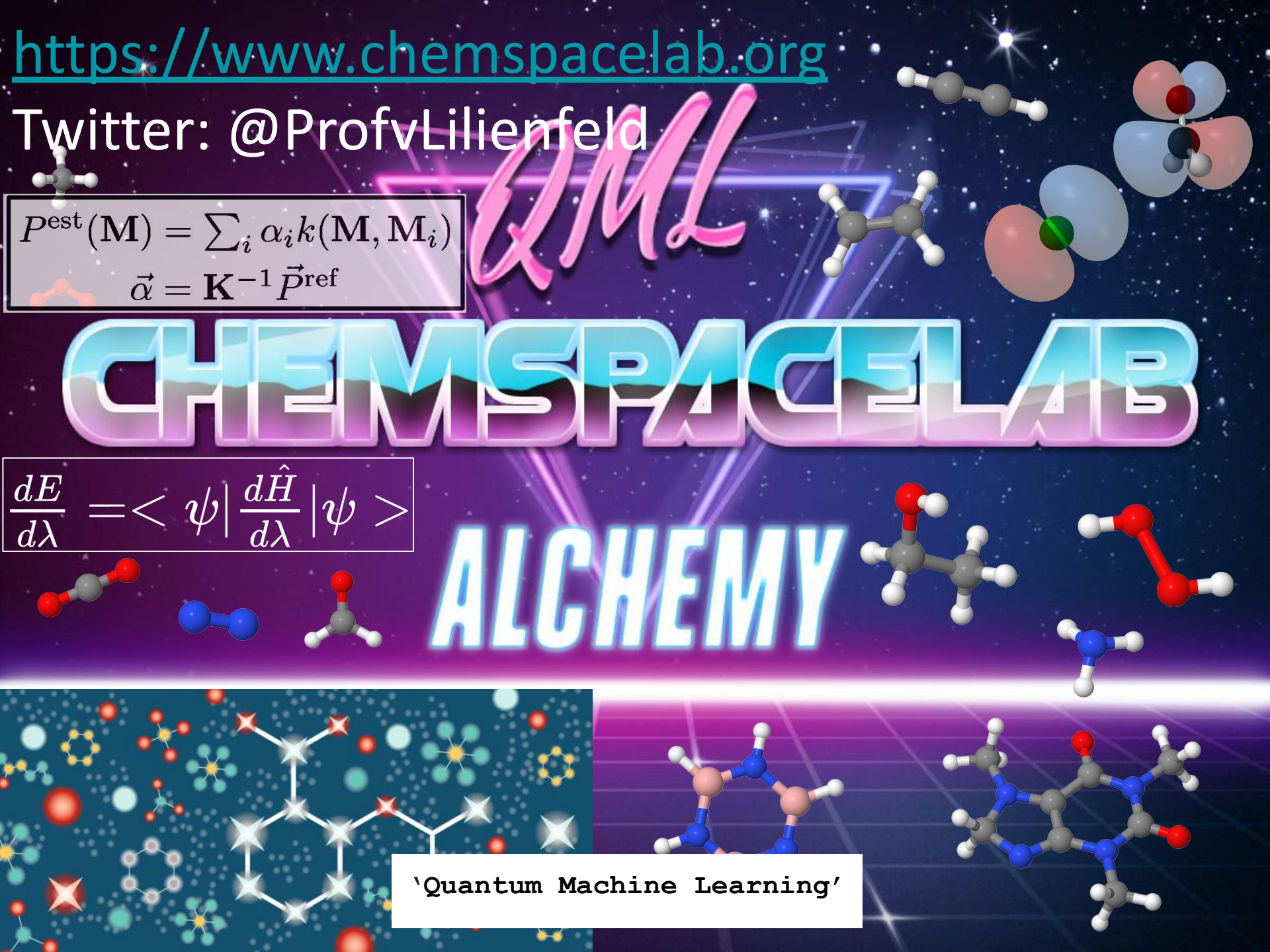

$$P^{\text{est}}(\mathbf{M}) = \sum_i \alpha_i k(\mathbf{M}, \mathbf{M}_i)$$


$$\vec{\alpha} = \mathbf{K}^{-1} \vec{P}^{\text{ref}}$$

$$\frac{dE}{d\lambda} = \langle \psi | \frac{d\hat{H}}{d\lambda} | \psi \rangle$$

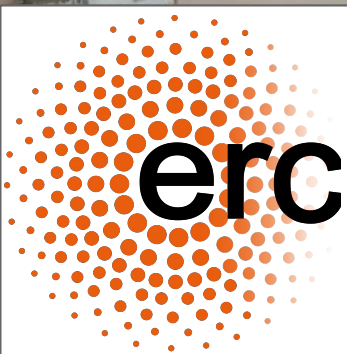
ALCHEMY

'Quantum Machine Learning'

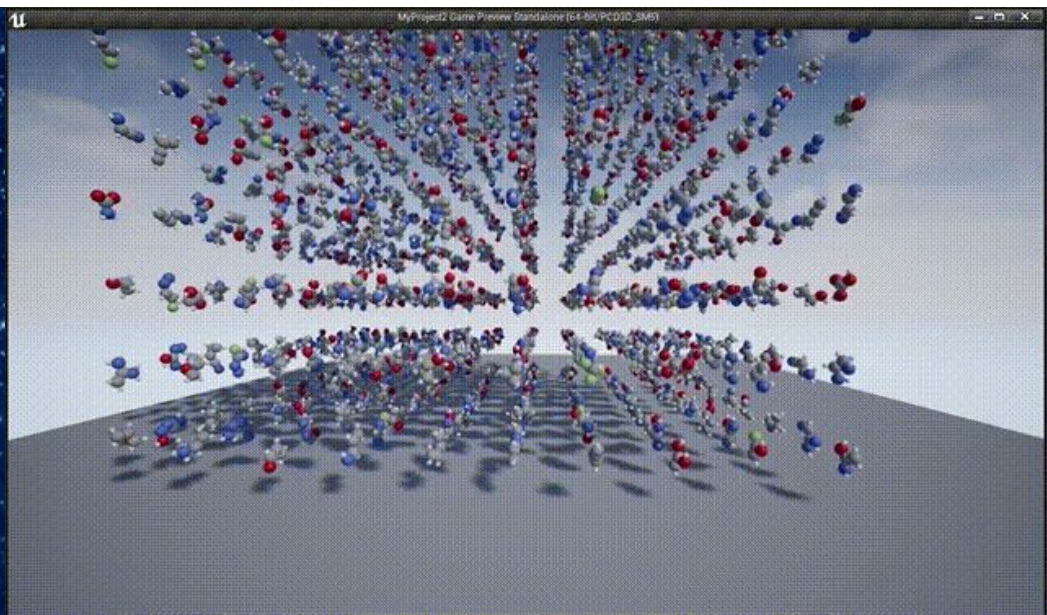
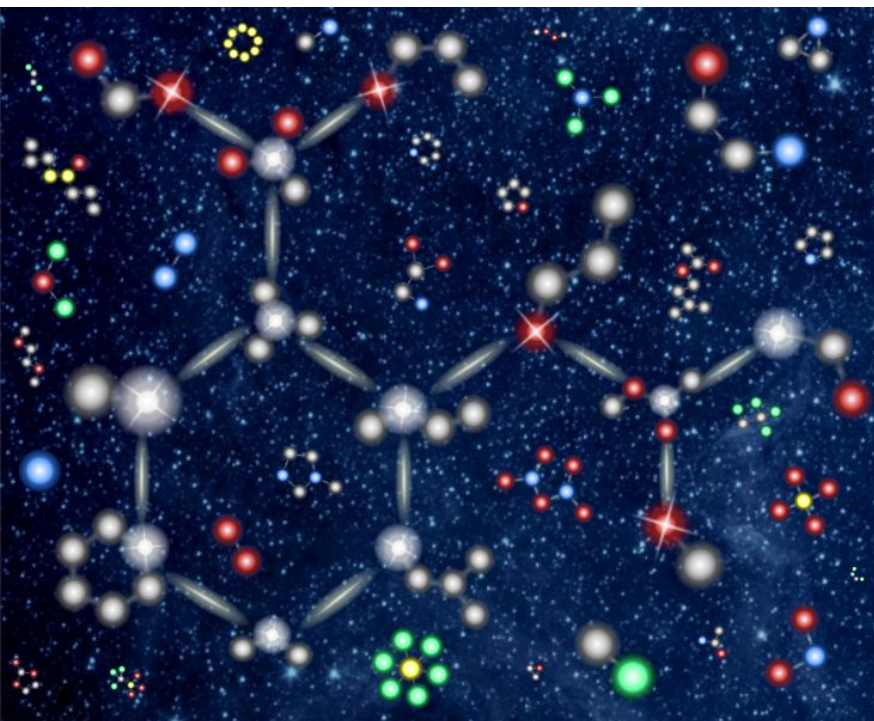




BIG-MAP



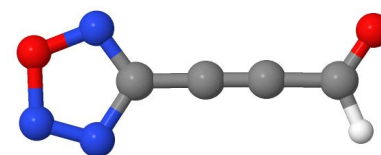
Ab initio view on chemical space



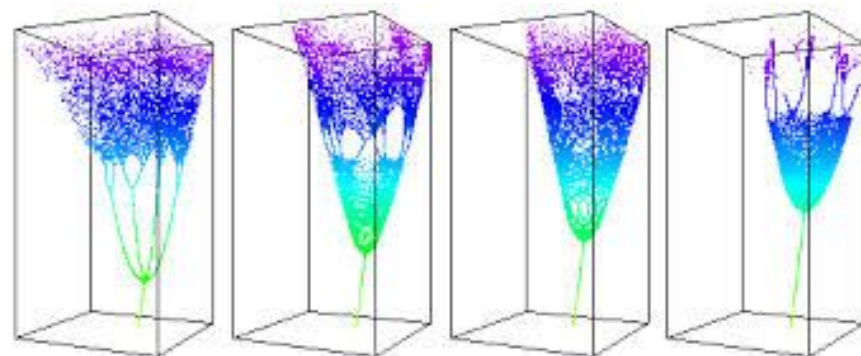
“Quantum machine learning using atom-in-molecule-based fragments selected on the fly”, Huang, von Lilienfeld,
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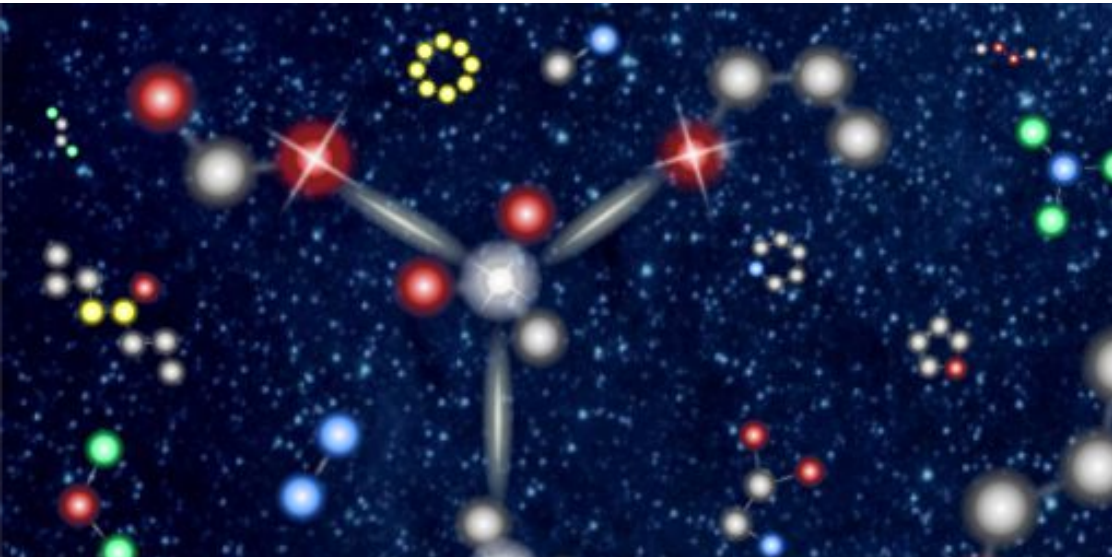
“Exploring **Chemical Compound Space** with Quantum-Based Machine Learning”, von Lilienfeld, Muller, Tkatchenko,
Nature Chemistry Reviews (2020)

“Ab initio machine learning in **chemical compound space**”, Huang, von Lilienfeld,
Chem Rev (2021)



→ **Quantum Compound Space** inherently
multi-scale: Composition/Constitution/Conformation
(reminiscent of fractal geometry)





Questions?

“Exploring Chemical Compound Space with Quantum-Based Machine Learning”, von Lilienfeld, Muller, Tkatchenko, *accepted in Nature Chemistry Reviews* (2019)